**Mathematics overview: Stage 8\***

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| *Unit* | *Hours* | *KNOWLEDGE* |
| [Numbers and the number system](#NANS) | 12 | * **use the concepts and vocabulary of prime numbers, highest common factor, lowest common multiple, prime factorisation, including using product notation and the unique factorisation theorem (7\*, 8\*)**
* **interpret standard form *A* × 10n, where 1 ≤ *A* < 10 and *n* is an integer (8\*, 9\*)**
* **apply the four operations, including formal written methods, to integers, decimals and simple fractions (proper and improper), and mixed numbers – all both positive and negative (8\*)**
* **use conventional notation for priority of operations, including brackets, powers, roots and reciprocals (7\*, 8\*)**
* **calculate with roots, and with integer indices (8\*, 9\*)**
* **use inequality notation to specify simple error intervals due to truncation or rounding (8\*, 9\*)**
* **measure line segments and angles in geometric figures, including interpreting maps and scale Drawings (8\*)**
* **interpret plans and elevations of 3D shapes (8\*)**
* **identify, describe and construct similar shapes, including on coordinate axes, by considering enlargement (7\*, 8\*)**
* **use the standard ruler and compass constructions (perpendicular bisector of a line segment, constructing a perpendicular to a given line from/at a given point, bisecting a given angle) (8\*, 9\*)**
* **use and interpret algebraic notation, including: *a*²*b* in place of *a* × *a* × *b*, coefficients written as fractions rather than as decimals (7\*, 8\*)**
* **rearrange formulae to change the subject (8\*, 9\*)**
* **argue mathematically to show algebraic expressions are equivalent, and use algebra to support and construct arguments (8\*)**
* **translate simple situations or procedures into algebraic expressions or formulae (8\*)**
* **work interchangeably with terminating decimals and their corresponding fractions (such as 3.5 and 7/2 or 0.375 or 3/8) (8\*)**
* **express the division of a quantity into two parts as a ratio; apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) (7\*, 8\*,9\*)**
* **understand and use proportion as equality of ratios (8\*)**
* **express a multiplicative relationship between two quantities as a ratio or a fraction (8\*)**
* **relate ratios to fractions and to linear functions (8\*)**
* **use compound units (such as speed, rates of pay, unit pricing and density (8\*, 9\*)**
* **solve problems involving direct and inverse proportion, including graphical and algebraic representations (8\*,9\*)**
* **generate terms of a sequence from either a term-to-term or a position-to-term rule (7\*,8\*)**
* **deduce expressions to calculate the nth term of linear sequences (7\*, 8\*)**
* **recognise and use Fibonacci type sequences (8\*)**
* **derive and use the sum of angles in a triangle (e.g. to deduce and use the angle sum in any polygon, and to derive properties of regular polygons) (8\*)**
* **interpret fractions and percentages as operators (8\*)**
* **solve problems involving percentage change, percentage increase and decrease, including original value problems, and simple interest including in financial mathematics (7\*, 8\*)**
* **express one quantity as a fraction of another where the fraction is less than 1 and greater than 1 (8\*)**
* **solve linear equations with the unknown on both sides of the equation (7\*, 8\*)**
* **find approximate solutions to linear equations using a graph (8\*)**
* **find approximate solutions to simultaneous equations using a graph (8\*)**
* **compare lengths, areas and volumes using ratio notation (8\*)**
* **calculate perimeters of 2D shapes, including circles (8\*)**
* **know the formulae: circumference of a circle = 2πr = πd, area of a circle = πr² (8\*)**
* **calculate areas of circles and composite shapes (8\*)**
* **know the formulae for: Pythagoras’ theorem, a² + b² = c², and apply it to find lengths in right-angled triangles in two dimensional figures (8\*, 9\*)**
* **know and apply formulae to calculate volume of right prisms (including cylinders) (8\*)**
* **identify and interpret gradients and intercepts of linear functions graphically and algebraically (8\*, 9\*)**
* **recognise, sketch and interpret graphs of linear functions and simple quadratic functions (8\*, 9\*)**
* **interpret graphs and graphs of non-standard (*piece-wise linear)* functions in real contexts, to find approximate solutions to problems such as**
* **interpret the gradient of a straight line graph as a rate of change (8\*)**
* **apply systematic listing strategies (8\*)**
* **record describe and analyse the frequency of outcomes of probability experiments using frequency trees (7\*,8\*)**
* **enumerate sets and combinations of sets systematically, using tables, grids and Venn diagrams (8\*,9\*)**
* **interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate graphical representation involving discrete, continuous and grouped data (8\*)**
* **use and interpret scatter graphs of bivariate data (8\*)**
* **recognise correlation (8\*)**
* **draw estimated lines of best fit; make predictions (8\*)**
* **know correlation does not indicate causation; interpolate and extrapolate apparent trends whilst knowing the dangers of so doing (8\*)**
* **interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate measures of central tendency (median, mean, mode and modal class) and spread (range, including consideration of outliers) (7\*, 8\*)**

