## AQA GCSE Maths 8300

## **Topic List - FOUNDATION**

	NUMBER	
N1	Order numbers	<ul> <li>□ Put in order of size, integers (whole numbers), decimals and fractions</li> <li>□ use the symbols =, ≠, &lt;, &gt;, ≤, and ≥</li> <li>□ Understand and use positive and negative numbers on a number line</li> </ul>
N2	Add, subtract, multiply, divide	<ul> <li>Add, subtract, multiply, and divide integers (whole numbers), decimals, simple fractions (including mixed numbers and improper fractions), both positive and negative</li> <li>Understand and use place value</li> <li>Understand the terms profit, loss, cost price, selling price, debit, credit, income tax, VAT and interest rate.</li> </ul>
N3	Operations	<ul> <li>Understand inverse (opposite) operations; x and ÷, + and -</li> <li>Use correct order of operations (BIDMAS)</li> <li>Be able to understand and use brackets, powers, roots and reciprocals</li> </ul>
N4	Factors, multiples and primes	Understand the terms; Prime number Factor Multiple Common factor Highest common factor Least (lowest) common multiple Express a number as a product of prime factors (factor tree) in index form and understand that this is unique for every number
N5	Listing and counting	List things in a systematic way
N6	Powers and roots	<ul> <li>Use positive integer powers and roots of numbers</li> <li>Recognise powers of 2, 3, 4 and 5</li> <li>Know square numbers up to 15<sup>2</sup></li> <li>Know that 10<sup>3</sup> = 1000 and that 10<sup>6</sup> = 1 million</li> </ul>

N7	Powers and roots and fractional indices	Calculate with roots and with whole number indices
N8	Exact calculations	<ul> <li>Calculate exactly with fractions</li> <li>Calculate exactly with multiples of π</li> </ul>
N9	Standard form	<ul> <li>Understand numbers written in standard form</li> <li>Calculate with numbers in standard form</li> </ul>
N10	Fractions and decimals	<ul> <li>Convert between fractions and decimals</li> <li>Be able to put fractions and decimals in order of size</li> </ul>
N11	Fractions and ratios	Be able to work with fractions in ratio problems
N12	Fractions and percentages	<ul> <li>Find a fraction of a quantity</li> <li>Find a percentage of a quantity</li> <li>Use a multiplier to increase of decrease a quantity (eg. use x 1.05 to increase by 5%, or 0.88 to decrease by 12%))</li> </ul>
N13	Units of measurement	<ul> <li>Be able to use units of mass, length, time, money and other measures, including using decimal amounts</li> <li>Convert between metric measurements of length</li> <li>Convert between metric measurements of area</li> <li>Convert between metric measurements of volume and capacity</li> <li>NB. Imperial (old) units to metric units do not need to be known, and conversions will be given in the question if required</li> </ul>
N14	Estimation	<ul> <li>Estimate answers (by rounding)</li> <li>Check calculations using approximation and estimation</li> </ul>
N15	Rounding	<ul> <li>□ Round to an appropriate degree of accuracy</li> <li>□ Round to a number of decimal places</li> <li>□ Round to a number of significant figures</li> <li>□ Use inequality signs to show an error interval due to rounding, eg. 8.5 ≤ a &lt; 9.5</li> <li>□ Know not to round in the middle of a calculation, but just to round the final answer</li> </ul>
N16		Understand and use limits of accuracy

	ALGEBRA	
A1	Basic notation	Understand and use algebraic notation, including ab, ab, 3a $a^2$ , $a^3$ , $a^2b$ , etc. $\frac{a}{b}$ Use fractions in algebra work instead of decimals Use brackets NB. Answers are expected to be given <u>in their simplest</u> form even when not asked to do so.
A2	Substitution	Substitute numbers into formulas, and expressions, including scientific formulas which may not have been seen before
A3	Algebraic terms	Understand and use the terms; Expression Equation Formula Inequality Term Factor Identity
A4	Manipulate algebra	<ul> <li>Simplify by collecting like terms</li> <li>Multiply out a single bracket</li> <li>Factorise a single bracket by taking out common factors</li> <li>Expand two brackets</li> <li>Factorise quadratics (with a single x<sup>2</sup>) into two brackets</li> <li>Factorise quadratics using the difference of two squares, eg. a<sup>2</sup> - 9 = (a + 3)(a - 3)</li> <li>Simplify algebraic expressions by adding, subtracting and multiplying</li> <li>Use index laws</li> </ul>
A5	Formulae	<ul> <li>Understand and use mathematical formulae</li> <li>Rearrange a formula to change the subject</li> </ul>

