

## Mathematics overview: Stage 7 Star

Unit	Hrs	KNOWLEDGE
<a href="#">Numbers and the number system</a>	6	<ul style="list-style-type: none"> <li>use the concepts and vocabulary of prime numbers, factors (divisors), multiples, common factors, common multiples, highest common factor and lowest common multiple</li> <li>use positive integer powers and associated real roots (square, cube and higher), recognise powers of 2, 3, 4, 5 (ALSO 6*)</li> <li>recognise and use sequences of triangular, square and cube numbers, simple arithmetic progressions</li> <li>order positive and negative integers, decimals and fractions</li> <li>use the symbols =, ≠, &lt;, &gt;, ≤, ≥ (ALSO 6*)</li> </ul>
<a href="#">Counting and comparing</a>	3	<ul style="list-style-type: none"> <li>identify the value of each digit in numbers given to three decimal places (NEW, ALSO 6*)</li> <li>understand and use place value (e.g. when working with very large or very small numbers, and when calculating with decimals)</li> <li>solve problems involving addition, subtraction, multiplication and division (NEW, ALSO 6*)</li> <li>multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places (NEW, ALSO 6*)</li> </ul>
<a href="#">Calculating</a>	9	<ul style="list-style-type: none"> <li>multiply one-digit numbers with up to two decimal places by whole numbers (NEW, ALSO 6*)</li> <li>use written division methods in cases where the answer has up to two decimal places (NEW, ALSO 6*)</li> </ul>
<a href="#">Visualising and constructing</a>	6	<ul style="list-style-type: none"> <li>associate a fraction with division and calculate decimal fraction equivalents (for example 0.375) for a simple fraction (for example 3/8) (NEW, ALSO 6*)</li> <li>solve addition and subtraction multi-step problems in contexts, deciding which operation and methods to use and why (NEW, ALSO 6*)</li> <li>use conventional notation for priority of operations, including brackets and powers</li> <li>recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions)</li> </ul>
<a href="#">Investigating properties of shapes</a>	6	<ul style="list-style-type: none"> <li>use conventional terms and notations: points, lines, vertices, edges, planes, parallel lines, perpendicular lines, right angles, polygons, regular polygons and polygons with reflection and/or rotation symmetries (ALSO 6*)</li> <li>use the standard conventions for labelling and referring to the sides and angles of triangles (ALSO 6*)</li> <li>draw diagrams from written description (ALSO 6*)</li> <li>interpret plans and elevations of 3D shapes (ALSO 8*)</li> <li>identify properties of the faces, surfaces, edges and vertices of: cubes, cuboids, prisms, cylinders, pyramids, cones and spheres</li> </ul>
<a href="#">Algebraic proficiency: tinkering</a>	9	<ul style="list-style-type: none"> <li>derive and apply the properties and definitions of: special types of quadrilaterals, including square, rectangle, parallelogram, trapezium, kite and rhombus; and triangles and other plane figures using appropriate language</li> <li>find unknown angles in any triangles, quadrilaterals and regular polygons (NEW)</li> <li>identify and apply circle definitions and properties, including: centre, radius, chord, diameter, circumference</li> <li>understand and use the concepts and vocabulary of expressions, equations, formulae, terms, identities and factors (ALSO 6*)</li> <li>use and interpret algebraic notation, including: <math>ab</math> in place of <math>a \times b</math>, <math>3y</math> in place of <math>y + y + y</math> and <math>3 \times y</math>, <math>a^2</math> in place of <math>a \times a</math>, <math>a^3</math> in place of <math>a \times a \times a</math>, <math>a/b</math> in place of <math>a \div b</math>, brackets (ALSO 6*)</li> </ul>
<a href="#">Exploring fractions, decimals and percentages</a>	6	<ul style="list-style-type: none"> <li>simplify and manipulate algebraic expressions by collecting like terms and multiplying a single term over a bracket (ALSO 6*)</li> <li>simplify and manipulate algebraic expressions by taking out common factors and simplifying expressions involving sums, products and powers, including the laws of indices (NEW)</li> <li>substitute numerical values into formulae and expressions</li> <li>where appropriate, interpret simple expressions as functions with inputs and outputs</li> <li>express one quantity as a fraction of another, where the fraction is less than 1 or greater than 1</li> <li>recall and use equivalencies between simple fractions, decimals and percentages, including in different contexts (NEW, ALSO 6*)</li> <li>define percentage as 'number of parts per hundred'</li> </ul>
<a href="#">Proportional reasoning</a>	3	<ul style="list-style-type: none"> <li>work interchangeably between terminating decimals and their corresponding fractions such as 3.5 and 7/2 or 0.375 and 3/8 (ALSO, 8*)</li> <li>use ratio notation, including reduction to simplest form (ALSO 6*)</li> <li>divide a given quantity into two parts in a given part: part or part: whole ratio (ALSO 6*)</li> </ul>
<a href="#">Pattern sniffing</a>	3	<ul style="list-style-type: none"> <li>identify and work with fractions in ratio problems (ALSO 8*)</li> <li>generate terms of a sequence from a term-to-term rule or a position-to-term rule</li> </ul>

<a href="#">Measuring space</a>	3	<ul style="list-style-type: none"> <li>deduce expressions to calculate the nth term of a linear sequence (ALSO 8*)</li> <li>use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimals places. (NEW, ALSO 6*)</li> <li>use standard units of mass, length, time, money and other measures (including standard compound measures) using decimal quantities where appropriate (ALSO 6*)</li> </ul>
<a href="#">Investigating angles</a>	3	<ul style="list-style-type: none"> <li>change freely between related standard units (e.g. time, length, area, volume/capacity, mass) in numerical contexts</li> <li>measure line segments and angles in geometric figures</li> <li>convert between miles and kilometres (ALSO 6*)</li> <li>apply the properties of angles at a point, angles at a point on a straight line, vertically opposite angles (ALSO 6*)</li> </ul>
<a href="#">Calculating fractions, decimals and percentages</a>	9	<ul style="list-style-type: none"> <li>apply the four operations, including formal written methods, to simple fractions (proper and improper), and mixed numbers</li> <li>add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions (NEW, ALSO 6*)</li> <li>multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, <math>1/4 \times 1/2 = 1/8</math>] (NEW, ALSO 6*)</li> <li>divide proper fractions by whole numbers (for example, <math>1/3</math> divided by <math>2 = 1/6</math>)</li> <li>interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively</li> <li>compare two quantities using percentages</li> <li>solve problems involving percentage change, including percentage increase/decrease</li> <li>solve problems involving percentage change, including original value problems, and simple interest including in financial mathematics (NEW, ALSO 8*)</li> </ul>
<a href="#">Solving equations and inequalities</a>	6	<ul style="list-style-type: none"> <li>solve linear equations in one unknown algebraically (ALSO 6*)</li> <li>solve linear equations with the unknown on both sides of the equation (ALSO 8*)</li> <li>solve linear inequalities in one variable</li> <li>represent the solution of an inequality on a number line</li> <li>use standard units of measure and related concepts (length, area, volume/capacity)</li> </ul>
<a href="#">Calculating space</a>	9	<ul style="list-style-type: none"> <li>calculate perimeters of 2D shapes (ALSO 6*)</li> <li>know and apply formulae to calculate area of triangles, parallelograms, trapezia</li> <li>calculate surface area of cubes and cuboids</li> <li>calculate the surface area of a triangular prism when lengths are known</li> <li>know and apply formulae to calculate volume of cuboids</li> </ul>
<a href="#">Checking, approximating and estimating</a>	3	<ul style="list-style-type: none"> <li>understand and use standard mathematical formulae</li> <li>round numbers and measures to an appropriate degree of accuracy (e.g. to a specified number of decimal places or significant figures)</li> <li>estimate answers; check calculations using approximation and estimation, including answers obtained using technology</li> <li>solve problems which require answers to be rounded to specified degrees of accuracy (NEW, ALSO 6*)</li> <li>recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions)</li> <li>work with coordinates in all four quadrants</li> </ul>
<a href="#">Mathematical movement</a>	6	<ul style="list-style-type: none"> <li>understand and use lines parallel to the axes, <math>y = x</math> and <math>y = -x</math></li> <li>plot graphs of equations that correspond to straight-line graphs in the coordinate plane (NEW)</li> <li>solve geometrical problems on coordinate axes</li> <li>identify, describe and construct congruent shapes including on coordinate axes, by considering rotation, reflection and translation</li> </ul>
<a href="#">Understanding Risk 1</a>	3	<ul style="list-style-type: none"> <li>describe translations as 2D vectors (ALSO 6*)</li> <li>relate relative expected frequencies to theoretical probability, using appropriate language and the 0 – 1 probability scale (ALSO 6*)</li> <li>record describe and analyse the frequency of outcomes of probability experiments using tables and frequency trees (ALSO 8*)</li> <li>construct theoretical possibility spaces for single and combined experiments with equally likely outcomes and use these to calculate theoretical probabilities</li> </ul>
<a href="#">Presentation of data</a>	6	<ul style="list-style-type: none"> <li>apply the property that the probabilities of an exhaustive set of outcomes sum to one (ALSO 6*)</li> <li>apply ideas of randomness, fairness and equally likely events to calculate expected outcomes of multiple future experiments (NEW)</li> <li>interpret and construct tables, charts and diagrams, including frequency tables, bar charts, frequency diagrams, pie charts and pictograms for categorical data, vertical line charts for ungrouped discrete numerical data and know their appropriate use</li> </ul>
<a href="#">Measuring data</a>	3	<ul style="list-style-type: none"> <li>Interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate measures of central tendency (median, mean and mode) and spread (range) (ALSO 6*)</li> </ul>

<b>KNOWLEDGE</b>	<b>The Big Picture:</b> <a href="#">Number and Place Value progression map</a>
<ul style="list-style-type: none"> <li>• use the concepts and vocabulary of prime numbers, factors (divisors), multiples, common factors, common multiples, highest common factor and lowest common multiple</li> <li>• use positive integer powers and associated real roots (square, cube and higher), recognise powers of 2, 3, 4, 5 (ALSO 6*)</li> <li>• recognise and use sequences of triangular, square and cube numbers, simple arithmetic progressions</li> </ul>	

SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>• Recall prime numbers up to 50</li> <li>• Know how to test if a number up to 150 is prime</li> <li>• Know the meaning of and find the ‘highest common factor’ and ‘lowest common multiple’</li> <li>• Recognise when a problem involves using the highest common factor or lowest common multiple of two numbers</li> <li>• Be able to break a number into product of its prime factors</li> <li>• Be able to use a venn diagram to find the HCF/LCM</li> <li>• Understand and use the notation and rules of powers (laws of indices)</li> <li>• Know the meaning of the square root symbol (<math>\sqrt{\quad}</math>)</li> <li>• Use a scientific calculator to calculate powers and roots</li> <li>• Make the connection between squares and square roots (and cubes and cube roots)</li> <li>• Recall the first 15 square numbers</li> <li>• Recall the first 5 cube numbers</li> </ul>	<p>KM: <a href="#">Exploring primes activities</a>: Factors of square numbers; Mersenne primes; LCM sequence; <math>n^2</math> and <math>(n + 1)^2</math>; <math>n^2</math> and <math>n^2 + n</math>; <math>n^2 + 1</math>; <math>n! + 1</math>; <math>n! - 1</math>; <math>x^2 + x + 41</math></p> <p>KM: Use the method of <a href="#">Eratosthenes' sieve</a> to identify prime numbers, but on a grid 6 across by 17 down instead. What do you notice?</p> <p>KM: <a href="#">Square number puzzle</a></p> <p>KM: <a href="#">History and Culture: Goldbach's Conjectures</a></p> <p>NRICH: <a href="#">Factors and multiples</a></p> <p>NRICH: <a href="#">Powers and roots</a></p> <p><b>Learning review</b>  <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></p>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Know how to find common multiples of two given numbers</li> <li>• Know how to find common factors of two given numbers</li> <li>• Recall multiplication facts to <math>12 \times 12</math> and associated division facts</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>                  Number and Place Value: <math>\sqrt{6}</math></p>	<p>((Lowest) common) multiple and LCM                  ((Highest) common) factor and HCF                  Power                  (Square and cube) root                  Triangular number, Square number, Cube number, Prime number                  Linear sequence</p> <p><b>Notation</b>                  Index notation: e.g. <math>5^3</math> is read as ‘5 to the power of 3’ and means ‘3 lots of 5 multiplied together’                  Radical notation: e.g. <math>\sqrt{49}</math> is generally read as ‘the square root of 49’ and means ‘the positive square root of 49’; <math>\sqrt[3]{8}</math> means ‘the cube root of 8’</p>	<p>Pupils need to know how to use a scientific calculator to work out powers and roots.                  Note that while the square root symbol (<math>\sqrt{\quad}</math>) refers to the positive square root of a number, every positive number has a negative square root too.                  NCETM: <a href="#">Departmental workshop: Index Numbers</a>                  NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b>  <i>The following definition of a prime number should be used in order to minimise confusion about 1: A prime number is a number with exactly two factors.</i>  <i>Every classroom has a set of <a href="#">number classification posters</a> on the wall</i></p>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• When using Eratosthenes sieve to identify prime numbers, why is there no need to go further than the multiples of 7? If this method was extended to test prime numbers up to 200, how far would you need to go? Convince me.</li> <li>• Kenny says ‘20 is a square number because <math>10^2 = 20</math>’. Explain why Kenny is wrong. Kenny is partially correct. How could he change his statement so that it is fully correct?</li> <li>• Always / Sometimes / Never: the lowest common multiple of two numbers is found by multiplying the two numbers together</li> </ul>		<ul style="list-style-type: none"> <li>• Many pupils believe that 1 is a prime number – a misconception which can arise if the definition is taken as ‘a number which is divisible by itself and 1’</li> <li>• A common misconception is to believe that <math>5^3 = 5 \times 3 = 15</math></li> <li>• See pedagogical note about the square root symbol too</li> </ul>

<b>KNOWLEDGE</b> <ul style="list-style-type: none"> <li>order positive and negative integers, decimals and fractions</li> <li>use the symbols =, ≠, &lt;, &gt;, ≤, ≥ (ALSO 6*)</li> <li>identify the value of each digit in numbers given to three decimal places (NEW, ALSO 6*)</li> </ul>	<b>The Big Picture:</b> <a href="#">Number and Place Value progression map</a>
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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>Place a set of mixed positive and negative numbers in order</li> <li>Place a set of decimals in order</li> <li>Identify a common denominator that can be used to order a set of fractions</li> <li>Order fractions where the denominators are not multiples of each other</li> <li>Convert between fractions, decimals and percentages</li> <li>Order a set of numbers including a mixture of fractions, decimals and negative numbers</li> <li>Use inequality symbols to compare numbers</li> <li>Make correct use of the symbols = and ≠</li> </ul>	KM: <a href="#">Farey Sequences</a> KM: <a href="#">Decimal ordering cards 2</a> KM: <a href="#">Maths to Infinity: Fractions, decimals and percentages</a> KM: <a href="#">Maths to Infinity: Directed numbers</a> NRICH: <a href="#">Greater than or less than?</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li><a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Understand that negative numbers are numbers less than zero</li> <li>Order a set of decimals with a mixed number of decimal places (up to a maximum of three)</li> <li>Order fractions where the denominators are multiples of each other</li> <li>Order fractions where the numerator is greater than 1</li> <li>Know how to simplify a fraction by cancelling common factors</li> </ul>	Positive number Negative number Integer Numerator Denominator  <b>Notation</b> The 'equals' sign: = The 'not equal' sign: ≠ The inequality symbols: < (less than), > (greater than), ≤ (less than or equal to), ≥ (more than or equal to)	Zero is neither positive nor negative. The set of integers includes the natural numbers {1, 2, 3, ...}, zero (0) and the 'opposite' of the natural numbers {-1, -2, -3, ...}. Pupil must use language correctly to avoid reinforcing misconceptions: for example, 0.45 should never be read as 'zero point forty-five'; $5 > 3$ should be read as 'five is greater than 3', not '5 is bigger than 3'. Ensure that pupils read information carefully and check whether the required order is smallest first or greatest first. The equals sign was designed by Robert Recorde in 1557 who also introduced the plus (+) and minus (-) symbols. NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Teachers use the language 'negative number' to avoid future confusion with calculation that can result by using 'minus number'</i> <i>Every classroom has a <a href="#">negative number washing line</a> on the wall</i>

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Jenny writes down <math>0.400 &gt; 0.58</math>. Kenny writes down <math>0.400 &lt; 0.58</math>. Who do you agree with? Why?</li> <li>Find a fraction which is greater than <math>3/5</math> and less than <math>7/8</math>. And another. And another ...</li> <li>Convince me that <math>-15 &lt; -3</math></li> </ul>		<ul style="list-style-type: none"> <li>Some pupils may believe that 0.400 is greater than 0.58</li> <li>Pupils may believe, incorrectly, that:               <ul style="list-style-type: none"> <li>- A fraction with a larger denominator is a larger fraction</li> <li>- A fraction with a larger numerator is a larger fraction</li> <li>- A fraction involving larger numbers is a larger fraction</li> </ul> </li> <li>Some pupils may believe that -6 is greater than -3. For this reason ensure pupils avoid saying 'bigger than'</li> </ul>

<p><b>KNOWLEDGE</b></p> <ul style="list-style-type: none"> <li>understand and use place value (e.g. when working with very large or very small numbers, and when calculating with decimals)</li> <li>solve problems involving addition, subtraction, multiplication and division (NEW, ALSO 6*)</li> <li>multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places (NEW, ALSO 6*)</li> <li>multiply one-digit numbers with up to two decimal places by whole numbers (NEW, ALSO 6*)</li> <li>use written division methods in cases where the answer has up to two decimal places (NEW, ALSO 6*)</li> <li>associate a fraction with division and calculate decimal fraction equivalents (for example 0.375) for a simple fraction (for example 3/8) (NEW, ALSO 6*)</li> <li>solve addition and subtraction multi-step problems in contexts, deciding which operation and methods to use and why (NEW, ALSO 6*)</li> <li>use conventional notation for priority of operations, including brackets and powers</li> <li>recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions)</li> </ul>	<p>The Big Picture: <a href="#">Calculation progression map</a></p>
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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>Be fluent at multiplying a three-digit or a two-digit number by a two-digit number</li> <li>Be fluent when using the method of short division, including decimal answers</li> <li>Be able to multiply and divide by powers of 10</li> <li>Use knowledge of place value to multiply with decimals</li> <li>Use knowledge of place value to divide a decimal</li> <li>Use knowledge of place value to divide by a decimal</li> <li>Use knowledge of inverse operations when dividing with decimals</li> <li>Be able to convert fractions to decimals by division</li> <li>Know the order of operations for the four operations</li> <li>Use brackets and powers in problems involving the order of operations</li> <li>Understand and apply the fact that addition and subtraction have equal priority</li> <li>Understand and apply the fact that multiplication and division have equal priority</li> </ul>	<p>KM: <a href="#">Long multiplication template</a></p> <p>KM: <a href="#">Dividing (lots)</a></p> <p>KM: <a href="#">Misplaced points</a></p> <p>KM: <a href="#">Maths to Infinity: Multiplying and dividing</a></p> <p>NRICH: <a href="#">Cinema Problem</a></p> <p>NRICH: <a href="#">Funny factorisation</a></p> <p>NRICH: <a href="#">Skeleton</a></p> <p>NRICH: <a href="#">Long multiplication</a></p> <p><b>Learning review</b></p> <ul style="list-style-type: none"> <li><a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Fluently recall multiplication facts up to <math>12 \times 12</math></li> <li>Fluently apply multiplication facts when carrying out division</li> <li>Know the formal written method of long multiplication</li> <li>Know the formal written method of short division</li> <li>Know the formal written method of long division</li> <li>Convert between an improper fraction and a mixed number</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b></p> <p>Calculating: v2, v3, v4, v5</p> <p>Fractions, decimals &amp; percentages: v6, v7</p> <p>Solving problems: v2</p>	<p>Improper fraction</p> <p>Top-heavy fraction</p> <p>Mixed number</p> <p>Operation</p> <p>Inverse</p> <p>Long multiplication</p> <p>Short division</p> <p>Long division</p> <p>Remainder</p>	<p>Establish level of understanding and ability based on expectations of pupils at primary school</p> <p>The grid method is promoted as a method that aids numerical understanding and later progresses to multiplying algebraic statements.</p> <p>NCETM: <a href="#">Departmental workshop: Place Value</a></p> <p>NCETM: <a href="#">Subtraction</a></p> <p>NCETM: <a href="#">Multiplication</a> and <a href="#">division</a></p> <p>NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b></p> <p><i>The use of long multiplication is to be promoted as the 'most efficient method'.</i></p> <p><i>Short division is promoted as the 'most efficient method'.</i></p> <p><i>If any acronym is promoted to help remember the order of operations, then BIDMAS is used as the I stands for indices.</i></p>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Jenny says that <math>2 + 3 \times 5 = 25</math>. Kenny says that <math>2 + 3 \times 5 = 17</math>. Who is correct? How do you know?</li> <li>Find missing digits in otherwise completed long multiplication / short division calculations</li> <li>Show me a calculation that is connected to <math>14 \times 26 = 364</math>. And another, and another ...</li> </ul>		<ul style="list-style-type: none"> <li>The use of BIDMAS (or BODMAS) can imply that division takes priority over multiplication, and that addition takes priority over subtraction. This can result in incorrect calculations.</li> <li>Pupils may incorrectly apply place value when dividing by a decimal for example by making the answer 10 times bigger when it should be 10 times smaller.</li> </ul>