**Key Stage 4*** **calculate with standard form A × 10n, where 1 ≤ A < 10 and n is an integer (KS4 (9\*)**
* **simplify and manipulate algebraic expressions by expanding products of two binomials and factorising quadratic expressions of the form x² + bx + c (KS4 (9\*))**
* **recognise and use quadratic sequences (KS4, 9\*)**
* **calculate exactly with multiples of pi (KS4)**
* **simple kinematic problems involving distance and speed (KS4 (9\*))**
* **use the form *y = mx + c* to identify parallel lines (KS4)**
* **enumerate sets and combinations of sets systematically, using tree diagrams (KS4 (9\*))**
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| [Calculating](#C) | 12 |
| [Visualising and constructing](#VC) | 12 |
| [Algebraic proficiency: tinkering](#APT) | 12 |
| [Exploring fractions, decimals and percentages](#EFDP) | 4 |
| [Proportional reasoning](#PR) | 12 |
| [Pattern sniffing](#PS) | 4 |
| [Investigating angles](#IA) | 8 |
| [Calculating fractions, decimals and percentages](#CFDP) | 8 |
| [Solving equations and inequalities](#SEI) | 4 |
| [Calculating space](#CS) | 12 |
| [Algebraic proficiency: visualising](#APV) | 12 |
| [Understanding risk II](#UR2) | 8 |
| [Presentation of data](#PD) | 8 |
| [Measuring data](#MD) | 8 |
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| *[Numbers and the number system](file:///%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Numbers%20and%20The%20Number%20System.xlsx)* | Stage 9\* | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Number and Place Value progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_NumberPlaceValue.xlsx) |
| * **use the concepts and vocabulary of prime numbers, highest common factor, lowest common multiple, prime factorisation, including using product notation and the unique factorisation theorem (7\*, 8\*)**
* **interpret standard form *A* × 10n, where 1 ≤ *A* < 10 and *n* is an integer (8\*, 9\*)**
* **calculate with standard form A × 10n, where 1 ≤ A < 10 and n is an integer (KS4 (9\*)**
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| SKILLS | Suggested resources  |
| * Recall prime numbers up to 100
* Understand the meaning of prime factor
* Write a number as a product of its prime factors
* Use a Venn diagram to sort information
* Use prime factorisations to find the highest common factor of two numbers
* Use prime factorisations to find the lowest common multiple of two numbers
* Use a Venn diagram to find hcf and lcm of two numbers
* Know how to identify the first (any) significant figure in any number
* Know how to round to the first (any) significant figure in any number
* Review of the multiplication and division rule of indices
* Write a large (small) number in standard form
* Interpret a large (small) number written in standard form
* Enter a calculation written in standard form into a scientific calculator
* Interpret the standard form display of a scientific calculator
* Convert the answer from a standard form calculation back to a standard form answer
* Add (subtract) numbers written in standard form
* Multiply (divide) numbers written in standard form
* Calculate with negative indices in the context of standard form
 | KM: [Astronomical numbers](http://kangaroomaths.com/free_resources/teaching/number/astro_numbers.docx)KM: [Interesting standard form](http://kangaroomaths.com/free_resources/teaching/number/interesting_standard_form.docx)KM: [Powers of ten](http://kangaroomaths.com/free_resources/teaching/number/powers_of_ten.xlsx)KM: [Maths to Infinity: Standard form](http://kangaroomaths.com/free_resources/infinity/standard_form.xlsm)[Powers of ten](http://www.powersof10.com/film) film (external site)[The scale of the universe](http://htwins.net/scale2/) animation (external site)**Learning review*** [www.diagnosticquestions.com](http://www.diagnosticquestions.com)
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| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Know the meaning of a prime number
* Recall prime numbers up to 50
* Understand the use of notation for powers
* Know how to round to the nearest whole number, 10, 100, 1000 and to decimal places
* Multiply and divide numbers by powers of 10
 | PrimePrime factorPrime factorisationProductVenn diagramHighest common factorLowest common multipleStandard formSignificant figure**Notation**Index notation: e.g. 53 is read as ‘5 to the power of 3’ and means ‘3 lots of 5 multiplied together’Standard form (see key concepts) is sometimes called ‘standard index form’, or more properly, ‘scientific notation’ | Pupils should explore the ways to enter and interpret numbers in standard form on a scientific calculator. Different calculators may very well have different displays, notations and methods.Liaise with the science department to establish when students first meet the use of standard form, and in what contexts they will be expected to interpret it.NRICH: [Divisibility testing](http://nrich.maths.org/1308)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***The following definition of a prime number should be used in order to minimise confusion about 1: A prime number is a number with exactly two factors.**The description ‘standard form’ is always used instead of ‘scientific notation’ or ‘standard index form’* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me two (three-digit) numbers with a highest common factor of 18. And another. And another…
* Show me two numbers with a lowest common multiple of 240. And another. And another…
* Jenny writes 7.1 × 10-5 = 0.0000071. Kenny writes 7.1 × 10-5 = 0.000071. Who do you agree with? Why?
