

**Addition Strategies**

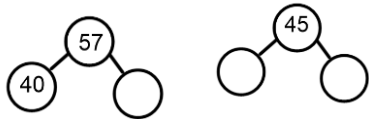
**Place Value**

Adding 1s, 10s to a 1 or 2 digit number. Use of part whole models and place value charts to show addition where no boundaries crossed:

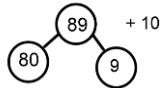
$20+3=$   
 $\underline{\quad} = 89+10$   
 $99+10=$   
 $68+20=$   
 $\underline{\quad} = 21+40$   
 $47+50=$

Part Whole Model/ PV Chart

Partition numbers to see which part will change following the calculation. Also, partition in as many ways as you can (50+7, 40+17, 30+27 etc) or give part whole with one of the parts missing.



$89 + 10 =$



OR

t	o
8	9

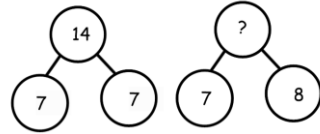
Unitising

Use of unitising language:  
**3 ones + 4 ones = 7 ones**  
**3 tens + 4 tens = 7 tens**

**Known facts**

(number bonds, near bonds, doubles, near doubles)

$7+8=$



Addition of 3 single digits:  
 **$8+5+4$ ;  $4+5+6$ ;  $15+3+3$ ;  $5+10+5$ .**

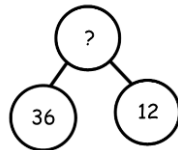
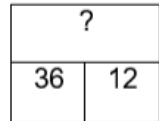
Unitising

Addition of multiples of 10:  
 **$4 \text{ ones} + 3 \text{ ones} = 7 \text{ ones}$**   
 **$3 \text{ tens} + 4 \text{ tens} = 7 \text{ tens}$**   
 **$40+30$**   
**Also,**  
 **$20+30+50$ .**  
 **$10+40+20$ .**

Addition of single digits and multiples of 10:  
 **$3+30+3$**   
 **$40+30+2$**   
 **$20+5+3+30$**

Exploring Relationships

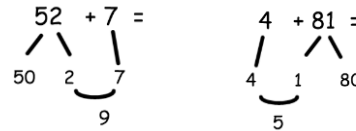
$\underline{\quad} - 12 = 36$



**Partitioning**

Single digit to 2-digit number (no crossing):

$22+7$   
 $5+32$   
 $99+1$



Single digit to 2-digit number (no crossing):

$46+7$   
 $37+5$   
 $7+84$   
 $97+5$   
 $98+4$

Addition of 2 two digit numbers (no crossing):

$54+22$   
 $84+12$

Addition of 2 two digit numbers (bond to 10):

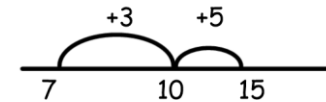
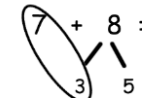
$67+33$   
 $23+37$   
 $36+24$   
 $69+11$

Addition of 2 two digit numbers (crossing tens) – some examples crossing 100.  
 $43+38$ ;  $55+17$ ;  $17+48$ ;  $52+29$ ;  $22+22$ .

**Bridging**

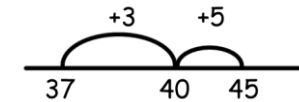
2 single digit numbers:

$9+4$   
 $9+5$   
 $7+8$   
 $8+6$



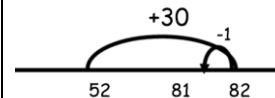
Single digit to 2-digit number:

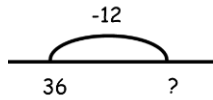
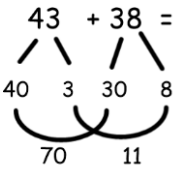
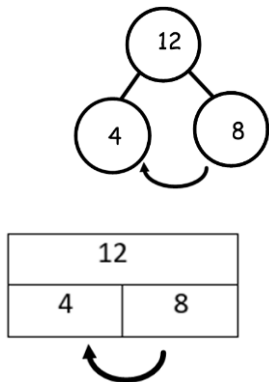
$46+7$   
 $37+5$   
 $7+84$   
 $97+5$   
 $98+4$



**Compensations/Adjustment (manipulation of numbers)**

$6+9=$   
 $52+29$



<p><u>Number Sequences</u></p> <p>___, ___, <b>57, 67</b>, ___ <i>etc.</i></p>	 <p>Write the inverse calculation to check it. (Known facts to be reused in partitioning and bridging strategies).</p>		<p><u>Manipulation</u></p> <p>Mentally move one digit to calculate</p> <p><math>4+8= \text{___} +7</math>  <math>4+8 &gt; \text{___} +7</math>  <math>4+8 &lt; \text{___} +7</math></p> <p>Relies on previous use of visuals with concrete apparatus to show how parts of numbers can be moved to make equivalent calculations:</p> <p><math>4+8=</math>  <math>5+7=</math>  <math>6+6=</math>  <math>7+5=</math></p> 
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## Subtraction Strategies

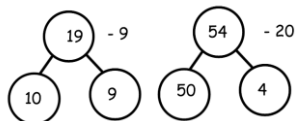
**Place Value**

Subtracting 1s, 10s from a 1 or 2 digit number. Use of part whole models and place value charts to show subtraction where no boundaries crossed:

$6-4$

$19-9$

$18-8$



$54-20$

$39-20$

$87-40$

$92-60$

$63-10-10$

t	o
5	4

(Or counters/dienes drawn in).

