

**Addition Strategies**

**Place Value and Known Facts**

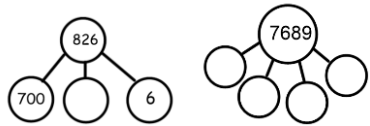
Adding 1s, 10s, 100s, 1000s, 10,000s, 100,000s, 0.1s, 0.01s and 0.001s to larger/smaller numbers. Use of part whole models and place value charts to show addition where no boundaries are crossed:

$435 + 30 = \underline{\quad}$   
 $40 + 1000 = \underline{\quad}$   
 $\underline{\quad} = 6000 + 90$   
 $789 + 100 = \underline{\quad}$   
 $0.7 + 3.014 = \underline{\quad}$

Part Whole Model

Partition numbers in as many ways as you can, or give part whole with one of the parts missing.

$3,050020 = 3,000,000 + \underline{\quad} + 20$   
 $826 = 700 + \underline{\quad} + 6$



Place Value Chart with Counters or Digits

e.g  $2.001 + 3.12$

o	0.1	0.01	0.001
•			
•			
•	•	•	•

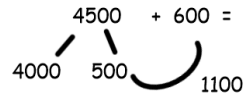
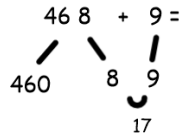
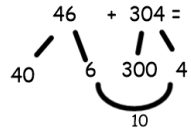
Complements

Include revision of complements to 100 and how these relate to complements to powers of 10.

E.g.  $56 + \underline{\quad} = 100$   
 $560 + \underline{\quad} = 1000$   
 (56 tens +  $\underline{\quad}$  tens = 100 tens).

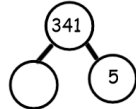
**Partitioning**

Involves number bonds, doubles, near doubles, bridging strategies

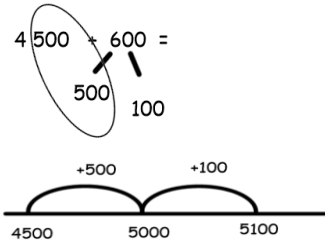
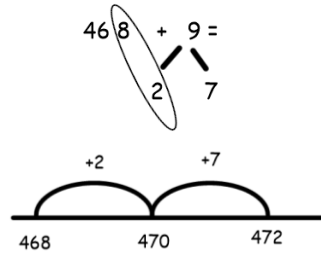


Explore Addition/Subtraction Relationships (inverse)

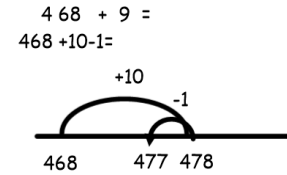
$\underline{\quad} + 5 = 341$



**Bridging**



**Compensations/ Adjustment (Manipulation of Numbers)**



OR

$468 + 9 =$   
Mentally move one from 468 to 9, so  $467 + 10$ .

$122,456 + 11,999 =$   
 $122,456 + 12,000 - 1$  (show on number line)  
Or  $122,455 + 12,000$  (mentally move the one).

Also include:

- $+199$
  - $+999$
  - $+\pounds 1.99$  etc
- Examples where need to **adjust by 3, 4, 5 etc** (e.g.  $457 + 95$ ).  
 $2.7 + 3.014$

Manipulation:

Mentally move one digit to calculate

$39 + \underline{\quad} = \underline{\quad} + 40$   
 $248 + \underline{\quad} = 46 + 247$   
 $2.7 + 3.014 = 2 + \underline{\quad}$

**Column Methods**

$\underline{\quad} = 936 + 285$

$\underline{\quad} = 8275 + 82$

$707 + 1818 =$

$15.98 + 26.314 = \underline{\quad}$

Missing Number Problems/ What is My Mistake?'

2	6	2	□	6
+	5	8	2	□
□	2	0	5	4

Write inverse (column) calculation to check addition/subtraction column calculation.

And how they relate to complements to other multiples of 100.

E.g.

$$\begin{array}{|c|c|c|} \hline & 8 & \\ \hline \end{array} + \begin{array}{|c|c|c|} \hline & 8 & \\ \hline \end{array} = \begin{array}{|c|} \hline 200 \\ \hline \end{array}$$

Link to complements to 1 with tenths, complements to 0.1 with hundredths in context of decimals).