 |  | * Many pupils believe that 1 is a prime number – a misconception which can arise if the definition is taken as ‘a number which is divisible by itself and 1’
* Some pupils may think 35 934 = 36 to two significant figures
* When converting between ordinary and standard form some pupils may incorrectly connect the power to the number of zeros; e.g. 4 × 105 = 400 000 so 4.2 × 105 = 4 200 000
* Similarly, when working with small numbers (negative powers of 10) some pupils may think that the power indicates how many zeros should be placed between the decimal point and the first non-zero digit
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| *[Calculating](file:///%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Calculating.xlsx)* | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Calculation progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_NumberCalculation.xlsx) |
| * **apply the four operations, including formal written methods, to integers, decimals and simple fractions (proper and improper), and mixed numbers – all both positive and negative (8\*)**
* **use conventional notation for priority of operations, including brackets, powers, roots and reciprocals (7\*, 8\*)**
* **calculate with roots, and with integer indices (8\*, 9\*)**
* **use inequality notation to specify simple error intervals due to truncation or rounding (8\*, 9\*)**
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| SKILLS | Suggested resources  |
| * Add or subtract from a negative number
* Add (or subtract) a negative number to (from) a positive number
* Add (or subtract) a negative number to (from) a negative number
* Multiply with negative numbers
* Divide with negative numbers
* Know how to square (or cube) a negative number, and understand why (at this level) you cannot square root a negative number
* Estimating the square root of a none square number
* Enter negative numbers into a calculator
* Interpret a calculator display when working with negative numbers
* Substitution and the application of the 4 operations and BIDMAS
* Understand how to use the order of operations including powers
* Understand how to use the order of operations including roots
* Calculate with positive indices (roots) using written methods
* Identify the minimum and maximum values of an amount that has been rounded (to nearest x, x d.p., x s.f.)
* Use inequalities to describe the range of values for a rounded value
* Solve problems involving the maximum and minimum values of an amount that has been rounded
* Introduce simple Upper / Lower Bound calculations
 | KM: [Summing up](http://kangaroomaths.com/free_resources/teaching/number/add_subtract_negatives.docx)KM: [Developing negatives](http://kangaroomaths.com/free_resources/teaching/number/mult_divide_negatives.docx)KM: [Sorting calculations](http://kangaroomaths.com/free_resources/teaching/number/sorting_calculations.docx)KM: [Maths to Infinity: Directed numbers](http://kangaroomaths.com/free_resources/infinity/directed_numbers.xlsm)Standards Unit: [N9 Evaluating directed number statements](http://www.nationalstemcentre.org.uk/elibrary/resource/1966/evaluating-directed-number-statements-n9)NRICH: [Working with directed numbers](http://nrich.maths.org/9919)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Fluently recall and apply multiplication facts up to 12 × 12
* Know and use column addition and subtraction
* Know the formal written method of long multiplication
* Know the formal written method of short division
* Convert between an improper fraction and a mixed number
* Know the order of operations for the four operations and brackets

**Bring on the Maths+: Moving on up!**Number and Place Value: v3 | Negative numberDirected numberImproper fractionTop-heavy fractionMixed numberOperationInverseLong multiplicationShort divisionPowerIndicesRoots | Pupils need to know how to enter negative numbers into their calculator and how to interpret the display.The grid method is promoted as a method that aids numerical understanding and later progresses to multiplying algebraic statements.NRICH: [Adding and subtracting positive and negative numbers](http://nrich.maths.org/5947)NRICH: [History of negative numbers](http://nrich.maths.org/5747)NCETM: [Departmental workshop: Operations with Directed Numbers](https://www.ncetm.org.uk/resources/10331)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Teachers use the language ‘negative number’, and not ‘minus number’, to avoid confusion with calculations**Every classroom has a* [*negative number washing line*](http://kangaroomaths.com/free_resources/display/number_line.docx) *on the wall**Long multiplication and short division are to be promoted as the ‘most efficient methods’.* *If any acronym is promoted to help remember the order of operations, then BIDMAS is used as the I stands for indices.* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Convince me that -3 - -7 = 4
* Show me an example of a calculation involving addition of two negative numbers and the solution -10. And another. And another …
* Create a Carroll diagram with ‘addition’, ‘subtraction’ as the column headings and ‘one negative number’, ‘two negative numbers’ as the row headings. Ask pupils to create (if possible) a calculation that can be placed in each of the four positions. If they think it is not possible, explain why. Repeat for multiplication and division.
 |  | * Some pupils may use a rule stated as ‘two minuses make a plus’ and make many mistakes as a result; e.g. -4 + -6 = 10
* Some pupils may incorrectly apply the principle of commutativity to subtraction; e.g. 4 – 7 = 3
* The order of operations is often not applied correctly when squaring negative numbers. As a result pupils may think that x2 = -9 when x = -3. The fact that a calculator applies the correct order means that -32 = -9 and this can actually reinforce the misconception. In this situation brackets should be used as follows: (-3)2 = 9.