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A6	Expressions	☐ Know the difference between an equation, like $2x + 3 = 17$ , and an identity, like $2x \equiv x + x$
		Be able to show that two expressions are equal
A7	Functions	Understand functions with inputs and outputs
A8	Graphs	Work with graphs in all four quadrants (ie. with negative values as well as positive)
A9	Straight line graphs	Plot straight line graphs
		$\Box$ Use y = mx + c to find parallel graphs
		Find the equation of a line when given the gradient and one point
		Find the equation of a line when given two points
A10	Gradients and intercepts	Find and use gradients and intercepts of graphs
A11	Key features of graphs	Look at a quadratic graph and identify from it
		Roots (where a graph crosses the x axis)
		Intercept (where it crosses the y axis)
		Turning points
		☐ Find the roots of a quadratic using algebra
		Understand the symmetry of a quadratic graph
A12	Other graphs	Recognise, sketch or interpret other graphs, including
		$\Box$ Cubic functions (x <sup>3</sup> , etc.)
		$\Box$ Reciprocal functions ( $\frac{1}{x}$ , etc.)
A14	Real life graphs	Plot and interpret graphs of speed, distance and time
		Use graphs to find solutions with problems of speed, distance and acceleration
		Understand and use reciprocal graphs
		Understand and use exponential graphs
A17	Linear equations	Solve linear equations
		Solve equations with x on both sides
		Solve equations with brackets
		Find a solution to a linear equation by reading it from a graph

A18	Quadratic equations	<ul> <li>Solve quadratic equations by factorising into 2 brackets</li> <li>Find solutions to a quadratic equation by reading them from a graph</li> </ul>
A19	Simultaneous equations	<ul> <li>Solve simultaneous linear equations</li> <li>Find solutions simultaneous equations by reading them from a graph</li> </ul>
A21	Creating expressions and equations	<ul> <li>Create an expression from a word or shape problem</li> <li>Create an equation from a word or shape problem and solve it</li> </ul>
A22	Inequalities	<ul> <li>Solve linear inequalities</li> <li>Represent solutions to linear inequalities on a number line</li> <li>NB. On a number line, open circles and closed circles must be used correctly, and on a graph, dashed lines and solid lines must be used correctly.</li> </ul>
A23	Sequences	<ul> <li>Generate a sequence from a term-to-term rule or an nth term expression</li> <li>Generate a sequence from patterns</li> </ul>
A24	Sequences	Recognise and use sequences, including          Square numbers         Cube numbers         Triangular numbers         Arithmetic (linear) sequences         Fibonacci sequences         Simple geometric sequences (eg. doubling or multiplying each term by 3)
A25	Nth term of a sequence	Find the nth term of a linear sequence

	RATIO, PROPOR	TION AND RATES OF CHANGE
R1	Units	Change between units for Time Length Area Volume/capacity Mass Change between units for compound measures of Speed Rates of pay Density Pressure
R2	Scale	Use scale factors, scale diagrams and maps
R3	Finding a fraction	Express one quantity as a fraction of another NB. The result may also be greater than one or a top- heavy fraction.
R4	Simple ratios	<ul> <li>Use ratio notation</li> <li>Simplify a ratio</li> </ul>
R5	Using ratios	<ul> <li>Dividing a quantity into a given ratio</li> <li>Make a division into two parts into a ratio</li> <li>Use ratio in problems, including mixing substances, conversions, scale problems, and best value for money, etc.</li> </ul>
R6	Writing as a ratio	Express two amounts as a ratio or fraction
R7	Proportion	Understand and use proportion
R8	Ratio and fractions	Understand the relationship between ratio and a fraction or a linear function