#### Unitising

Unitising language when boundaries crossed:

$$\begin{array}{r} \underline{\quad} = 3936 + 200 \\ \quad \swarrow \quad \searrow \\ 3900 \quad 36 \end{array}$$

39 hundreds + 2 hundreds +36 =41 hundreds +36

#### Number Sequences

**4856, 4956, \_\_\_\_\_, \_\_\_\_\_** etc.

Include negative numbers.

E.g. -17, -12, -7, \_\_\_\_\_, \_\_\_\_\_.

341	
	5

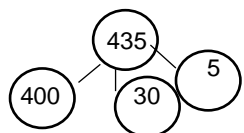
Write inverse calculation to check addition/subtraction calculation.

**Subtraction Strategies**

**Place Value/ Known Facts**

Subtracting 1s, 10s, 100s, 1000s, 10,000s, 100,000s, 0.1s, 0.01s and 0.001s from larger/smaller numbers. Use of part whole models and place value charts to show subtraction where no boundaries are crossed:

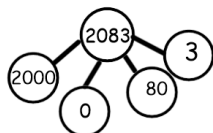
$\underline{\quad} = 435 - 30$



**Unitising**

Unitising language when boundaries crossed:

$2083 - 300 =$



$2000 = 300 =$   
20 hundreds - 3 hundreds.

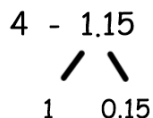
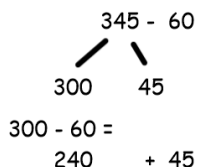
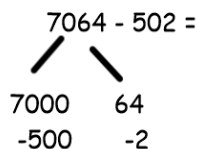
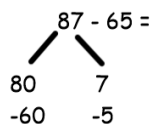
**Explore Relationships**

$\underline{\quad} - 10 = 298$   
 $\underline{\quad} - 100 = 1059$

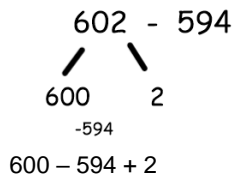
?	
1059	100

**Partitioning**

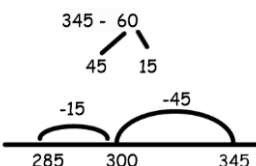
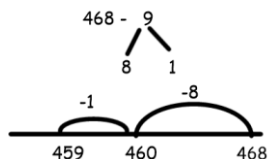
Including halving/near halves



$4 - 1 = 3$   
 $3 - 0.15$  (use knowledge of complements to 100).



**Bridging**

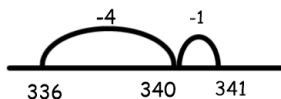


**Explore Addition/Subtraction Relationships (inverse)**

$\underline{\quad} + 5 = 341$

Explore parts and whole relationship on bar model or part whole then solve.

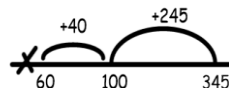
341	
	5



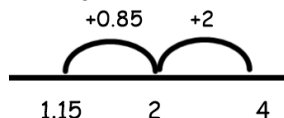
**Difference/Comparison/ Counting On**

$345 - 60 =$

345	
60	

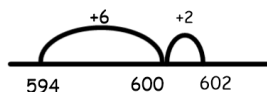


$4 - 1.15 =$

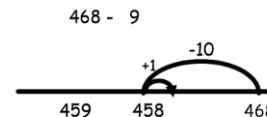


$602 - \underline{\quad} = 594$

Explore parts and whole on bar model, then use number line or mental method to count up.



**Compensations/Adjustment (Manipulation of Numbers)**



$9 - 1.9 = 9 - 2 + 0.1$

**Constant Difference**

Discussion point as it works in a different way to addition. The difference between 21 and 29 is the same as the difference between 20 and 28 so  $29 - 21 = 28 - 20$ .