**Known facts**

$\underline{\quad} + 5 = 9$

$\underline{\quad} + 8 = 20$

**Unitising**

$8 \text{ ones} - 1 \text{ one} = 7 \text{ ones}$

$8 \text{ tens} - 1 \text{ ten} = 7 \text{ tens}$

Subtracting multiples of ten:

$80-10$

$10+20$

$90-80$

$100-10$

$50 + \underline{\quad} = 80$

$20 + \underline{\quad} = 70$

$50 - \underline{\quad} = 20$

**Partitioning**

Single digit from 2-digit number

$17-6$

$88-4$

$39-8$

$\underline{\quad} = 15-2$

$\underline{\quad} = 19-5$

$$\begin{array}{r} 88 \\ \diagdown \quad \diagup \\ 80 \quad 8 \end{array} - 4 =$$

Subtraction of single digit from multiple of ten. (Needed for bridging):

$70-8$

$100 - \underline{\quad} = 52$

$$\begin{array}{r} 70 \\ \diagdown \quad \diagup \\ 60 \quad 10 \end{array} - 8 =$$

Also draw place value counters and show on 100 squares.

Subtraction of 2 two digit numbers (bond to 10):

$70-18$

$$\begin{array}{r} \quad -8 \quad -10 \\ \hline 52 \quad 60 \quad 70 \end{array}$$

(Also draw place value counters).

Subtraction of 2 two digit numbers (no crossing):

$86-21$

$85-21$

$64-11$

Also use place value charts.

**Bridging**

Subtraction of single digit from 2 digit.

$12-7$

$18-6$

$63-4$

$43-5$

$54-8$

$$\begin{array}{r} 63 \\ \diagdown \quad \diagup \\ 3 \quad 1 \end{array} - 4 =$$

$$\begin{array}{r} \quad -1 \quad -3 \\ \hline 59 \quad 60 \quad 63 \end{array}$$

Subtraction of 2 two digit numbers (crossing tens):

$73-19$

$62-54$

$71-14$

$91-48$

$59-15$

$74-47$

$$\begin{array}{r} \quad -3 \quad -1 \quad -10 \\ \hline 27 \quad 30 \quad 31 \quad 41 \end{array}$$

**Counting on (difference):**

Subtraction of 2 two digit numbers (crossing tens):

$73-19$

$62-54$

$71-14$

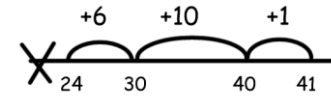
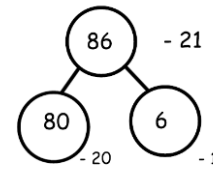
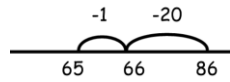
$91-48$

$59-15$

$74-47$

Take 24 from the start of the bar model/ number line and count on.

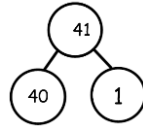
	41
24	



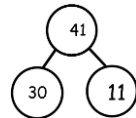
Subtraction of 2 two digit numbers (crossing tens):

- 41-24
- 73-19
- 62-54
- 71-14
- 91-48
- 59-15
- 74-47.

41-24 =



Tens	Ones



Tens	Ones

-20 -4

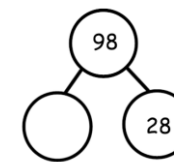
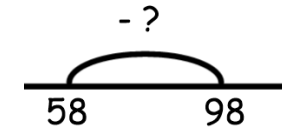
Tens	Ones

-10 -4

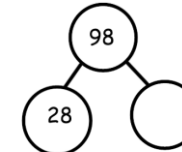
**Exploring inverse relationships:**

Through addition, subtraction work, use range of visuals to explore subtraction as counting back and counting on (difference).

- 10-\_\_=2;
- 3+\_\_+6=16
- 98-\_\_=28;
- 56-\_\_=51.
- 65+\_\_=93
- 28+\_\_=35



98	
	28



98	
28	

### Multiplication Strategies

#### Place Value and known facts (see also scaling)

Multiplying by 0 and by 1.  
2 x 0; 1 x 9

**8x10**  
**10x9=**  
**6x10=**  
**3x10=**  
**10x10=**

How many ways can you solve?

$$\underline{\quad} \times \underline{\quad} = 40.$$

Which numbers couldn't it be?  
Why not?

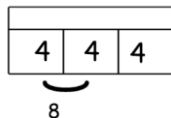
See Times Table Programme of  
Study for further examples.

#### Doubles/Halving/Tripling

**7x2=**  
**3x2=**  
**6x2=**  
Show link to doubling on arrays.

Tripling as well as counting in 3s:  
Double then bridge to add on last  
multiple.