R9	Percentages	<ul> <li>Understand the meaning of percentage</li> <li>Change percentages to fractions or decimals and the other way round</li> <li>Use percentages, fractions and decimals to multiply</li> <li>Express one amount as a percentage of another</li> <li>Compare two quantities by using percentages</li> <li>Use percentages greater than 100%</li> <li>Solve problems using percentage change</li> <li>Work with percentage increase and decrease</li> <li>Calculate an original value (reverse percentages)</li> <li>Find simple interest</li> </ul>
R10	Proportion	<ul> <li>Solve problems involving direct proportion</li> <li>Solve problems involving inverse proportion</li> <li>Understand graphs of direct and inverse proportion</li> </ul>
R11	Compound units	Use units for compound measures of Speed Rates of pay Density Price per item/amount Pressure
R12	Comparisons	<ul> <li>Compare lengths, areas and volumes using ratio notation</li> <li>Apply ratio comparisons in similar shapes or in trigonometry ratios</li> </ul>
R13	Direct and inverse proportion	<ul> <li>Understand that x inversely proportional to y means x is proportional to <sup>1</sup>/<sub>y</sub></li> <li>Use equations for direct and inverse proportion</li> </ul>
R14	Graphs and proportion	<ul> <li>Understand and use the gradient of a straight line graph as a rate of change</li> <li>Recognise and use graphs that show direct or inverse proportion</li> </ul>
R16	Growth and decay	<ul> <li>Set up and solve problems of growth and decay</li> <li>Set up and solve problems of compound interest</li> </ul>

	GEOMETRY AND	MEASURE
G1	Understanding terms	Understand and use the terms points, lines, vertices and planes
		Understand and use the terms parallel, perpendicular and right angle
		Understand and use the terms polygon and regular polygon
		Understand symmetry and rotational symmetry of polygons
		Understand labelling of sides and angles on shapes
		Draw a diagram from a description
G2	Constructions	Use ruler and compasses to construct
		Perpendicular bisector of a line
		Perpendicular at a point on a line
		Perpendicular from a separate point to a line
		Angle bisector
		An angle of 60°
		Use constructions in loci problems
		Know that the perpendicular from a point to a line is the shortest distance from the point to the line
G3	Basic angle facts	Know and use
		☐ Angles at a point add up to 360⁰
		Angles at a point on a straight line add up to 180°
		Vertically opposite angles are equal
		In parallel lines, alternate angles are equal
		In parallel lines, corresponding angles are equal
		Angles in a triangle add up to 180°
		Be able to find the sum of angles in any polygon
		Be able to find exterior and interior angles of any regular polygon
		NB. In parallel lines, "Z angles" and "F angles" are not allowed as reasons

G4	Triangles, quadrilaterals and other polygons	Know and use the special properties of quadrilaterals: Square Rectangle Parallelogram Trapezium Kite Rhombus Know and use the special properties of triangles: Isosceles triangle Equilateral triangle Scalene triangle Acute angled triangle Obtuse angled triangle Hexagon Hexagon Decagon
G5	Congruent triangles	Know and use the criteria for congruent triangles: SSS, SAS, ASA and RHS
G6	Applying angle facts and other properties	<ul> <li>Apply angle facts and facts about congruence and similar shapes to find angles and sides</li> <li>Use Pythagoras' theorem</li> <li>Use base angles in an isosceles triangle are equal</li> <li>Use angle facts and other properties for simple proofs</li> </ul>
G7	Transformations	<ul> <li>Identify, describe or draw similar shapes</li> <li>Identify, describe or draw congruent shapes</li> <li>Describe and use transformations:         <ul> <li>Rotation</li> <li>Reflection</li> <li>Translation (including using vectors)</li> <li>Enlargement</li> </ul> </li> <li>Describe and use enlargements with fractional scale factors</li> </ul>