<b>KNOWLEDGE</b>	The Big Picture: <a href="#">Properties of Shape progression map</a>
<ul style="list-style-type: none"> <li>use conventional terms and notations: points, lines, vertices, edges, planes, parallel lines, perpendicular lines, right angles, polygons, regular polygons and polygons with reflection and/or rotation symmetries (ALSO 6*)</li> <li>use the standard conventions for labelling and referring to the sides and angles of triangles (ALSO 6*)</li> <li>draw diagrams from written description (ALSO 6*)</li> <li>interpret plans and elevations of 3D shapes (ALSO 8*)</li> </ul>	

SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>Know the meaning of faces, edges and vertices</li> <li>Use notation for parallel lines</li> <li>Know the meaning of 'perpendicular' and identify perpendicular lines</li> <li>Know the meaning of 'regular' polygons</li> <li>Identify line and rotational symmetry in polygons</li> <li>Use AB notation for describing lengths</li> <li>Use <math>\angle ABC</math> notation for describing angles</li> <li>Use a ruler to accurately measure line segments to the nearest millimetre</li> <li>Use a protractor to accurately measure angles to the nearest degree</li> <li>Use ruler and protractor to construct triangles from written descriptions</li> <li>To be able to use a compass</li> <li>Use ruler and compasses to construct triangles when all three sides known</li> <li>Know and understand the vocabulary of plans and elevations</li> <li>Interpret plans and elevations and planes of symmetry in 3D shapes</li> </ul>	KM: <a href="#">Shape work</a> (selected activities) NRICH: <a href="#">Notes on a triangle</a>  <b>Learning review</b> <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Use a ruler to measure and draw lengths to the nearest millimetre</li> <li>Use a protractor to measure and draw angles to the nearest degree</li> </ul>	Edge, Face, Vertex (Vertices) Plane Parallel Perpendicular Regular polygon Rotational symmetry Plan, Elevation  <b>Notation</b> The line between two points A and B is AB The angle made by points A, B and C is $\angle ABC$ The angle at the point A is $\hat{A}$ Arrow notation for sets of parallel lines Dash notation for sides of equal length	NCETM: <a href="#">Departmental workshop: Constructions</a> The equals sign was designed (by Robert Recorde in 1557) based on two equal length lines that are equidistant NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Dynamic geometry software to be used by all students to construct and explore dynamic diagrams of perpendicular and parallel lines.</i>

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Given SSS, how many different triangles can be constructed? Why? Repeat for ASA, SAS, SSA, AAS, AAA.</li> <li>Always / Sometimes / Never: to draw a triangle you need to know the size of three angles; to draw a triangle you need to know the size of three sides.</li> <li>Convince me that a hexagon can have rotational symmetry with order 2.</li> </ul>		<ul style="list-style-type: none"> <li>Two line segments that do not touch are perpendicular if they would meet at right angles when extended</li> <li>Pupils may believe, incorrectly, that:               <ul style="list-style-type: none"> <li>- perpendicular lines have to be horizontal / vertical</li> <li>- only straight lines can be parallel</li> <li>- all triangles have rotational symmetry of order 3</li> <li>- all polygons are regular</li> </ul> </li> </ul>

## KNOWLEDGE

The Big Picture: [Properties of Shape progression map](#)

- identify properties of the faces, surfaces, edges and vertices of: cubes, cuboids, prisms, cylinders, pyramids, cones and spheres
- derive and apply the properties and definitions of: special types of quadrilaterals, including square, rectangle, parallelogram, trapezium, kite and rhombus; and triangles and other plane figures using appropriate language
- find unknown angles in any triangles, quadrilaterals and regular polygons (NEW)
- identify and apply circle definitions and properties, including: centre, radius, chord, diameter, circumference

SKILLS		Suggested resources
<ul style="list-style-type: none"> <li>• Know the vocabulary of 3D shapes</li> <li>• Know the connection between faces, edges and vertices in 3D shapes</li> <li>• Recall the names and shapes of special triangles and quadrilaterals</li> <li>• Know the properties of the special quadrilaterals (including diagonals)</li> <li>• Apply the properties of triangles to solve problems and calculate unknown angles</li> <li>• Apply the properties of quadrilaterals to solve problems and calculate unknown angles</li> <li>• Be able to find the interior angle sum and angle of a regular polygon</li> <li>• Know the total of the exterior angles in any polygon</li> <li>• Establish the size of an exterior angle in a regular polygon</li> <li>• Be able to label parts of a circle</li> </ul>		KM: <a href="#">Euler's formula</a> KM: <a href="#">Visualising 3D shapes</a> KM: <a href="#">Dotty activities</a> : Shapes on dotted paper KM: <a href="#">What's special about quadrilaterals?</a> Constructing quadrilaterals from diagonals and summarising results. KM: <a href="#">Investigating polygons</a> . Tasks one and two should be carried out with irregular polygons. NRICH: <a href="#">Property chart</a> NRICH: <a href="#">Quadrilaterals game</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>
Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Know the names of common 3D shapes</li> <li>• Know the meaning of face, edge, vertex</li> <li>• Understand the principle of a net</li> <li>• Know the names of special triangles</li> <li>• Know the names of special quadrilaterals</li> <li>• Know the meaning of parallel, perpendicular</li> <li>• Know the notation for equal sides, parallel sides, right angles</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b> Properties of shapes: v1, v2</p>	Face, Edge, Vertex (Vertices) Cube, Cuboid, Prism, Cylinder, Pyramid, Cone, Sphere Quadrilateral Square, Rectangle, Parallelogram, (Isosceles) Trapezium, Kite, Rhombus Delta, Arrowhead Diagonal Perpendicular Parallel Triangle Scalene, Right-angled, Isosceles, Equilateral  <b>Notation</b> Dash notation to represent equal lengths in shapes and geometric diagrams Right angle notation	Ensure that pupils do not use the word 'diamond' to describe a kite, or a square that is 45° to the horizontal. 'Diamond' is not the mathematical name of any shape. A cube is a special case of a cuboid and a rhombus is a special case of a parallelogram A prism must have a polygonal cross-section, and therefore a cylinder is not a prism. Similarly, a cone is not a pyramid. NCETM: <a href="#">Departmental workshop: 2D shapes</a> NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Every classroom has a set of <a href="#">triangle posters</a> and <a href="#">quadrilateral posters</a> on the wall</i> <i>Models of 3D shapes to be used by all students during this unit of work</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Show me an example of a trapezium. And another. And another ...</li> <li>• Always / Sometimes / Never: The number of vertices in a 3D shape is greater than the number of edges</li> <li>• Which quadrilaterals are special examples of other quadrilaterals? Why? Can you create a 'quadrilateral family tree'?</li> <li>• What is the same and what is different: Rhombus / Parallelogram?</li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils may think that all trapezia are isosceles</li> <li>• Some pupils may think that a diagonal cannot be horizontal or vertical</li> <li>• Two line segments that do not touch are perpendicular if they would meet at right angles when extended. Therefore the diagonals of an arrowhead (delta) are perpendicular despite what some pupils may think</li> <li>• Some pupils may think that a square is only square if 'horizontal', and even that a 'non-horizontal' square is called a diamond</li> <li>• The equal angles of an isosceles triangle are not always the 'base angles' as some pupils may think</li> </ul>



## KNOWLEDGE

The Big Picture: [Algebra progression map](#)

- understand and use the concepts and vocabulary of expressions, equations, formulae, terms, identities and factors (ALSO 6\*)
- use and interpret algebraic notation, including:  $ab$  in place of  $a \times b$ ,  $3y$  in place of  $y + y + y$  and  $3 \times y$ ,  $a^2$  in place of  $a \times a$ ,  $a^3$  in place of  $a \times a \times a$ ,  $a/b$  in place of  $a \div b$ , brackets (ALSO 6\*)
- simplify and manipulate algebraic expressions by collecting like terms and multiplying a single term over a bracket (ALSO 6\*)
- simplify and manipulate algebraic expressions by taking out common factors and simplifying expressions involving sums, products and powers, including the laws of indices (NEW)
- substitute numerical values into formulae and expressions
- where appropriate, interpret simple expressions as functions with inputs and outputs

## SKILLS

## Suggested resources

- Know the meaning of expression, term, formula, equation, identity, inequality and factor
- Know basic algebraic notation (the rules of algebra)
- Use letters to represent variables
- Identify like terms in an expression
- Simplify an expression by collecting like terms (including powers)
- Know how to multiply a (positive) single term over a bracket (including powers)
- Know how to factorise a linear expression by identifying a common factor (including powers)
- Substitute positive and negative numbers into expressions and formulae
- Be able to write an expression

KM: [Pairs in squares](#). Prove the results algebraically.  
 KM: [Algebra ordering cards](#)  
 KM: [Spiders and snakes](#). See the 'clouding the picture' approach  
 KM: Use [number patterns](#) to develop the multiplying out of brackets  
 KM: [Maths to Infinity: Brackets](#)  
 NRICH: [Your number is ...](#)  
 NRICH: [Crossed ends](#)  
 NRICH: [Number pyramids](#) and [More number pyramids](#)

## Learning review

- [www.diagnosticquestions.com](http://www.diagnosticquestions.com)

## Prerequisites

- Use symbols (including letters) to represent missing numbers
- Substitute numbers into worded formulae
- Substitute numbers into simple algebraic formulae
- Know the order of operations

## Bring on the Maths\*: Moving on up!

Algebra: v1

## Mathematical language

Algebra  
 Expression, Term, Formula (formulae), Equation, Function, Variable  
 Mapping diagram, Input, Output  
 Represent  
 Substitute  
 Evaluate  
 Like terms  
 Simplify / Collect  
 Identity  
 Factor  
 Notation  
 See key concepts above

## Agreed Common Teaching Approaches

Pupils will have experienced some algebraic ideas previously. Ensure that there is clarity about the distinction between representing a variable and representing an unknown.