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| *Visualising and constructing* | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE*** **measure line segments and angles in geometric figures, including interpreting maps and scale Drawings (8\*)**
* **interpret plans and elevations of 3D shapes (8\*)**
 | **The Big Picture**: [Properties of Shape progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_GeometryPropertiesShape.xlsx) |
| * **identify, describe and construct similar shapes, including on coordinate axes, by considering enlargement (7\*, 8\*)**
* **use the standard ruler and compass constructions (perpendicular bisector of a line segment, constructing a perpendicular to a given line from/at a given point, bisecting a given angle) (8\*, 9\*)**
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| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Use the concept of scaling in diagrams
* Recap alternate, corresponding, interior and opposite angles
* Measure and state a specified bearing
* Construct a scale diagram involving bearings
* Use bearings to solve geometrical problems
* Understand the concept of back bearings
* Know the vocabulary of enlargement
* Find the centre of enlargement
* Find the scale factor of an enlargement
* Use the centre and scale factor to carry out an enlargement with positive and/or negative integer and fractional scale factors
* Know and understand the vocabulary of plans and elevations
* Interpret plans and elevations
 | KM: [Outdoor Leisure 13](http://kangaroomaths.com/free_resources/teaching/geometry/ol13.docx)KM: [Airports and hilltops](http://kangaroomaths.com/free_resources/teaching/geometry/airports_and_hilltops.docx)KM: [Plans and elevations](http://kangaroomaths.com/free_resources/teaching/geometry/plans_elevations.pptx)KM: [Transformation template](http://kangaroomaths.com/free_resources/teaching/geometry/transformation_template.docx)KM: [Enlargement I](http://kangaroomaths.com/free_resources/teaching/geometry/enlargement.docx)KM: [Enlargement II](http://kangaroomaths.com/free_resources/teaching/geometry/enlargement.pptx)KM: [Investigating transformations](http://kangaroomaths.com/free_resources/teaching/geometry/autograph_transformations.docx) with Autograph (enlargement and Main Event II). [Dynamic example](http://kangaroomaths.com/free_resources/teaching/geometry/enlarge.agg).WisWeb applet: [Building houses](http://www.fi.uu.nl/toepassingen/00249/toepassing_wisweb.en.html)NRICH: [Who’s the fairest of them all?](http://nrich.maths.org/5461)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Give an example of a shape and its enlargement (e.g. scale factor 2) with the guidelines drawn on. How many different ways can the scale factor be derived?
* Show me an example of a sketch where the bearing of A from B is between 90° and 180°.
* The bearing of A from B is ‘x’. Find the bearing of B from A in terms of ‘x’. Explain why this works.
* Provide the plan and elevations of shapes made from some cubes. Challenge pupils to build the shape and place it in the correct orientation.
 | Compasses, Perpendicular bisectorLocus, Loci, Arc, Plan, PerpendicularElevation, Line segment, Bisect | Describing enlargement as a ‘scaling’ will help prevent confusion when dealing with fractional scale factorsNCETM: [Departmental workshops: Enlargement](https://www.ncetm.org.uk/resources/12849)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All pupils should experience using dynamic software (e.g. Autograph) to visualise the effect of moving the centre of enlargement, and the effect of varying the scale factor.* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Give an example of a shape and its enlargement (e.g. scale factor 2) with the guidelines drawn on. How many different ways can the scale factor be derived?
* Show me an example of a sketch where the bearing of A from B is between 90° and 180°.
* The bearing of A from B is ‘x’. Find the bearing of B from A in terms of ‘x’. Explain why this works.
* Provide the plan and elevations of shapes made from some cubes. Challenge pupils to build the shape and place it in the correct orientation.
 |  | * Some pupils may think that the centre of enlargement always has to be (0,0), or that the centre of enlargement will be in the centre of the object shape.
* If the bearing of A from B is ‘x’, then some pupils may think that the bearing of B from A is ‘180 – x’.
* The north elevation is the view of a shape from the north (the north face of the shape), not the view of the shape while facing north.
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| *[Algebraic proficiency: tinkering](file:///%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Algebraic%20Proficiency%20-%20Tinkering.xlsx)* | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Algebra progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Algebra.xlsx) |
| * **use and interpret algebraic notation, including: *a*²*b* in place of *a* × *a* × *b*, coefficients written as fractions rather than as decimals (7\*, 8\*)**
* **rearrange formulae to change the subject (8\*, 9\*)**
* **simplify and manipulate algebraic expressions by expanding products of two binomials and factorising quadratic expressions of the form x² + bx + c (KS4 (9\*))**
* **argue mathematically to show algebraic expressions are equivalent, and use algebra to support and construct arguments (8\*)**
* **translate simple situations or procedures into algebraic expressions or formulae (8\*)**
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| SKILLS | Suggested resources  |
| * Know how to write products algebraically
* Use fractions when working in algebraic situations
* Identify common factors (numerical and algebraic) of terms in an expression
* Factorise an expression by taking out common factors
* Simplify an expression involving terms with combinations of variables (e.g. 3a²b + 4ab2 + 2a2 – a2b)
* Know the multiplication (division, power, zero) law of indices
* Understand that negative powers can arise
* Substitute positive and negative numbers into formulae
* Be aware of common scientific formulae
* Know the meaning of the ‘subject’ of a formula
* Change the subject of a formula when one step is required
* Change the subject of a formula when two steps are required
* Introduce changing the subject of a formula when two steps are required and factorisation is neccessary
* Multiply two linear expressions of the form (x + a)(x + b)
* Multiply two linear expressions of the form (x ± a)(x ± b)
* Expand the expression (x ± a)2
* Introduce the difference of two squares
* Introduce the expansion of 3 sets of brackets
* Factorise a quadratic expression of the form x² + bx + c
 | KM: [Missing powers](http://kangaroomaths.com/free_resources/teaching/number/investigating_powers.docx)KM: [Laws of indices](http://kangaroomaths.com/free_resources/teaching/algebra/laws_indices.pptx). Some useful questions.KM: [Maths to Infinity: Indices](http://kangaroomaths.com/free_resources/infinity/indices.xlsm)NRICH: [Temperature](http://nrich.maths.org/5608)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Know basic algebraic notation (the rules of algebra)
* Simplify an expression by collecting like terms
* Know how to multiply a single term over a bracket
* Substitute positive numbers into expressions and formulae
* Calculate with negative numbers
 | ProductVariableTermCoefficientCommon factorFactorisePowerIndicesFormula, FormulaeSubjectChange the subject**Notation**See key concepts above | During this unit pupils should experience factorising a quadratic expression such as 6x2 + 2x.Collaborate with the science department to establish a list of formulae that will be used, and ensure consistency of approach and experience.NCETM: [Algebra](https://www.ncetm.org.uk/resources/43649)NCETM: [Departmental workshop: Index Numbers](https://www.ncetm.org.uk/resources/13249)NCETM: [Departmental workshops: Deriving and Rearranging Formulae](https://www.ncetm.org.uk/resources/12930)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Once the laws of indices have been established, all teachers refer to ‘like numbers multiplied, add the indices’ and ‘like numbers divided, subtract the indices. They also generalise to am × an = am+n, etc.**When changing the subject of a formula the principle of balancing (doing the same to both sides) must be used rather than a ‘change side, change sign’ approach.* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Establish the multiplication, division and power laws of indices by writing products in full. Use the division law of indices to establish why a0 = 1.