$5000 - 2356$  as formal method can be difficult, so make equivalent calculation,  $4999 - 2355 =$

$122,456 - 11,999 =$   
 $122,456 - 12,000 + 1$   
OR  $122,457 - 12,000$

**Column Methods**

$4912 - 824 =$

$7064 - 502 =$

$\underline{\quad} = 5776 - 855$

$37.8 - 14.671$

$5.87 - 3.123$

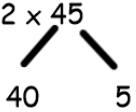
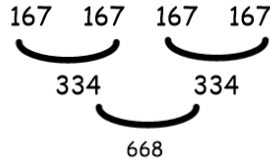
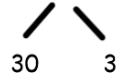
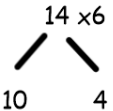
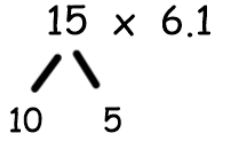
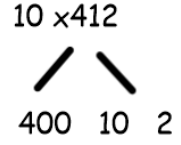
**Missing Number Problems/ What is My Mistake?**

Include these questions and use part whole model and PV grid to show exchange alongside column method.

Write the addition to check the given column subtraction calculation.

## Number Talk Strategies Year 6

## Multiplication Strategies

<u>Place Value and Known Facts</u> (Also see Scaling)	<u>Doubling//Halving/Tripling</u>	<u>Partitioning</u> (Distributive Law)	<u>Scaling and Associated Language</u>	<u>Associative Law</u>	<u>Written Methods</u>								
<p><math>213 \times 0</math></p> <p><math>1 \times 314</math></p> <p><u>PV Counters</u> Use PV counters (tens) to show relationship between <math>3 \times 40</math> and <math>30 \times 40</math>. Link to scaling – make <math>30 \times 4</math> ten times greater.</p> <p><math>30 \times 4</math> <math>30 \times 40</math> <math>5 \times 70</math> <math>50 \times 70</math></p> <p>Include decimals</p> <p><math>0.3 \times 4</math> <math>0.03 \times 4</math></p> <p><math>6^2 + 10</math> <math>3^3 + 10</math> Revise regularly known facts within 100 and links to larger powers of 10 and also decimals. Show links (e.g. halving 25 to find 12.5) on bar models.</p> <table border="1" data-bbox="129 1118 412 1259"> <tr> <td><math>\_ \times 2 = 100.</math></td> <td><math>\_ \times 2 = 1</math></td> </tr> <tr> <td><math>\_ \times 4 = 100.</math></td> <td><math>\_ \times 4 = 1</math></td> </tr> <tr> <td><math>\_ \times 5 = 100</math></td> <td><math>\_ \times 5 = 1</math></td> </tr> <tr> <td><math>\_ \times 8 = 100.</math></td> <td><math>\_ \times 8 = 1</math></td> </tr> </table>	$\_ \times 2 = 100.$	$\_ \times 2 = 1$	$\_ \times 4 = 100.$	$\_ \times 4 = 1$	$\_ \times 5 = 100$	$\_ \times 5 = 1$	$\_ \times 8 = 100.$	$\_ \times 8 = 1$	<p><math>2 \times 45</math></p>  <p><math>16 \times 8 =</math> double <math>8 \times 8</math>.</p> <p><math>\times 4</math> - By doubling and doubling again <math>\times 8</math> - <math>\times 2, \times 2, \times 2</math></p> <p><math>167 \times 4</math></p>  <p>Or partition and <math>\times</math> all parts by 4).</p> <p><u>Tripling</u></p> <p><math>8 \times 33</math></p>  <p>Triple 8 by doubling then adding one more (or use known facts). <math>8 \times 3 = 24</math> <math>80 \times 3 = 240</math>, so 264.</p> <p>OR <math>33 \times 2 \times 2 \times 2</math> (associative law) – doubling, doubling, doubling again.</p>	<p><math>14 \times 6 =</math></p>  <p><math>14 \times 6 = \_ \times 6 + \_ \times 6</math></p> <p><math>15 \times 6.1</math></p>  <p><math>10 \times 6.1 = 61</math> <math>5 \times 6.1 = 30.5</math></p> <p><u>Compensation</u> <math>9 \times 41 =</math> Use counting stick or draw number line and show <math>10 \times 41</math> then subtract <math>(1 \times 41)</math>.</p>	<p>Across tables, use language of scaling.</p> <p><math>3 \times 10</math> means 10 lots of 3 or 3 ten times. Show both on part whole and bar models and number lines (See Times table Programme of Study).</p> <p><b>Make 45 twice as big</b> <b>Make 45 four times larger.</b> <b>Make 41 ten times greater.</b> <b>Make 45 eight times larger.</b></p> <p><math>41 \times 10</math> <math>41 \times 100</math> <math>2345 \times 1000</math> <math>25.34 \times 10</math></p> <p><u>PV Counters</u> Use PV chart and counters to show making each counter ten times its value (<math>\times 100 = \times 10</math>, then <math>\times 10</math>).</p> 	<p><math>5 \times 4 \times 10</math> See Times Table Programme of study for examples of visuals</p> <p><math>30 \times 40</math> <math>50 \times 70</math></p> <p>Explore visually how <math>3 \times 40 = 3 \times 10 \times 4</math> then scale up to <math>30 \times 40 = 30 \times 4 \times 10</math>.</p> <p><math>0.9 \times 200 = 0.9 \times 100 \times 2</math>. (Show on place value grid).</p> <p><math>0.5 \times 28</math></p> <p><math>3.9 \times 30 = 3.9 \times 3 \times 10</math></p>	<p><math>879 \times 3</math></p> <p><math>418 \times 6</math></p> <p><math>541 \times 8</math></p> <p><math>3468 \times 6</math></p> <p><math>836 \times 7</math></p> <p><math>71 \times 46</math></p> <p><math>785 \times 23</math></p> <p><math>5413 \times 86</math></p> <p>Include missing numbers in column methods.</p>
$\_ \times 2 = 100.$	$\_ \times 2 = 1$												
$\_ \times 4 = 100.$	$\_ \times 4 = 1$												
$\_ \times 5 = 100$	$\_ \times 5 = 1$												
$\_ \times 8 = 100.$	$\_ \times 8 = 1$												