Note that each of the statements  $4x$ ,  $42$  and  $4\frac{1}{2}$  involves a different operation after the 4, and this can cause problems for some pupils when working with algebra.

NCETM: [Algebra](#)  
 NCETM: [Glossary](#)

## Common approaches

*All pupils are expected to learn about the connection between mapping diagrams and formulae (to represent functions) in preparation for future representations of functions graphically.*

## Reasoning opportunities and probing questions

- Show me an example of an expression / formula / equation
- Always / Sometimes / Never:  $4(g+2) = 4g+8$ ,  $3(d+1) = 3d+1$ ,  $a^2 = 2a$ ,  $ab = ba$
- [What is wrong?](#)
- Jenny writes  $2a + 3b + 5a - b = 7a + 3$ . Kenny writes  $2a + 3b + 5a - b = 9ab$ . What would you write? Why?

## Cross Curricular Links

## Possible misconceptions

- Some pupils may think that it is always true that  $a=1$ ,  $b=2$ ,  $c=3$ , etc.
- A common misconception is to believe that  $a^2 = a \times 2 = a2$  or  $2a$  (which it can do on rare occasions but is not the case in general)
- When working with an expression such as  $5a$ , some pupils may think that if  $a=2$ , then  $5a = 52$ .
- Some pupils may think that  $3(g+4) = 3g+4$
- The convention of not writing a coefficient of 1 (i.e. '1x' is written as 'x' may cause some confusion. In particular some pupils may think that  $5h - h = 5$



## KNOWLEDGE

The Big Picture: [Fractions, decimals and percentages progression map](#)

- express one quantity as a fraction of another, where the fraction is less than 1 or greater than 1
- recall and use equivalencies between simple fractions, decimals and percentages, including in different contexts (NEW, ALSO 6\*)
- define percentage as 'number of parts per hundred'
- work interchangeably between terminating decimals and their corresponding fractions such as 3.5 and  $7/2$  or 0.375 and  $3/8$  (ALSO, 8\*)

SKILLS		Suggested resources
<ul style="list-style-type: none"> <li>• Write one quantity as a fraction of another where the fraction is less than 1</li> <li>• Write one quantity as a fraction of another where the fraction is greater than 1</li> <li>• Write a fraction in its lowest terms by cancelling common factors</li> <li>• Convert between mixed numbers and improper fractions</li> <li>• Find a fraction of an amount</li> <li>• Be able to convert between fractions, decimals and percentages</li> <li>• Understand that a percentage means 'number of parts per hundred'</li> <li>• Write a quantity as a percentage of another</li> <li>• Find a percentage of an amount</li> <li>• Be able to identify whether a decimal is terminating or recurring</li> </ul>	KM: <a href="#">Crazy cancelling, silly simplifying</a> NRICH: <a href="#">Rod fractions</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>	
Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Understand the concept of a fraction as a proportion</li> <li>• Understand the concept of equivalent fractions</li> <li>• Understand the concept of equivalence between fractions and percentages</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>            Fractions, decimals &amp; percentages: v1, v2</p>	Fraction Improper fraction Proper fraction Vulgar fraction Percentage Proportion Terminating Recurring  <b>Notation</b> Diagonal fraction bar / horizontal fraction bar	NRICH: <a href="#">Teaching fractions with understanding</a> NCETM: <a href="#">Teaching fractions</a> NCETM: <a href="#">Departmental workshop: Fractions</a> NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>All pupils are made aware that 'per cent' is derived from Latin and means 'out of one hundred'</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Jenny says '1/10 is the same as proportion as 10% so 1/5 is the same proportion as 5%.' What do you think? Why?</li> <li>• What is the same and what is different: 1/10 and 10% ... 1/5 and 20%?</li> <li>• Show this fraction as part of a square / rectangle / number line / ...</li> </ul>		<ul style="list-style-type: none"> <li>• A fraction can be visualised as divisions of a shape (especially a circle) but some pupils may not recognise that these divisions must be equal in size, or that they can be divisions of any shape.</li> <li>• Pupils may not make the connection that a percentage is a different way of describing a proportion</li> <li>• Pupils may think that it is not possible to have a percentage greater than 100%</li> </ul>

<b>KNOWLEDGE</b>	<b>The Big Picture:</b> <a href="#">Ratio and Proportion progression map</a>
<ul style="list-style-type: none"> <li>• use ratio notation, including reduction to simplest form (ALSO 6*)</li> <li>• divide a given quantity into two parts in a given part: part or part: whole ratio (ALSO 6*)</li> <li>• identify and work with fractions in ratio problems (ALSO 8*)</li> </ul>	

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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>• Describe a comparison of measurements or objects using the language ‘a to b’</li> <li>• Describe a comparison of measurements or objects using ratio notation a:b</li> <li>• Use ratio notation to describe a comparison of more than two measurements or objects</li> <li>• Use fractions fluently in situations involving ratio and proportion</li> <li>• Convert between different units of measurement</li> <li>• State a ratio of measurements in the same units and different units</li> <li>• Simplify a ratio by cancelling common factors</li> <li>• Identify when a ratio is written in its lowest terms</li> <li>• Find the value of a ‘unit’ in a division in a ratio problem</li> <li>• Divide a quantity in two parts in a given part:part ratio</li> <li>• Divide a quantity in two parts in a given part:whole ratio</li> </ul>	<p>KM: <a href="#">Maths to Infinity: FDP RP</a></p> <p>KM: <a href="#">Stick on the Maths: Ratio and proportion</a></p> <p>NRICH: <a href="#">Toad in the hole</a></p> <p>NRICH: <a href="#">Mixing lemonade</a></p> <p>NRICH: <a href="#">Food chains</a></p> <p>NRICH: <a href="#">Tray bake</a></p> <p><b>Learning review</b></p> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Find common factors of pairs of numbers</li> <li>• Convert between standard metric units of measurement</li> <li>• Convert between units of time</li> <li>• Recall multiplication facts for multiplication tables up to <math>12 \times 12</math></li> <li>• Recall division facts for multiplication tables up to <math>12 \times 12</math></li> <li>• Solve comparison problems</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b> Ratio and proportion: #1</p>	<p>Ratio</p> <p>Proportion</p> <p>Compare, comparison</p> <p>Part</p> <p>Simplify</p> <p>Common factor</p> <p>Cancel</p> <p>Lowest terms</p> <p>Unit</p> <p><b>Notation</b></p> <p>Ratio notation a:b for part:part or part:whole</p>	<p>Note that ratio notation is first introduced in this stage. When solving division in a ratio problems, ensure that pupils express their solution as two quantities rather than as a ratio.</p> <p>NCETM: <a href="#">The Bar Model</a></p> <p>NCETM: <a href="#">Multiplicative reasoning</a></p> <p>NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b></p> <p><i>All pupils are explicitly taught to use the bar model as a way to represent a division in a ratio problem</i></p>

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Show me a set of objects that demonstrates the ratio 3:2. And another, and another ...</li> <li>• Convince me that the ratio 120mm:0.3m is equivalent to 2:5</li> <li>• Always / Sometimes / Never: the smaller number comes first when writing a ratio</li> <li>• Using Cuisenaire rods: If the red rod is 1, explain why d (dark green) is 3. Can you say the value for all the rods? (w, r, g, p, y, d, b, t, B, o). Extend this understanding of proportion by changing the unit rod e.g. if <math>r = 1</math>, <math>p = ?</math>; <math>b = ?</math>; <math>o + 2B = ?</math> If <math>B = 1</math>; <math>y = ?</math> <math>3y = ?</math>; <math>o = ?</math> <math>o + p = ?</math> If <math>o + r = 6/7</math>; <math>t = ?</math></li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils may think that a:b always means part:part</li> <li>• Some pupils may try to simplify a ratio without first ensuring that the units of each part are the same</li> <li>• Many pupils will want to identify an additive relationship between two quantities that are in proportion and apply this to other quantities in order to find missing amounts</li> </ul>

<a href="#">Pattern sniffing</a>	<a href="#">Stage 8*</a>	3 hours
<b>KNOWLEDGE</b> <ul style="list-style-type: none"> <li>generate terms of a sequence from a term-to-term rule or a position-to-term rule</li> <li>deduce expressions to calculate the nth term of a linear sequence (ALSO 8*)</li> </ul>		The Big Picture: <a href="#">Algebra progression map</a>