* What is wrong with this statement and how can it be corrected: 52 × 54 = 58 ?
* Jenny thinks that if y = 2x + 1 then x = (y – 1)/2. Kenny thinks that if y = 2x + 1 then x = y/2 – 1. Who do you agree with? Why?
 |  | * Some pupils may misapply the order of operation when changing the subject of a formula
* Many pupils may think that a0 = 0
* Some pupils may not consider 4ab and 3ba as ‘like terms’ and therefore will not ‘collect’ them when simplifying expressions
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| *[Exploring fractions, decimals and percentages](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Exploring%20FDP.xlsx)* | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *3 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Fractions, decimals and percentages progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_NumberFDP.xlsx) |
| * **work interchangeably with terminating decimals and their corresponding fractions (such as 3.5 and 7/2 or 0.375 or 3/8) (8\*)**
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| SKILLS | Suggested resources  |
| * Write a decimal as a fraction
* Write a fraction as a decimal
* Write a decimal as a percentage
* Write a percentage as a decimal
* Write a fraction as a percentage
* Write a percentage as a fraction
* Identify if a fraction is terminating or recurring
* Convert a recurring decimal into a fraction
* Recall some decimal and fraction equivalents (e.g. tenths, fifths, eighths)
* Write a fraction in its lowest terms by cancelling common factors
* Identify when a fraction can be scaled to tenths or hundredths
* Convert a fraction to a decimal by scaling (when possible)
* Use a calculator to change any fraction to a decimal and all the other conversions
 | KM: [FDP conversion](http://kangaroomaths.com/free_resources/teaching/number/fdp_conversion.docx). Templates for taking notes.KM: [Fraction sort](http://kangaroomaths.com/free_resources/teaching/number/fraction_sort.docx). Tasks one and two only.KM: [Maths to Infinity: Fractions, decimals, percentages, ratio, proportion](http://kangaroomaths.com/free_resources/infinity/fdprp.xlsm)NRICH: [Matching fractions, decimals and percentages](http://nrich.maths.org/1249)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Understand that fractions, decimals and percentages are different ways of representing the same proportion
* Convert between mixed numbers and top-heavy fractions
* Write one quantity as a fraction of another
 | FractionMixed numberTop-heavy fractionPercentageDecimalProportionTerminatingRecurringSimplify, Cancel**Notation**Diagonal and horizontal fraction bar | The diagonal fraction bar (solidus) was first used by Thomas Twining (1718) when recorded quantities of tea. The division symbol (÷) is called an obelus, but there is no name for a horizontal fraction bar.NRICH: [History of fractions](http://nrich.maths.org/2515)NRICH: [Teaching fractions with understanding](http://nrich.maths.org/2550)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All pupils should use the horizontal fraction bar to avoid confusion when fractions are coefficients in algebraic situations* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Without using a calculator, convince me that 3/8 = 0.375
* Show me a fraction / decimal / percentage equivalent. And another. And another …
* What is the same and what is different: 2.5, 25%, 0.025 ?
 |  | * Some pupils may make incorrect links between fractions and decimals such as thinking that 1/5 = 0.15
* Some pupils may think that 5% = 0.5, 4% = 0.4, etc.
* Some pupils may think it is not possible to have a percentage greater than 100%.