**71 x 8**

Find  $71 \times 4$  and double it  
(show relationship between  $\times 4$  and  $\times 8$  on bar model).

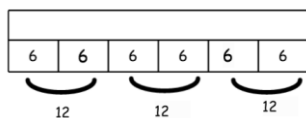
Find  $\times 20$  by doubling  $\times 10$

$\times 5$  by halving  $\times 10$ .

Explore Relationships

E.g.  $\times 4$ ,  $\times 8 / \times 6$ ,  $\times 12 / \times 3$ ,  $\times 6$

E.g.  $6 \times 6$



**14 x 3 =** \_\_\_ x 6 etc.

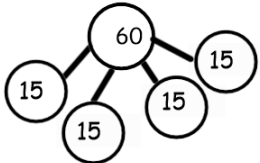
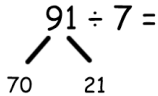
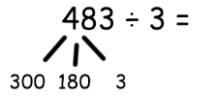
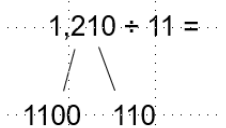
(See Scaling for halving  
examples -  
cover halves of multiples of  
10, 100, 1000 etc.)

Cover decimals facts.

**Double 0.7, 0.9 etc.**



## Division Strategies

<u>Place Value and Known Facts</u>	<u>Halving/Halving Again</u>	<u>Partitioning</u>	<u>Scaling and Associated Language</u>	<u>Associative Law</u>	<u>Written Methods</u>																																
<p><math>326 \div 1</math>  <math>838 \div 1</math>  <math>505 \div 1</math></p> <p><math>99 \div 11</math>  <math>120 \div 12</math></p> <p><u>Unitising</u>            Use of unitising language  <math>180 \div 3</math>            (18 tens <math>\div 3 = 6</math> tens). Use tens counters to <u>share</u>.  <math>270 \div 3</math>  <math>72 \div 9</math>  <math>720 \div 9</math>  <math>5400 \div 9</math>  <math>1210 \div 11 =</math>            121 tens <math>\div 11 = 11</math> tens            (known facts)</p> <p><u>Grouping/Sharing</u>            Make decision about whether to share or group.  <math>60 \div 15 =</math> (by grouping)</p>  <p><math>100 \div 25</math>  <math>200 \div 25</math></p>	<p>Divide by 4 by halving and halving again:  <math>96 \div 4 =</math>  <math>96 \div 2 \div 2</math> (half and half again).</p> <table border="1" data-bbox="459 427 743 515"> <tr><td colspan="4">328</td></tr> <tr><td colspan="2">164</td><td colspan="2">164</td></tr> <tr><td>82</td><td>82</td><td>82</td><td>82</td></tr> </table> <p>Include decimals facts.</p> <p><i>Find half of 0.3</i>  <i>Find half of 0.5</i>  <i>Find half of 0.7</i></p>	328				164		164		82	82	82	82	<p><math>91 \div 7 =</math></p>  <p><math>70 \div 7 = 10</math>  <math>21 \div 7 = 3</math></p> <p><math>95 \div 5</math>  <math>96 \div 8</math>  <math>96 \div 4</math></p> <p><math>483 \div 3 =</math></p>  <p><math>300 \div 3 = 100</math>  <math>180 \div 3 = 60</math>  <math>3 \div 3 = 1</math></p> <p><math>1,210 \div 11 =</math></p>  <p><math>1100 \div 11 = 100</math>  <math>110 \div 11 = 10</math></p> <p><u>Compensation</u>  <math>95 \div 5 =</math>  <math>100 \div 5 = 20 - (1 \times 5)</math>,            so 19 lots of 5 in 95.