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SKILLS		Suggested resources
<ul style="list-style-type: none"> <li>Use a term-to-term rule to generate a linear sequence</li> <li>Use a term-to-term rule to generate a non-linear sequence</li> <li>Find the term-to-term rule for a sequence</li> <li>Describe a number sequence</li> <li>Solve problems involving the term-to-term rule for a sequence</li> <li>Solve problems involving the term-to-term rule for a non-numerical sequence</li> <li>Understand the meaning of a position to term rule</li> <li>Use algebra to describe the position-to-term rule of a linear sequence</li> <li>Use the nth term of a sequence to deduce if a given number is in a sequence</li> <li>Use linear number patterns to solve problems</li> <li>Identify the first 10 triangular numbers</li> </ul>		KM: <a href="#">Maths to Infinity: Sequences</a> NRICH: <a href="#">Shifting times tables</a> NRICH: <a href="#">Odds and evens and more evens</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li><a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>
Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Know the vocabulary of sequences</li> <li>Find the next term in a linear sequence</li> <li>Find a missing term in a linear sequence</li> <li>Generate a linear sequence from its description</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>            Number and Place Value: #4, #5</p>	Pattern Sequence Linear Term Term-to-term rule Ascending Descending Expression	'Term-to-term rule' is the only new vocabulary for this unit. Position-to-term rule, and the use of the nth term, are not developed until later stages. NRICH: <a href="#">Go forth and generalise</a> NCETM: <a href="#">Algebra</a>  <b>Common approaches</b> <i>All students are taught to describe the term-to-term rule for both numerical and non-numerical sequences</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Show me a (non-)linear sequence. And another. And another.</li> <li>What's the same, what's different: 2, 5, 8, 11, 14, ... and 4, 7, 10, 13, 16, ...?</li> <li>Create a (non-linear/linear) sequence with a 3<sup>rd</sup> term of '7'</li> <li>Always/ Sometimes /Never: The 10<sup>th</sup> term of is double the 5<sup>th</sup> term of the (linear) sequence</li> <li>Kenny thinks that the 20<sup>th</sup> term of the sequence 5, 9, 13, 17, 21, ... will be 105. Do you agree with Kenny? Explain your answer.</li> </ul>		<ul style="list-style-type: none"> <li>When describing a number sequence some students may not appreciate the fact that the starting number is required as well as a term-to-term rule</li> <li>Some pupils may think that all sequences are ascending</li> <li>Some pupils may think the (2n)<sup>th</sup> term of a sequence is double the n<sup>th</sup> term of a (linear) sequence</li> </ul>

<b>KNOWLEDGE</b>	<b>The Big Picture:</b> <a href="#">Measurement and mensuration progression map</a>
<ul style="list-style-type: none"> <li>• use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places. (NEW, ALSO 6*)</li> <li>• use standard units of mass, length, time, money and other measures (including standard compound measures) using decimal quantities where appropriate (ALSO 6*)</li> <li>• change freely between related standard units (e.g. time, length, area, volume/capacity, mass) in numerical contexts</li> <li>• convert between miles and kilometres (ALSO 6*)</li> </ul>	

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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>• Convert fluently between metric units of length</li> <li>• Convert fluently between metric units of mass</li> <li>• Convert fluently between metric units of volume / capacity</li> <li>• Convert fluently between units of time</li> <li>• Convert fluently between units of money</li> <li>• Solve practical problems that involve converting between units</li> <li>• State conclusions clearly using the units correctly</li> </ul>	<p>KM: <a href="#">Sorting units</a>                      KM: <a href="#">Stick on the Maths: Units</a>                      NRICH: <a href="#">Temperature</a></p> <p><b>Learning review</b></p> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Convert between metric units</li> <li>• Use decimal notation up to three decimal places when converting metric units</li> <li>• Convert between common Imperial units; e.g. feet and inches, pounds and ounces, pints and gallons</li> <li>• Convert between units of time</li> <li>• Use 12- and 24-hour clocks, both analogue and digital</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>                      Measures: #3</p>	<p>Length, distance                      Mass, weight                      Volume                      Capacity                      Metre, centimetre, millimetre                      Tonne, kilogram, gram, milligram                      Litre, millilitre                      Hour, minute, second                      Inch, foot, yard                      Pound, ounce                      Pint, gallon                      Line segment</p> <p><b>Notation</b>                      Abbreviations of units in the metric system: m, cm, mm, kg, g, l, ml                      Abbreviations of units in the Imperial system: lb, oz</p>	<p>Weight and mass are distinct though they are often confused in everyday language. Weight is the force due to gravity, and is calculated as mass multiplied by the acceleration due to gravity. Therefore weight varies due to location while mass is a constant measurement.</p> <p>The prefix 'centi-' means one hundredth, and the prefix 'milli-' means one thousandth. These words are of Latin origin.</p> <p>The prefix 'kilo-' means one thousand. This is Greek in origin.</p> <p>Classify/Estimate angle first                      NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b>  <i>Every classroom has a sack of sand (25 kg), a bag of sugar (1 kg), a cheque book (1 cheque is 1 gram), a bottle of water (1 litre, and also 1 kg of water) and a teaspoon (5 ml)</i></p>

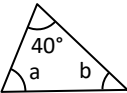
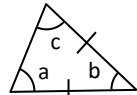
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Show me another way of describing 2.5km. And another. And another.</li> <li>• Show me another way of describing 3.4 litres. And another. And another.</li> <li>• Show me another way of describing 3.7kg. And another. And another.</li> <li>• Kenny thinks that 14:30 is the same time as 2.30 p.m. Do you agree with Kenny? Explain your answer.</li> <li>• What's the same, what's different: 2 hours 30 minutes, 2.5 hours, 2½ hours and 2 hours 20 minutes?</li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils may write amounts of money incorrectly; e.g. £3.5 for £3.50, especially if a calculator is used at any point</li> <li>• Some pupils may apply an incorrect understanding that there are 100 minutes in a hour when solving problems</li> <li>• Some pupils may struggle when converting between 12- and 24-hour clock notation; e.g. thinking that 15:00 is 5 o' clock</li> <li>• Some pupils may use the wrong scale of a protractor. For example, they measure an obtuse angle as 60° rather than 120°.</li> </ul>

KNOWLEDGE

The Big Picture: [Position and direction progression map](#)

- apply the properties of angles at a point, angles at a point on a straight line, vertically opposite angles, corresponding and alternate angles (ALSO 6\*)

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SKILLS		Suggested resources
<ul style="list-style-type: none"> <li>• Identify fluently angles at a point, angles at a point on a line and vertically opposite angles</li> <li>• Identify known angle facts in more complex geometrical diagrams</li> <li>• Use knowledge of angles to calculate missing angles in geometrical diagrams</li> <li>• Explain reasoning using vocabulary of angles</li> <li>• Identify alternate angles and know that they are equal</li> <li>• Identify corresponding angles and know that they are equal</li> </ul>		KM: <a href="#">Maths to Infinity: Lines and angles</a> KM: <a href="#">Stick on the Maths: Angles</a> NRICH: <a href="#">Triangle problem</a> NRICH: <a href="#">Square problem</a> NRICH: <a href="#">Two triangle problem</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>
Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Identify angles that meet at a point</li> <li>• Identify angles that meet at a point on a line</li> <li>• Identify vertically opposite angles</li> <li>• Know that vertically opposite angles are equal</li> </ul>	Angle Degrees Right angle Acute angle Obtuse angle Reflex angle Protractor Vertically opposite Geometry, geometrical, alternate, corresponding, interior, exterior  <b>Notation</b> Right angle notation Arc notation for all other angles The degree symbol (°)	It is important to make the connection between the total of the angles in a triangle and the sum of angles on a straight line by encouraging pupils to draw any triangle, rip off the corners of triangles and fitting them together on a straight line. However, this is not a proof and this needs to be revisited in Stage 8 using alternate angles to prove the sum is always 180°. The word 'isosceles' means 'equal legs'. What do you have at the bottom of equal legs? Equal ankles! NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Teachers convince pupils that the sum of the angles in a triangle is 180° by ripping the corners of triangles and fitting them together on a straight line.</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Show me possible values for a and b. And another. And another.</li> <li>• Convince me that the angles in a triangle total 180°</li> <li>• Convince me that the angles in a quadrilateral must total 360°</li> <li>• What's the same, what's different: Vertically opposite angles, angles at a point, angles on a straight line and angles in a triangle?</li> <li>• Kenny thinks that a triangle cannot have two obtuse angles. Do you agree? Explain your answer.</li> <li>• Jenny thinks that the largest angle in a triangle is a right angle? Do you agree? Explain your thinking.</li> </ul> 		<ul style="list-style-type: none"> <li>• Some pupils may think it's the 'base' angles of an isosceles that are always equal. For example, they may think that <math>a = b</math> rather than <math>a = c</math>.</li> </ul>  <ul style="list-style-type: none"> <li>• Some pupils may make conceptual mistakes when adding and subtracting mentally. For example, they may see that one of two angles on a straight line is 127° and quickly respond that the other angle must be 63°.</li> <li>• Avoid using the terms 'F and Z angles' to represent corresponding and alternate angles.</li> </ul>

**KNOWLEDGE**

The Big Picture: [Fractions, decimals and percentages progression map](#)

- apply the four operations, including formal written methods, to simple fractions (proper and improper), and mixed numbers
- add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions (NEW, ALSO 6\*)
- multiply simple pairs of proper fractions, writing the answer in its simplest form [for example,  $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$ ] (NEW, ALSO 6\*)
- divide proper fractions by whole numbers (for example,  $\frac{1}{3}$  divided by 2 =  $\frac{1}{6}$ )
- interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively
- compare two quantities using percentages
- solve problems involving percentage change, including percentage increase/decrease
- solve problems involving percentage change, including original value problems, and simple interest including in financial mathematics (NEW, ALSO 8\*)