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| *[Proportional reasoning](file:///%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Proportional%20Reasoning.xlsx)* | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Ratio and Proportion progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_RatioProportion.xlsx) |
| * **express the division of a quantity into two parts as a ratio; apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) (7\*, 8\*,9\*)**
* **understand and use proportion as equality of ratios (8\*)**
* **express a multiplicative relationship between two quantities as a ratio or a fraction (8\*)**
* **relate ratios to fractions and to linear functions (8\*)**
* **use compound units (such as speed, rates of pay, unit pricing and density (8\*, 9\*)**
* **solve problems involving direct and inverse proportion, including graphical and algebraic representations (8\*)**
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| SKILLS | Suggested resources  |
| * Identify ratio in a real-life context
* Write a ratio to describe a situation
* Identify proportion in a situation
* Find a relevant multiplier in a situation involving proportion
* Use fractions fluently in situations involving ratio or proportion
* Understand the connections between ratios and fractions
* Understand the meaning of a compound unit
* Know the connection between speed, distance and time
* Solve problems involving speed
* Identify when it is necessary to convert quantities in order to use a sensible unit of measure
* Know the difference between direct and inverse proportion
* Recognise direct (inverse) proportion in a situation
* Know the features of a graph that represents a direct (inverse) proportion situation
* Know the features of an expression (or formula) that represents a direct (inverse) proportion situation
* Understand why speed, density and pressure are known as compound units
* Know the definition of density (pressure, population density, speed)
* Solve problems involving density (pressure, speed)
* Convert between units of density
 | KM: [Proportion for real](http://kangaroomaths.com/free_resources/teaching/number/proportion_for_real.docx)KM: [Investigating proportionality](http://kangaroomaths.com/free_resources/teaching/number/investigating_proportionality.docx)KM: [Maths to Infinity: Fractions, decimals, percentages, ratio, proportion](http://kangaroomaths.com/free_resources/infinity/fdprp.xlsm)NRICH: [In proportion](http://nrich.maths.org/9136)Standards Unit: [N6 Developing proportional reasoning](http://www.nationalstemcentre.org.uk/elibrary/resource/1963/developing-proportional-reasoning-n6)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Understand and use ratio notation
* Divide an amount in a given ratio
 | RatioProportionProportionalMultiplierSpeedUnitary methodUnitsCompound unit**Notation**Kilometres per hour is written as km/h or kmh-1Metres per second is written as m/s or ms-1 | NRICH: [Ratio or proportion?](http://nrich.maths.org/4825)NRICH: [Roasting old chestnuts 3](http://nrich.maths.org/1372)NCETM: [The Bar Model](https://www.ncetm.org.uk/resources/44568)NCETM: [Multiplicative reasoning](https://www.ncetm.org.uk/resources/43669)NCETM: [Departmental workshops: Proportional Reasoning](https://www.ncetm.org.uk/resources/10334)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All pupils are taught to set up a ‘proportion table’ and use it to find the multiplier in situations involving proportion* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me an example of two quantities that will be in proportion. And another. And another …
* (Showing a table of values such as the one below) convince me that this information shows a proportional relationship

|  |  |
| --- | --- |
| 6 | 9 |
| 10 | 15 |
| 14 | 21 |

* Which is the faster speed: 60 km/h or 10 m/s? Explain why.
 |  | * Many pupils will want to identify an additive relationship between two quantities that are in proportion and apply this to other quantities in order to find missing amounts
* Some pupils may think that a multiplier always has to be greater than 1
* When converting between times and units, some pupils may base their working on 100 minutes = 1 hour
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| *[Pattern sniffing](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Pattern%20Sniffing.xlsx)* | [Stage 9\*](file:///%5C%5Csweep%5Cteacher%24%5Cmaths%5CTeaching%20Plans%20%28Linked%29%5C2017%2018%20Teaching%20Plans%20and%20SOW%5CSchemes%20Of%20Work%5CKS3%20Stages%5CSt9%20Star_sow.docx) | *3 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Algebra progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Algebra.xlsx) |
| * **generate terms of a sequence from either a term-to-term or a position-to-term rule (7\*,8\*)**
* **deduce expressions to calculate the nth term of linear sequences (7\*, 8\*)**
* **recognise and use Fibonacci type sequences (8\*)**
* **recognise and use quadratic sequences (KS4, 9\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Generate a sequence from a term-to-term rule
* Understand the meaning of a position-to-term rule
* Use a position-to-term rule to generate a sequence
* Find the position-to-term rule for a given sequence
* Use algebra to describe the position-to-term rule of a linear sequence (the nth term)
* Use the nth term of a sequence to deduce if a given number is in a sequence
* Generate a sequence using a spreadsheet
* Generate terms of a quadratic sequence
* Identify quadratic sequences
* Establish the first and second differences of a quadratic sequence
* Find the next three terms in any quadratic sequence
* Find the term in x2 for a quadratic sequence
 | KM: [Spreadsheet sequences](http://kangaroomaths.com/free_resources/teaching/algebra/spreadsheet_sequences.docx)KM: [Generating sequences](http://kangaroomaths.com/free_resources/teaching/algebra/no_it_room.docx)KM: [Maths to Infinity: Sequences](http://kangaroomaths.com/free_resources/infinity/sequences.xlsm)KM: [Stick on the Maths: Linear sequences](http://kangaroomaths.com/free_resources/teaching/sotm/level6/6alg3_ewb.doc)NRICH: [Charlie’s delightful machine](http://nrich.maths.org/7024)NRICH: [A little light thinking](http://nrich.maths.org/7016)NRICH: [Go forth and generalise](http://nrich.maths.org/2338)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Use a term-to-term rule to generate a sequence
* Find the term-to-term rule for a sequence
* Describe a sequence using the term-to-term rule
 | SequenceLinearTermDifferenceTerm-to-term rulePosition-to-term ruleAscendingDescending**Notation**T(n) is often used when finding the nth term of sequence  | Using the nth term for times tables is a powerful way of finding the nth term for any linear sequence. For example, if the pupils understand the 3 times table can ne described as ‘3n’ then the linear sequence 4, 7, 10, 13, … can be described as the 3 times table ‘shifted up’ one place, hence 3n + 1.Exploring statements such as ‘is 171 is in the sequence 3, 9, 15, 21, 27, ..?’ is a very powerful way for pupils to realise that ‘term-to-term’ rules can be inefficient and therefore ‘position-to-term’ rules (nth term) are needed.NCETM: [Algebra](https://www.ncetm.org.uk/resources/43649)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Teachers refer to a sequence such as 2, 5, 8, 11, … as ‘the three times table minus one’, to help pupils construct their understanding of the nth term of a sequence.**All students have the opportunity to use spreadsheets to generate sequences* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me a sequence that could be generated using the nth term 4n $\pm $ c. And another. And another …
* What’s the same, what’s different: 4, 7, 10, 13, 16, …. , 2, 5, 8, 11, 14, … , 4, 9, 14, 19, 24, …. and 4, 10, 16, 22, 28, …?