</p>	<p><i>Divide by 10 or 100 etc, make 10 times smaller/10 times as small.</i></p> <p><math>60 \div 10</math></p> <p><math>486 \div 10</math></p> <p>Divide by 100 by dividing by 10 and 10 again. Show on place value chart (once covered decimals)</p> <p><math>58 \div 10</math>  <math>58 \div 100</math>  <math>0.9 \div 10</math>  <math>0.04 \div 10</math>  <math>0.1 \div 100</math></p> <p>Link to decimals  <math>0.5 \times 48</math>            (Half of 48)  <math>1.5 \times 48</math>            (1 x 28 + half of 48)</p>	<p><u>Divide by 5</u> by dividing by 10 and doubling.</p> <p><u>Divide by 8</u> by dividing by 4 and halving.</p> <p><u>Divide by 6</u> by dividing by 3 and halving.</p> <p><u>Divide by 20</u> by dividing by 10 and halving</p> <p>Show on number lines, arrays and bar models.</p> <p><math>545 \div 5</math>            Show on bar model, divide by 10 and double.</p> <table border="1" data-bbox="1458 758 1776 837"> <tr><td colspan="10">545</td></tr> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> </table>	545																				<p><math>486 \div 3</math></p> <p><math>1320 \div 12</math></p> <p><math>725 \div 29</math></p> <p><math>2242 \div 59</math></p> <p>Use alongside partitioning methods to develop conceptual understanding.</p>
328																																					
164		164																																			
82	82	82	82																																		
545																																					

### Fraction Strategies

#### Known Facts and Complements to 1

Revise known facts:

$\frac{1}{2}, \frac{1}{4}, \frac{3}{4}, \frac{1}{5}, \frac{1}{8}$  of 100 with links to 1000 and 1 (decimals).

$$\frac{2}{10} + \frac{5}{10} + \frac{3}{10} = 1$$

$$\frac{9}{11} - \frac{4}{11} =$$

$$1 - \frac{1}{10} =$$

$$1 - \frac{1}{10} =$$

#### Going Over 1 Whole

$$2 \frac{1}{6} + \frac{5}{6} =$$

$$1 \frac{1}{3} - \frac{1}{3} =$$

$$1 \frac{1}{5} + 2 \frac{1}{5} =$$

$$1 \frac{5}{8} - \frac{2}{8} =$$

$$1 \frac{1}{5} - \frac{2}{5} =$$

#### Ordering/Comparing

$$\frac{1}{5}, \frac{1}{10}, \frac{1}{100}$$

$$\frac{2}{5}, \frac{2}{10}, \frac{2}{100}$$

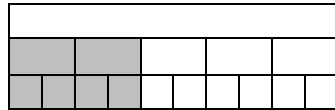
Write the fraction which is closest to 1.

$$\frac{99}{100}, \frac{49}{50}, \frac{19}{20}$$

#### Visual Representations

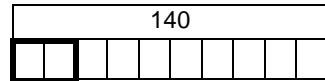
$$\frac{2}{5} = \frac{\quad}{10}$$

Draw bar model to find out



$$\frac{2}{5} \times 140$$

Show on bar model, divide by 10 and double.