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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>• Apply addition to proper fractions, improper fractions and mixed numbers</li> <li>• Apply subtraction to proper fractions, improper fractions and mixed numbers</li> <li>• Multiply proper and improper fractions</li> <li>• Multiply mixed numbers</li> <li>• Divide a proper fraction by a proper fraction</li> <li>• Apply division to improper fractions and mixed numbers</li> <li>• Use calculators to find a percentage of an amount using multiplicative methods</li> <li>• Identify the multiplier for a percentage increase or decrease</li> <li>• Use calculators to increase (decrease) an amount by a percentage using multiplicative methods</li> <li>• Compare two quantities using percentages</li> <li>• Know that percentage change = actual change ÷ original amount</li> <li>• Calculate the percentage change in a given situation, including percentage increase / decrease</li> <li>• Solve problems involving simple and compound interest</li> <li>• Solve problems involving percentage change, including original value problems</li> </ul>	<p>KM: <a href="#">Stick on the Maths: Percentage increases and decreases</a>                      KM: <a href="#">Maths to Infinity: FDP RP</a>                      KM: <a href="#">Percentage methods</a>                      NRICH: <a href="#">Would you rather?</a>                      NRICH: <a href="#">Keep it simple</a>                      NRICH: <a href="#">Egyptian fractions</a>                      NRICH: <a href="#">The greedy algorithm</a>                      NRICH: <a href="#">Fractions jigsaw</a>                      NRICH: <a href="#">Countdown fractions</a></p> <p><b>Learning review</b></p> <ul style="list-style-type: none"> <li>• <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Add and subtract fractions with different denominators</li> <li>• Add and subtract mixed numbers with different denominators</li> <li>• Multiply a proper fraction by a proper fraction</li> <li>• Divide a proper fraction by a whole number</li> <li>• Simplify the answer to a calculation when appropriate</li> <li>• Use non-calculator methods to find a percentage of an amount</li> <li>• Convert between fractions, decimals and percentages</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>                      Fractions, decimals &amp; percentages: #3, #4, #5                      Ratio and proportion: #2</p>	<p>Mixed number                      Equivalent fraction                      Simplify, cancel, lowest terms                      Proper fraction, improper fraction, top-heavy fraction, vulgar fraction                      Percent, percentage                      Multiplier                      Increase, decrease                      Compound</p> <p><b>Notation</b>                      Mixed number notation                      Horizontal / diagonal bar for fractions</p>	<p>It is important that pupils are clear that the methods for addition and subtraction of fractions are different to the methods for multiplication and subtraction. A fraction wall is useful to help visualize and re-present the calculations.</p> <p>NCETM: <a href="#">The Bar Model</a>                      NCETM: <a href="#">Teaching fractions</a>                      NCETM: <a href="#">Fractions videos</a>                      NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b>  <i>When multiplying a decimal by a whole number pupils are taught to use the corresponding whole number calculation as a general strategy</i>  <i>When adding and subtracting mixed numbers pupils are taught to convert to improper fractions as a general strategy</i>  <i>Teachers use the horizontal fraction bar notation at all times</i></p>

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Show me a proper (improper) fraction. And another. And another.</li> <li>• Show me a mixed number fraction. And another. And another.</li> <li>• Jenny thinks that you can only multiply fractions if they have the same common denominator. Do you agree with Jenny? Explain your answer.</li> <li>• Benny thinks that you can only divide fractions if they have the same common denominator. Do you agree with Jenny? Explain.</li> <li>• Kenny thinks that <math>\frac{6}{10} \div \frac{3}{2} = \frac{2}{5}</math>. Do you agree with Kenny? Explain.</li> <li>• Always/Sometimes/Never: To reverse an increase of x%, you decrease by x%</li> <li>• Lenny calculates the % increase of £6 to £8 as 25%. Do you agree with Lenny? Explain your answer.</li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils may think that you simply can simply add/subtract the whole number part of mixed numbers and add/subtract the fractional part of mixed numbers when adding/subtracting mixed numbers, e.g. <math>3\frac{1}{3} - 2\frac{1}{2} = 1\frac{-1}{6}</math></li> <li>• Some pupils may make multiplying fractions over complicated by applying the same process for adding and subtracting of finding common denominators.</li> <li>• Some pupils may think the multiplier for, say, a 20% decrease is 0.2 rather than 0.8</li> <li>• Some pupils may think that percentage change = actual change ÷ new amount</li> </ul>



## KNOWLEDGE

The Big Picture: [Algebra progression map](#)

- solve linear equations in one unknown algebraically (ALSO 6\*)
- solve linear equations with the unknown on both sides of the equation (ALSO 8\*)
- solve linear inequalities in one variable
- represent the solution of an inequality on a number line

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## SKILLS

- Choose the required inverse operation when solving an equation or inequality
- Identify the correct order of undoing the operations in an equation or inequality
- Solve one-step equations and inequalities when the solution is a whole number (fraction)
- Solve two-step equations and inequalities (including the use of brackets) when the solution is a whole number
- Solve two-step equations and inequalities (including the use of brackets) when the solution is a fraction
- Solve three-step equations and inequalities (including the use of brackets) when the solution is a whole number
- Solve three-step equations and inequalities (including the use of brackets) when the solution is a fraction
- Check the solution to an equation by substitution
- Know how to show a range of values that solve an inequality on a number line
- Know when to use an open and filled circle to represent a solution to an inequality on a number line

## Suggested resources

KM: [Spiders and snakes](#). The example is for an unknown on both sides but the same idea can be used.  
 NRICH: [Inspector Remorse](#)  
 NRICH: [Quince, quonce, quance](#)  
 NRICH: [Weighing the baby](#)

## Learning review

- [www.diagnosticquestions.com](http://www.diagnosticquestions.com)

## Prerequisites

- Know the basic rules of algebraic notation
- Express missing number problems algebraically
- Solve missing number problems expressed algebraically

## Bring on the Maths\*: Moving on up!

Algebra: #2

## Mathematical language

Algebra, algebraic, algebraically  
 Unknown  
 Equation  
 Operation  
 Solve  
 Solution  
 Brackets  
 Symbol  
 Substitute

## Notation

The lower case and upper case of a letter should not be used interchangeably when worked with algebra  
 Juxtaposition is used in place of '×'. 2a is used rather than a2.  
 Division is written as a fraction

## Agreed Common Teaching Approaches

This unit focuses on solving linear equations with unknowns on one side. Although linear equations with the unknown on both sides are addressed in Stage 8, pupils should be encouraged to think how to solve these equations by exploring the equivalent family of equations such as if  $2x = 8$  then  $2x + 2 = 10$ ,  $2x - 3 = 5$ ,  $3x = x + 8$ ,  $3x + 2 = x + 10$ , etc.

Encourage pupils to re-present the equations such as  $2x + 8 = 23$  using the Bar Model.

NCETM: [The Bar Model](#)NCETM: [Algebra](#),NCETM: [Glossary](#)

x	x	8
23		
x	x	
15		
x		
7.5		

## Common approaches

Pupils should explore solving equations by applying inverse operations, but the expectation is that all pupils should solve by balancing:

$$\begin{array}{rcl}
 2x + 8 & = & 23 \\
 -8 & & -8 \\
 \hline
 2x & = & 15 \\
 \div 2 & & \div 2 \\
 \hline
 x & = & 7.5 \text{ (or } 15/2)
 \end{array}$$

Pupils are expected to multiply out the brackets before solving an equation involving brackets. This makes the connection with two step equations such as  $2x + 6 = 22$

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions		
<ul style="list-style-type: none"> <li>Show me an (one-step, two-step) equation with a solution of 14 (positive, fractional solution). And another. And another ...</li> <li>Kenny thinks if <math>6x = 3</math> then <math>x = 2</math>. Do you agree with Kenny? Explain</li> <li>Jenny and Lenny are solving: <math>3(x - 2) = 51</math>. Who is correct? Explain</li> </ul> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; vertical-align: top;"> <p><b>Jenny's solution</b></p> <math display="block">3(x - 2) = 15</math> <math display="block">\div 3 \quad \div 3</math> <math display="block">x - 2 = 5</math> <math display="block">\div 2 \quad \div 2</math> <math display="block">x = 7</math> </td> <td style="width: 50%; vertical-align: top;"> <p><b>Lenny's solution</b></p> <math display="block">3(x - 2) = 15</math> <p style="color: red;"><i>Multiplying out brackets</i></p> <math display="block">3x - 6 = 15</math> <math display="block">+2 \quad +2</math> <math display="block">3x = 21</math> <p style="color: red;"><i>÷ 3</i></p> <math display="block">x = 7</math> </td> </tr> </table>	<p><b>Jenny's solution</b></p> $3(x - 2) = 15$ $\div 3 \quad \div 3$ $x - 2 = 5$ $\div 2 \quad \div 2$ $x = 7$	<p><b>Lenny's solution</b></p> $3(x - 2) = 15$ <p style="color: red;"><i>Multiplying out brackets</i></p> $3x - 6 = 15$ $+2 \quad +2$ $3x = 21$ <p style="color: red;"><i>÷ 3</i></p> $x = 7$		<ul style="list-style-type: none"> <li>Some pupils may think that equations always need to be presented in the form <math>ax + b = c</math> rather than <math>c = ax + b</math>.</li> <li>Some pupils may think that the solution to an equation is always positive and/or a whole number.</li> <li>Some pupils may get the use the inverse operations in the wrong order, for example, to solve <math>2x + 18 = 38</math> the pupils divide by 2 first and then subtract 18.</li> </ul>
<p><b>Jenny's solution</b></p> $3(x - 2) = 15$ $\div 3 \quad \div 3$ $x - 2 = 5$ $\div 2 \quad \div 2$ $x = 7$	<p><b>Lenny's solution</b></p> $3(x - 2) = 15$ <p style="color: red;"><i>Multiplying out brackets</i></p> $3x - 6 = 15$ $+2 \quad +2$ $3x = 21$ <p style="color: red;"><i>÷ 3</i></p> $x = 7$			

**KNOWLEDGE**

The Big Picture: [Measurement and mensuration progression map](#)

- use standard units of measure and related concepts (length, area, volume/capacity)
- **calculate perimeters of 2D shapes (ALSO 6\*)**
- **know and apply formulae to calculate area of triangles, parallelograms, trapezia**
- calculate surface area of cubes and cuboids
- calculate the surface area of a triangular prism when lengths are known
- **know and apply formulae to calculate volume of cuboids**
- **understand and use standard mathematical formulae**

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**SKILLS** Suggested resources

- Recognise that the value of the perimeter can equal the value of area
- Use standard formulae for area and volume
- Find missing lengths in 2D shapes when the area is known
- Find the area and perimeter of squares, rectangles, parallelograms and triangles
- Find the area and perimeter of compound shapes
- Know that the area of a trapezium is given by the formula  $\text{area} = \frac{1}{2} \times (a + b) \times h = \left(\frac{a+b}{2}\right)h = \frac{(a+b)h}{2}$
- Calculate the area of a trapezium
- Understand the meaning of surface area
- Find the surface area and volume of cuboids (including cubes) when lengths are known
- Find the surface area and volume of a triangular prism when lengths are known
- Find missing lengths in 3D shapes when the volume or surface area is known

- KM: [Equable shapes](#) (for both 2D and 3D shapes)
- KM: [Triangle takeaway](#)
- KM: [Surface area](#)
- KM: [Class of rice](#)
- KM: [Stick on the Maths: Area and Volume](#)
- KM: [Maths to Infinity: Area and Volume](#)
- NRICH: [Can They Be Equal?](#)