* The 4th term of a linear sequence is 15. Show me the nth term of a sequence with this property. And another. And another …
* Convince me that the nth term of the sequence 2, 5, 8, 11, … is 3n -1 .
* Kenny says the 171 is in the sequence 3, 9, 15, 21, 27, … Do you agree with Kenny? Explain your reasoning.
 |  | * Some pupils will think that the nth term of the sequence 2, 5, 8, 11, … is n + 3.
* Some pupils may think that the (2n)th term is double the nth term of a linear sequence.
* Some pupils may think that sequences with nth term of the form ‘ax ± b’ must start with ‘a’.
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| *[Investigating angles](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Investigating%20Angles.xlsx)* | [Stage 9\*](file:///%5C%5Csweep%5Cteacher%24%5Cmaths%5CTeaching%20Plans%20%28Linked%29%5C2017%2018%20Teaching%20Plans%20and%20SOW%5CSchemes%20Of%20Work%5CKS3%20Stages%5CSt9%20Star_sow.docx) | *6 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Position and direction progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_GeometryPositionDirection.xlsx) |
| * **derive and use the sum of angles in a triangle (e.g. to deduce and use the angle sum in any polygon, and to derive properties of regular polygons) (8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Identify alternate angles and know that they are equal
* Identify corresponding angles and know that they are equal
* Use knowledge of alternate and corresponding angles to calculate missing angles in geometrical diagrams
* Establish the fact that angles in a triangle must total 180°
* Use the fact that angles in a triangle total 180° to work out the total of the angles in any polygon
* Establish the size of an interior angle in a regular polygon
* Know the total of the exterior angles in any polygon
* Establish the size of an exterior angle in a regular polygon
* Know the criteria for triangles to be congruent (SSS, SAS, ASA, RHS)
* Identify congruent triangles
 | KM: [Alternate and corresponding angles](http://kangaroomaths.com/free_resources/teaching/geometry/alternate_corresponding_angles.pptx)KM: [Perplexing parallels](http://kangaroomaths.com/free_resources/teaching/geometry/perplexing_parallels.docx)KM: [Investigating polygons](http://kangaroomaths.com/free_resources/teaching/geometry/investigating_polygons.docx)KM: [Maths to Infinity: Lines and angles](http://kangaroomaths.com/free_resources/infinity/angles_lines.xlsm)KM: [Stick on the Maths: Alternate and corresponding angles](http://kangaroomaths.com/free_resources/teaching/sotm/level6/6ssm3_ewb.doc)KM: [Stick on the Maths: Geometrical problems](http://kangaroomaths.com/free_resources/teaching/sotm/level6/6ssm2_ewb.doc)NRICH: [Ratty](http://nrich.maths.org/712)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Use angles at a point, angles at a point on a line and vertically opposite angles to calculate missing angles in geometrical diagrams
* Know that the angles in a triangle total 180°
 | DegreesRight angle, acute angle, obtuse angle, reflex angleVertically oppositeGeometry, geometricalParallelAlternate angles, corresponding anglesInterior angle, exterior angleRegular polygon**Notation**Dash notation to represent equal lengths in shapes and geometric diagramsArrow notation to show parallel lines | The KM: [Perplexing parallels](http://kangaroomaths.com/free_resources/teaching/geometry/perplexing_parallels.docx) resource is a great way for pupils to discover practically the facts for alternate and corresponding angles.Pupils have established the fact that angles in a triangle total 180° in Stage 7. However, using alternate angles they are now able to prove this fact.Encourage pupils to draw regular and irregular convex polygons to discover the sum of the interior angles = (n – 2) × 180°.NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Teachers insist on correct mathematical language (and not F-angles or Z-angles for example)* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me a pair of alternate (corresponding) angles. And another. And another …
* Jenny thinks that hexagons are the only polygon that tessellates. Do you agree? Explain your reasoning.