G9	The circle	Know and use definitions and properties of circle parts:
		Chord
		Diameter
		Circumference
		Tangent
		Arc
		Sector
		Segment
G11	Geometry on a grid	Solve geometrical problems on a coordinate grid
G12	Solid shapes	Know properties of the faces, surfaces, edges and vertices of
		Cylinders
		Pyramids
		Spheres
G13	Plans and elevations	Draw and interpret plans and elevations of 3D shapes
G14	Units of measure	Use standard units of measure for length, area, volume/capacity, mass, time, money, etc.
G15	Maps and scale	Measure and use lines and angles in diagrams
	drawings	Use maps and scale drawings
		Use bearings, including the 8 compass points and 3- figure angles for bearings
G16	Area and volume	Know and use formulas to calculate
		Area of a triangle
		Area of a parallelogram
		Area of a trapezium
		Volume of a cuboid
		Volume of a prism
		Volume of a cylinder

G17	Circles and other shapes	<ul> <li>Know and use the formula for circumference of a circle</li> <li>Know and use the formula for area of a circle</li> <li>Calculate perimeters of 2D shapes</li> <li>Calculate areas of compound shapes</li> <li>Find the surface area and volume of</li> <li>Sphere</li> </ul>
		Pyramid
		Frustum
		Composite solids
		NB. Answers may be asked for in terms of $\pi$
G18	Sectors and arcs	Calculate length of an arc
		Calculate area of a sector
		Calculate the angle of a sector
G19	Congruence and	Understand congruent shapes
similarity	Understand similar shapes	
		Calculate lengths in similar shapes
G20		Know and use the formula for Pythagoras' Theorem to find a length
		$\Box$ Know and use the sin, cos and tan ratios to find a length
		Know and use the sin, cos and tan ratios to find an angle
G21	Exact values of sin, cos and tan	Know the exact values of sin and cos for angles of 0°, 30°, 45°, 60° and 90°
		Know the exact values of tan for angles of 0°, 30°, 45°, and 60°
G24	Vectors for translations	Use a vector to describe a translation
G25	Using vectors	<ul> <li>Add and subtract vectors</li> <li>Multiply a vector by a number</li> </ul>
		Use column vectors and vectors on diagrams

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	PROBABILITY	
P1	Basic probability	Use tables and probability trees to show outcomes and probabilities
		NB. Probabilities should be shown as fractions, decimals or percentages
P2	Random, fair and equally likely events	Understand and use ideas of random events, fairness, and equally likely events
		Use these ideas to calculate expected outcomes
P3	Relative frequency	Understand the relationship between relative frequency and probability
P4	Exhaustive outcomes	Understand and use the fact that the probabilities of exhaustive outcomes (all possible outcomes) add up to 1
P5	Experimental probability	Understand that the greater the sample size or number of events in experimental probability, the closer the results will be to the theoretical probability
P6	Diagrams	Use diagrams for showing and calculating sets of data, including
		Tables and grids
		🗌 Venn diagrams
		Tree diagrams
P7	Sample spaces	Use sample spaces for single or combined events with equally likely outcomes
		Use sample spaces to calculate theoretical probabilities
P8	Probability trees	Use tree diagrams to represent independent events
		Use tree diagrams to represent dependent events
		Use adding and multiplying correctly for combined probabilities

	STATISTICS	
S1	Sample populations	Understand how a sample of a population can be used to represent the whole population
S2	Graphs and diagrams	Construct and use
		Frequency tables
		Bar charts
		Pie charts
		Pictograms
		Vertical line charts
		Tables and line graphs for time series data
S4	Measures of data	Be able to represent data in graphs or diagrams
		Understand and use
		Median
		🗌 Mean
		Mode and modal class
		Range
		Know and understand the terms
		Primary data
		Secondary data
		Discrete data
		Continuous data
S5	Describing a population	Describe a population, eg. using range, median, etc.
S6	Scatter graphs	Use and interpret scatter graphs
		Recognise correlation (positive or negative, and strong or weak, or no correlation)
		Understand that a correlation doesn't mean that one variable is a cause of the other
		Draw a line of best fit
		Use a line of best fit to predict results
		Extrapolate data, but understand why this is not always advisable