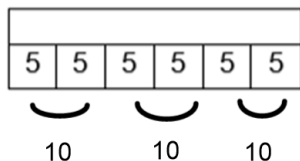
**3x3**  
**8x3**  
**6x3.**



Find, x5 by using relationship to  
10s.

**5x8**  
**5x12**

**5x6**



**10x5=**  
**20x5=**

#### Partitioning (Distributive Law)

Use arrays to explore

$$\underline{\mathbf{3}} \times \underline{\mathbf{2}} + \underline{\mathbf{2}} \times \underline{\mathbf{2}} =$$

How many ways can you solve?

$$\mathbf{7x5} = \underline{\quad} \times \mathbf{5} \text{ and } \underline{\quad} \times \mathbf{5}.$$

#### Scaling and Associated Language

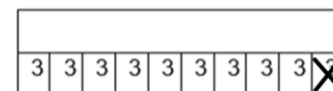
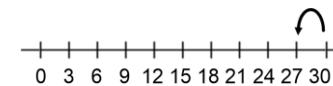
Across tables, use language of  
scaling.

3x10 means 10 lots of 3 or 3 ten  
times. Show both on part whole  
and bar models and number lines  
(See Times table Programme of  
Study).

**Make 3 ten times bigger.**  
**Make 6 twice the size/twice as  
big.**  
**Show me 4 five times. Write the  
calculation.**

#### Compensation

9 x 8, use counting stick, draw  
number line and use bar models  
and part whole models to show  
relationship between 10x and 9x.  
Use same strategy to help find 11x  
or 12x.



### Division Strategies

#### Place value and known facts

Explore both grouping/Sharing (See Times Table Programme of Study).

$$\begin{aligned} 35 \div 1 \\ 50 \div 1 \\ 5 \div 5 \\ 10 \div 10 \end{aligned}$$

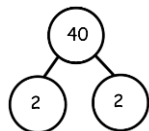
$$\begin{aligned} 40 \div 10 = \\ 80 \div 10 = \\ 120 \div 10 = \end{aligned}$$

(Use of unitising language – 12 tens  $\div$  10).

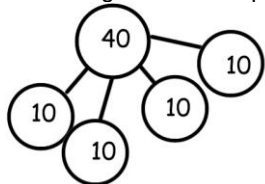
#### Grouping/Sharing

Begin to make decision about whether to share or group in arithmetic situation.

E.g. E.g.  $40 \div 2$ , more efficient to share (halve) rather than group in twos.



E.g.  $40 \div 10$ . More efficient to take away groups of 10 rather than sharing between 10 people.



#### Halving

Methods should involve discussion about division by 2 as halving.

$$\begin{aligned} 2 \div 2 = \\ 8 \div 2 = \\ 12 \div 2 = \\ 14 \div 2 = \end{aligned}$$

Use arrays, part whole model and bar models.

#### Scaling and Associated Language

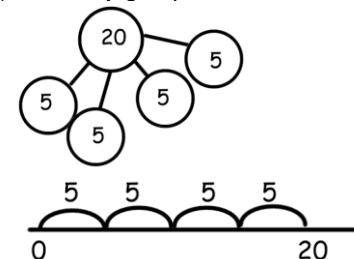
Divide by 10, make 10 times smaller/10 times as small.  
Divide by 2, half as many/much.

$$\begin{aligned} 40 \div 10 \\ 80 \div 10 \\ 120 \div 10 \end{aligned}$$

Explore relationships with part whole models, bar models and number lines.

$$\underline{\quad} \times 5 = 20$$

(How many groups of five are in 20).

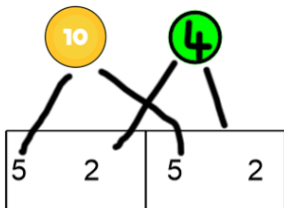


## Fractions Strategies.

Half of numbers to 20.  
Halve the ten then halve the ones.

$$\frac{1}{2} \text{ of } 14$$

$$\frac{1}{2} \text{ of } 16$$



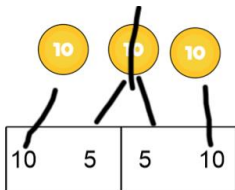
Halves of multiples of 10.

$$\frac{1}{2} \text{ of } 20$$

$$\frac{1}{2} \text{ of } 30$$

$$\frac{1}{2} \text{ of } 40$$

$$\frac{1}{2} \text{ of } 90$$



Find quarters by halving and halving again.

16			
8		8	
4	4	4	4

Use bar model to find two quarters or three quarters.

$$\frac{3}{4} \text{ of } 16;$$

$$\frac{3}{4} \text{ of } 20;$$

$$\frac{2}{4} \text{ of } 36.$$

16			
8		8	
4	4	4	4

$$\frac{1}{4} \text{ of } 100=$$

$$\frac{3}{4} \text{ of } 100=$$

$$\frac{1}{3} \text{ of } 6$$

$$\frac{1}{3} \text{ of } 12$$

$$\frac{1}{3} \text{ of } 30$$

$$\frac{1}{3} \text{ of } 21$$

Share out 12 between 3 (count rows in threes to check).

12		

x	x	x
x	x	x
x	x	x
x	x	x