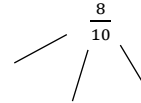


Continue fraction sequences where same fraction added each time. Use bar model to demonstrate.

$$-, \frac{3}{5}, 1 \frac{2}{10}, 1 \frac{8}{100}, -$$

#### Partitioning

How many ways can you partition  $\frac{8}{10}$ ?

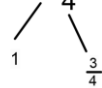


etc

Bar Model.

$$\frac{4}{7} + \frac{5}{7} =$$

$$1 \frac{3}{4} \times 10$$



$$1 \times 10 + \frac{3}{4} \text{ of } 10$$

#### Scaling and Associated Language

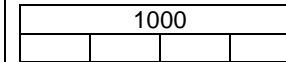
$$\frac{1}{4} \text{ of } 100 =$$

$$\frac{3}{4} \text{ of } 100 =$$

$$\frac{1}{4} \text{ of } 1000 =$$

$$\frac{3}{4} \text{ of } 1000 =$$

Relate to all powers ten and scale up to 200, 300 etc.



$$\frac{1}{2} \times 26 =$$

$$1 \frac{1}{2} \times 40 =$$

$$\frac{1}{5} \times 25 =$$

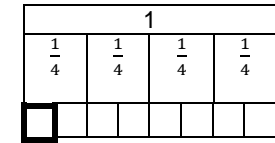
$$1 \frac{3}{4} \times 10 =$$

#### Written Methods

Make use of doubling, halving and visuals alongside these.

$$\frac{1}{4} \div 2 = \frac{1}{4} \times \frac{1}{2}$$

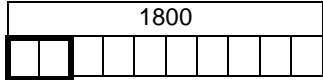
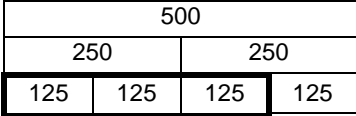
OR  $\frac{1}{4} \div 2$  (is the same as half of  $\frac{1}{4}$ )



$$\frac{3}{10} - \frac{1}{20}$$

$$\frac{3}{10} - \frac{1}{20}$$

$$\frac{2}{5} \text{ of } 140 =$$

Percentages Strategies (Teaching note – use x as well as ‘of’)			
Known Facts/Scaling	Visual Representations	Partitioning	Compensation/Adjustment
<p>Know 25%, 50%, 75% are equivalent to <math>\frac{1}{4}</math>, <math>\frac{1}{2}</math>, <math>\frac{3}{4}</math>.</p> <p>Know 25%, 50%, 75% of 100, 1000 and 1 (decimal equivalents). Use of halving and halving again strategy. Link to 10,000, 100,000 etc.</p> <p>Find 5% by halving 10%.</p> <p>Use 1%, 5%, 10% and 20% to find any percentage.</p> <p><b>7% of 500</b> 1% of 500, then x 7 7% of 100, then x 5.</p>	<p><b>20% of 1800 =</b> Show on bar model, divide by 10 and double.</p> 	<p>Find 25%, 50% and 75% of whole numbers (using knowledge for halving/quartering by halving and halving again etc).</p> <p><b>75% x 500</b></p>  <p>Use of 10% to find percentages which are multiples of 10.</p> <p>Use of 10% and doubling to find 20%, 40%, 80% through use of 10% and doubling or through finding <math>\frac{1}{5}</math>, <math>\frac{2}{5}</math>, <math>\frac{4}{5}</math>.</p> <p>Use 10% and 5% to find 15%, 35% etc.</p> <p><b>15% of 440 =</b> 10% of 440 + 5% of 440</p> <p><b>28% of 650 =</b> Find 20% then 8%.</p>	<p><b>90% of 200</b> Find 10% and subtract.</p> <p><b>99% of 200</b> Find 1% and subtract.</p> <p><b>40% of 460.</b> Find 50% then take away 10%.</p> <p><b>99% of 200.</b> Find 1% and subtract from 100%</p> <p><b>45% of 460.</b> Find 50% then take away 5%.</p> <p><b>51% x 900.</b> Find half (50%), then find 1% and add them together</p>