**Learning review**

- [www.diagnosticquestions.com](http://www.diagnosticquestions.com)

**Prerequisites** **Mathematical language** **Agreed Common Teaching Approaches**

- Understand the meaning of area, perimeter, volume and capacity
- Know how to calculate areas of rectangles, parallelograms and triangles using the standard formulae
- Know that the area of a triangle is given by the formula  $\text{area} = \frac{1}{2} \times \text{base} \times \text{height} = \text{base} \times \text{height} \div 2 = \frac{bh}{2}$
- Know appropriate metric units for measuring area and volume

**Bring on the Maths\*: Moving on up!**

Measures: #4, #5, #6

Perimeter, area, volume, capacity, surface area  
 Square, rectangle, parallelogram, triangle, trapezium (trapezia)  
 Polygon  
 Cube, cuboid  
 Square 18isualize18, square 18isualize18, square metre, square 18isualize  
 Cubic 18isualize18, 18isualize18 cube  
 Formula, formulae  
 Length, breadth, depth, height, width

**Notation**

Abbreviations of units in the metric system: km, m, cm, mm, mm<sup>2</sup>, cm<sup>2</sup>, m<sup>2</sup>, km<sup>2</sup>, mm<sup>3</sup>, cm<sup>3</sup>, km<sup>3</sup>

Ensure that pupils make connections with the area and volume work in Stage 6 and below, in particular the importance of the perpendicular height.  
 NCETM: [Glossary](#)

**Common approaches**

*Pupils have already derived the formula for the area of a parallelogram. They use this to derive the formula for the area of a trapezium as  $\frac{(a+b)h}{2}$  by copying and rotating a trapezium as shown above.*



*Pupils use the area of a triangle as given by the formula  $\text{area} = \frac{bh}{2}$ .*

*Every classroom has a set of [area posters](#) on the wall.*

**Reasoning opportunities and probing questions** **Cross Curricular Links** **Possible misconceptions**

- Always / Sometimes / Never: The value of the volume of a cuboid is greater than the value of the surface area
- Convince me that the area of a triangle =  $\frac{1}{2} \times \text{base} \times \text{height} = \text{base} \times \text{height} \div 2 = \frac{bh}{2}$
- (Given a right-angled trapezium with base labelled 8 cm, height 5 cm, top 6 cm) Kenny uses the formula for the area of a trapezium and Benny splits the shape into a rectangle and a triangle. What would you do? Why?
- Find me a cuboid with a surface area of 120cm<sup>2</sup>

- Some pupils may use the sloping height when finding the areas of parallelograms, triangles and trapezia
- Some pupils may think that the area of a triangle is found using  $\text{area} = \text{base} \times \text{height}$
- Some pupils may think that you multiply all the numbers to find the area of a shape
- Some pupils may confuse the concepts of surface area and volume
- Some pupils may only find the area of the three 'distinct' faces when finding surface area

## Checking, approximating and estimating

Stage 8\*

3 hours

### KNOWLEDGE

The Big Picture: [Number and Place Value progression map](#)

- round numbers and measures to an appropriate degree of accuracy (e.g. to a specified number of decimal places or significant figures)
- estimate answers; check calculations using approximation and estimation, including answers obtained using technology
- solve problems which require answers to be rounded to specified degrees of accuracy (NEW, ALSO 6\*)
- recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions)

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SKILLS		Suggested resources
<ul style="list-style-type: none"> <li>• Approximate by rounding to any number of decimal places or significant figures</li> <li>• Know how to identify the first significant figure in any number</li> <li>• Approximate by rounding to the first significant figure in any number</li> <li>• Understand estimating as the process of finding a rough value of an answer or calculation</li> <li>• Use estimation to predict the order of magnitude of the solution to a (decimal) calculation</li> <li>• Estimate calculations by rounding numbers to one significant figure</li> </ul>		KM: <a href="#">Approximating calculations</a> KM: <a href="#">Stick on the Maths: CALC6: Checking solutions</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li>• KM: <a href="#">7M6 BAM Task</a></li> </ul>
Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>• Approximate any number by rounding to the nearest 10, 100 or 1000, 10 000, 100 000 or 1 000 000</li> <li>• Approximate any number with one or two decimal places by rounding to the nearest whole number</li> <li>• Approximate any number with two decimal places by rounding to the one decimal place</li> <li>• Simplify a fraction by cancelling common factors</li> </ul>	Approximate (noun and verb) Round Decimal place Check Solution Answer Estimate (noun and verb) Order of magnitude Accurate, Accuracy Significant figure Cancel Inverse Operation  <b>Notation</b> The approximately equal symbol ( $\approx$ ) Significant figure is abbreviated to 's.f.' or 'sig fig'	This unit is an opportunity to develop and practice calculation skills with a particular emphasis on checking, approximating or estimating the answer. Pupils should be able to estimate calculations involving integers and decimals. Also see big pictures: <a href="#">Calculation progression map</a> and <a href="#">Fractions, decimals and percentages progression map</a> NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>All pupils are taught to visualize rounding through the use of a number line</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Convince me that 39 652 rounds to 40 000 to one significant figure</li> <li>• Convince me that 0.6427 does <u>not</u> round to 1 to one significant figure</li> <li>• What is wrong: <math>\frac{11 \times 28.2}{0.54} \approx \frac{10 \times 30}{0.5} = 150</math>. How can you correct it?</li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils may truncate instead of round</li> <li>• Some pupils may round down at the half way point, rather than round up.</li> <li>• Some pupils may think that a number between 0 and 1 rounds to 0 or 1 to one significant figure</li> <li>• Some pupils may divide by 2 when the denominator of an estimated calculation is 0.5</li> </ul>

KNOWLEDGE

The Big Picture: [Position and direction progression map](#)

- work with coordinates in all four quadrants
- **understand and use lines parallel to the axes,  $y = x$  and  $y = -x$**
- **plot graphs of equations that correspond to straight-line graphs in the coordinate plane (NEW)**
- **solve geometrical problems on coordinate axes**
- **identify, describe and construct congruent shapes including on coordinate axes, by considering rotation, reflection and translation**
- **describe translations as 2D vectors (ALSO 6\*)**

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SKILLS

- Plot co-ordinates in all four quadrants
- Draw axis and scale them correctly
- Write the equation of a line parallel to the x-axis or the y-axis
- Draw a line parallel to the x-axis or the y-axis given its equation
- Identify the lines  $y = x$  and  $y = -x$
- Draw the lines  $y = x$  and  $y = -x$
- Draw simple straight lines e.g.  $y = 2x + 1$
- Carry out a reflection in a given equation (e.g.  $y = 3$  and  $y = x$ )
- Find and name the equation of the mirror line for a given reflection
- Describe a translation as a 2D vector
- Carry out a translation using a vector
- Understand the concept and language of rotations
- Describe a rotation using a centre, a direction and an angle of turn
- Carry out a rotation using a given angle, direction and centre of rotation
- Describe a rotation using mathematical language

Suggested resources

- KM: [Lines](#)  
 KM: [Moving house](#)  
 KM: [Autograph transformations](#)  
 KM: [Stick on the Maths SSM7: Transformations](#)  
 NRICH: [Transformation Game](#)
- Learning review**
- KM: [7M11 BAM Task](#)

Prerequisites Mathematical language Agreed Common Teaching Approaches

- Work with coordinates in all four quadrants
  - Carry out a reflection in a given vertical or horizontal mirror line
  - Carry out a translation
- Bring on the Maths+: Moving on up!**  
 Position and direction: #1, #2

(Cartesian) coordinates  
 Axis, axes, x-axis, y-axis  
 Origin  
 Quadrant  
 Translation, Reflection, Rotation  
 Transformation  
 Object, Image  
 Congruent, congruence  
 Mirror line  
 Vector  
 Centre of rotation

**Notation**  
 Cartesian coordinates should be separated by a comma and enclosed in brackets (x, y)  
 Vector notation  $\begin{pmatrix} a \\ b \end{pmatrix}$  where a = movement right and b = movement up

Pupils should be able to use a centre of rotation that is outside, inside, or on the edge of the object  
 Pupils should be encouraged to see the line  $x = a$  as the complete (and infinite) set of points such that the x-coordinate is a.  
 The French mathematician Rene Descartes introduced Cartesian coordinates in the 17<sup>th</sup> century. It is said that he thought of the idea while watching a fly moving around on his bedroom ceiling.  
 NCETM: [Glossary](#)

**Common approaches**  
*Pupils use ICT to explore these transformations*  
*Teachers do not use the phrase 'along the corridor and up the stairs' as it can encourage a mentality of only working in the first quadrant. Later, pupils will have to use coordinates in all four quadrants. A more helpful way to remember the order of coordinates is 'x is a cross, wise up!'*  
*Teachers use the language 'negative number', and not 'minus number', to avoid future confusion with calculations.*

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>• Always / Sometimes / Never: The centre of rotation is in the centre of the object</li> <li>• Convince me that <math>y = 0</math> is the x-axis</li> <li>• Always / Sometimes / Never: The line <math>x = a</math> is parallel to the x-axis</li> </ul>		<ul style="list-style-type: none"> <li>• Some pupils will wrestle with the idea that a line <math>x = a</math> is parallel to the y-axis</li> <li>• When describing or carrying out a translation, some pupils may count the squares between the two shapes rather than the squares that describe the movement between the two shapes.</li> <li>• When reflecting a shape in a diagonal mirror line some students may draw a translation</li> <li>• Some pupils may think that the centre of rotation is always in the centre of the shape</li> <li>• Some pupils will confuse the order of x- and y-coordinates</li> <li>• When constructing axes, some pupils may not realise the importance of equal divisions on the axes</li> </ul>

<b>KNOWLEDGE</b>	<b>The Big Picture:</b> <a href="#">Probability progression map</a>
<ul style="list-style-type: none"> <li>relate relative expected frequencies to theoretical probability, using appropriate language and the 0 – 1 probability scale (ALSO 6*)</li> <li>record describe and analyse the frequency of outcomes of probability experiments using tables and frequency trees (ALSO 8*)</li> <li>construct theoretical possibility spaces for single and combined experiments with equally likely outcomes and use these to calculate theoretical probabilities</li> <li>apply the property that the probabilities of an exhaustive set of outcomes sum to one (ALSO 6*)</li> <li>apply ideas of randomness, fairness and equally likely events to calculate expected outcomes of multiple future experiments (NEW)</li> </ul>	

SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>Know that probability is a way of measuring likeliness and know and use the vocabulary of probability</li> <li>Understand the use of the 0-1 scale to measure probability (FDP)</li> <li>Assess likeliness and place events on a probability scale</li> <li>List all the outcomes for an experiment</li> <li>Identify equally likely outcomes</li> <li>Use sample spaces to work out theoretical probabilities for events with equally likely outcomes</li> <li>Recognise when it is not possible to work out a theoretical probability for an event</li> <li>Know that the sum of probabilities for all outcomes is 1</li> <li>Apply the fact that the sum of probabilities for all outcomes is 1</li> <li>Calculate expected outcomes of future experiments with equally likely events</li> <li>Use a tree diagram to calculate the probability of two events</li> </ul>	<p>KM: <a href="#">Probability scale</a> and <a href="#">slideshow version</a>                      KM: <a href="#">Probability loop cards</a>                      NRICH: <a href="#">Dice and spinners interactive</a></p> <p><b>Learning review</b></p> <ul style="list-style-type: none"> <li><a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Understand the equivalence between fractions, decimals and percentages</li> <li>Compare fractions, decimals or percentages</li> <li>Simplify a fraction by cancelling common factors</li> </ul>	Probability, Theoretical probability Event Outcome Impossible, Unlikely, Evens chance, Likely, Certain Equally likely Mutually exclusive Exhaustive Possibility space Experiment  <b>Notation</b> Probabilities are expressed as fractions, decimals or percentage. They should not be expressed as ratios (which represent odds) or as words	It is not immediately apparent how to use words to label the middle of the probability scale. ‘Evens chance’ is a common way to do so, although this can be misleading as it could be argued that there is an even chance of obtaining any number when rolling a fair die. NRICH: <a href="#">Introducing probability</a> NRICH: <a href="#">Why Do People Find Probability Unintuitive and Difficult?</a> NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Every classroom has a display of a probability scale labeled with words and numbers. Pupils create events and outcomes that are placed on this scale.</i>
Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Show me an example of an event and outcome with a probability of 0. And another. And another...</li> <li>Always / Sometimes / Never: if I pick a card from a pack of playing cards then the probability of picking a club is <math>\frac{1}{4}</math></li> <li>Label this (eight-sided) spinner so that the probability of scoring a 2 is <math>\frac{1}{4}</math>.</li> </ul>		<ul style="list-style-type: none"> <li>Some pupils will initially think that, for example, the probability of it raining tomorrow is <math>\frac{1}{2}</math> as it either will or it won't.</li> <li>Some students may write a probability as odds (e.g. 1:6 or ‘1 to 6’). There is a difference between probability and odds, and therefore probabilities must only be written as fractions, decimals or percentages.</li> <li>Some pupils may think that, for example, if they flip a fair coin three times and obtain three heads, then it must be more than likely they will obtain a head next.</li> </ul>



<a href="#">Presentation of data</a>	<a href="#">Stage 8*</a>	6 hours
<b>KNOWLEDGE</b> <ul style="list-style-type: none"> <li>interpret and construct tables, charts and diagrams, including frequency tables, bar charts, frequency diagrams, pie charts and pictograms for categorical data, vertical line charts for ungrouped discrete numerical data and know their appropriate use</li> </ul>		The Big Picture: <a href="#">Statistics progression map</a>

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SKILLS	Suggested resources
<ul style="list-style-type: none"> <li>Know the meaning of categorical and numerical data</li> <li>Know the meaning of discrete and continuous data</li> <li>Interpret and construct frequency tables</li> <li>Construct and interpret pictograms (bar charts, tables) and know their appropriate use</li> <li>Construct and interpret comparative bar charts</li> <li>Interpret pie charts and know their appropriate use</li> <li>Construct pie charts when the total frequency is not a factor of 360</li> <li>Choose appropriate graphs or charts to represent data</li> <li>Construct and interpret vertical line charts</li> </ul>	KM: <a href="#">Maths to Infinity: Averages, Charts and Tables</a> NRICH: <a href="#">Picturing the World</a> NRICH: <a href="#">Charting Success</a>  <b>Learning review</b> <ul style="list-style-type: none"> <li><a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a></li> </ul>

Prerequisites	Mathematical language	Agreed Common Teaching Approaches
<ul style="list-style-type: none"> <li>Construct and interpret a pictogram</li> <li>Construct and interpret a bar chart</li> <li>Construct and interpret a line graph</li> <li>Understand that pie charts are used to show proportions</li> <li>Use a template to construct a pie chart by scaling frequencies</li> </ul> <p><b>Bring on the Maths*: Moving on up!</b>            Statistics: #1, #2, #3</p>	Data, Categorical data, Discrete data Pictogram, Symbol, Key Frequency Table, Frequency table Tally Bar chart Time graph, Time series Bar-line graph, Vertical line chart Scale, Graph Axis, axes Line graph Pie chart Sector Angle Maximum, minimum  <b>Notation</b> When tallying, groups of five are created by striking through each group of four	In stage 6 pupils constructed pie charts when the total of frequencies is a factor of 360. More complex cases can now be introduced. Much of the content of this unit has been covered previously in different stages. This is an opportunity to bring together the full range of skills encountered up to this point, and to develop a more refined understanding of usage and vocabulary.  William Playfair, a Scottish engineer and economist, introduced the bar chart and line graph in 1786. He also introduced the pie chart in 1801. NCETM: <a href="#">Glossary</a>  <b>Common approaches</b> <i>Pie charts are constructed by calculating the angle for each section by dividing 360 by the total frequency and not using percentages. The angle for the first section is measured from a vertical radius. Subsequent sections are measured using the boundary line of the previous section.</i>

Reasoning opportunities and probing questions	Cross Curricular Links	Possible misconceptions
<ul style="list-style-type: none"> <li>Show me a pie chart representing the following information: Blue (30%), Red (50%), Yellow (the rest). And another. And another.</li> <li>Always / Sometimes / Never: Bar charts are vertical</li> <li>Always / Sometimes / Never: Bar charts, pie charts, pictograms and vertical line charts can be used to represent any data</li> <li>Kenny says 'If two pie charts have the same section then the amount of data the section represents is the same in each pie chart.' Do you agree with Kenny? Explain your answer.</li> </ul>		<ul style="list-style-type: none"> <li>Some pupils may think that a line graph is appropriate for discrete data</li> <li>Some pupils may think that each square on the grid used represents one unit</li> <li>Some pupils may confuse the fact that the sections of the pie chart total 100% and 360°</li> <li>Some pupils may not leave gaps between the bars of a bar chart</li> </ul>

<a href="#">Measuring data</a>	<a href="#">Stage 8*</a>	3 hours
<b>KNOWLEDGE</b> <ul style="list-style-type: none"> <li>Interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate measures of central tendency (median, mean and mode) and spread (range) (ALSO 6*)</li> </ul>		The Big Picture: <a href="#">Statistics progression map</a>

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SKILLS		SUGGESTED RESOURCES
<ul style="list-style-type: none"> <li>Investigate averages</li> <li>Explore ways of summarising data</li> <li>Analyse and compare sets of data</li> <li>Understand the mode and median as measures of typicality (or location)</li> <li>Find the mode of set of data</li> <li>Find the median of a set of data</li> <li>Find the median of a set of data when there are an even number of numbers in the data set</li> <li>Use the mean to find a missing number in a set of data</li> <li>Calculate the mean from a frequency table</li> <li>Find the mode from a frequency table</li> <li>Find the median from a frequency table</li> <li>Understand the range as a measure of spread (or consistency)</li> <li>Calculate the range of a set of data</li> <li>Analyse and compare sets of data</li> <li>Appreciate the limitations of different statistics (mean, median, mode, range)</li> </ul>		<ul style="list-style-type: none"> <li></li> </ul>
Prerequisites	Mathematical language	Pedagogical notes
<ul style="list-style-type: none"> <li>Understand the meaning of 'average' as a typicality (or location)</li> <li>Calculate the mean of a set of data</li> </ul> <p><b>Bring on the Maths<sup>+</sup>: Moving on up!</b> Statistics: #4</p>	Average Spread Consistency Mean Median Mode Range Measure Data Statistic Statistics Approximate Round	<p>The word 'average' is often used synonymously with the mean, but it is only one type of average. In fact, there are several different types of mean (the one in this unit properly being named as the 'arithmetic mean'). NCETM: <a href="#">Glossary</a></p> <p><b>Common approaches</b> Every classroom has a set of <a href="#">statistics posters</a> on the wall Always use brackets when writing out the calculation for a mean, e.g. <math>(2 + 3 + 4 + 5) \div 4 = 14 \div 4 = 3.5</math></p>
Reasoning opportunities and probing questions	Suggested resources	Possible misconceptions
<ul style="list-style-type: none"> <li>Show me a set of data with a mean (mode, median, range) of 5.</li> <li>Always / Sometimes / Never: The mean is greater than the mode for a set of data</li> <li>Always / Sometimes / Never: The mean is greater than the median for a set of data</li> <li>Convince me that a set of data could have more than one mode.</li> <li>What's the same and what's different: mean, mode, median, range?</li> </ul>	KM: <a href="#">Maths to Infinity: Averages</a> KM: <a href="#">Maths to Infinity: Averages, Charts and Tables</a> KM: <a href="#">Stick on the Maths HD4: Averages</a> NRICH: <a href="#">M, M and M</a> NRICH: <a href="#">The Wisdom of the Crowd</a>  <b>Learning review</b> <a href="http://www.diagnosticquestions.com">www.diagnosticquestions.com</a>	<ul style="list-style-type: none"> <li>If using a calculator some pupils may not use the '=' symbol (or brackets) correctly; e.g. working out the mean of 2, 3, 4 and 5 as <math>2 + 3 + 4 + 5 \div 4 = 10.25</math>.</li> <li>Some pupils may think that the range is a type of average</li> <li>Some pupils may think that a set of data with an even number of items has two values for the median, e.g. 2, 4, 5, 6, 7, 8 has a median of 5 and 6 rather than 5.5</li> <li>Some pupils may not write the data in order before finding the median.</li> </ul>