* Convince me that the angles in a triangle total 180°.
* Convince me that the interior angle of a pentagon is 540°.
* Always/ Sometimes/ Never: The sum of the interior angles of an n-sided polygon can be calculated using sum = (n – 2) × 180°.
* Always/ Sometimes/ Never: The sum of the exterior angles of a polygon is 360°.
 |  | * Some pupils may think that alternate and/or corresponding angles have a total of 180° rather than being equal.
* Some pupils may think that the sum of the interior angles of an n-sided polygon can be calculated using Sum = n × 180°.
* Some pupils may think that the sum of the exterior angles increases as the number of sides of the polygon increases.
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| *[Calculating fractions, decimals and percentages](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Calculating%20Fractions%2C%20Decimals%20and%20Percentages.xlsx)* | [Stage 9\*](file:///%5C%5Csweep%5Cteacher%24%5Cmaths%5CTeaching%20Plans%20%28Linked%29%5C2017%2018%20Teaching%20Plans%20and%20SOW%5CSchemes%20Of%20Work%5CKS3%20Stages%5CSt9%20Star_sow.docx) | *6 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Fractions, decimals and percentages progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_NumberFDP.xlsx) |
| * **interpret fractions and percentages as operators (8\*)**
* **solve problems involving percentage change, percentage increase and decrease, including original value problems, and simple interest including in financial mathematics (7\*, 8\*)**
* **express one quantity as a fraction of another where the fraction is less than 1 and greater than 1 (8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Recognise when a fraction (percentage) should be interpreted as a number
* Recognise when a fraction (percentage) should be interpreted as a operator
* Identify the multiplier for a percentage increase or decrease when the percentage is greater than 100%
* Use calculators to increase an amount by a percentage greater than 100%
* Solve problems involving percentage change
* Solve original value problems when working with percentages
* Solve financial problems including simple interest
* Understand the meaning of giving an exact solution
* Solve problems that require exact calculation with fractions
 | KM: [Stick on the Maths: Proportional reasoning](http://kangaroomaths.com/free_resources/teaching/sotm/level6/6calc3_ewb.doc)KM: [Stick on the Maths: Multiplicative methods](http://kangaroomaths.com/free_resources/teaching/sotm/level7/7calc1_ewb.doc)KM: [Percentage identifying](http://kangaroomaths.com/free_resources/teaching/number/percentage_identifying.xlsx)NRICH: [One or both](http://nrich.maths.org/794)NRICH: [Antiques roadshow](http://nrich.maths.org/5704)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Apply the four operations to proper fractions, improper fractions and mixed numbers
* Use calculators to find a percentage of an amount using multiplicative methods
* Identify the multiplier for a percentage increase or decrease
* Use calculators to increase (decrease) an amount by a percentage using multiplicative methods
* Know that percentage change = actual change ÷ original amount
 | Proper fraction, improper fraction, mixed numberSimplify, cancel, lowest termsPercent, percentagePercentage changeOriginal amountMultiplier(Simple) interestExact**Notation**Mixed number notationHorizontal / diagonal bar for fractions | The bar model is a powerful strategy for pupils to ‘re-present’ a problem involving percentage change.Only simple interest should be explored in this unit. Compound interest will be developed later.NCETM: [The Bar Model](https://www.ncetm.org.uk/resources/44568)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***When adding and subtracting mixed numbers pupils are taught to convert to improper fractions as a general strategy**Teachers use the horizontal fraction bar notation at all times* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Agreed common teaching approahes |
| * Convince me that the multiplier for a 150% increase is 2.5
* Kenny buys a poncho in a 25% sale. The sale price is £40. Kenny thinks that the original is £50. Do you agree with Kenny? Explain your answer.
* Jenny thinks that increasing an amount by 200% is the same as multiplying by 3. Do you agree with Jenny? Explain your answer.
 |  | * Some pupils may think that the multiplier for a 150% increase is 1.5
* Some pupils may think that increasing an amount by 200% is the same as doubling.
* In isolation, pupils may be able to solve original value problems confidently. However, when it is necessary to identify the type of percentage problem, many pupils will apply a method for a more simple percentage increase / decrease problem. If pupils use models (e.g. the bar model, or proportion tables) to represent all problems then they are less likely to make errors in identifying the type of problem.
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| *[Solving equations](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Solving%20Equations%20and%20Inequalities.xlsx)*  | [Stage 9\*](file:///%5C%5Csweep%5Cteacher%24%5Cmaths%5CTeaching%20Plans%20%28Linked%29%5C2017%2018%20Teaching%20Plans%20and%20SOW%5CSchemes%20Of%20Work%5CKS3%20Stages%5CSt9%20Star_sow.docx) | *3 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Algebra progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Algebra.xlsx) |
| * **solve linear equations with the unknown on both sides of the equation (7\*, 8\*)**
* **find approximate solutions to linear equations using a graph (8\*)**
* **find approximate solutions to simultaneous equations using a graph (8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Identify the correct order of undoing the operations in an equation
* Solve linear equations with the unknown on one side when the solution is a negative number
* Solve linear equations with the unknown on both sides when the solution is a whole number
* Solve linear equations with the unknown on both sides when the solution is a fraction
* Solve linear equations with the unknown on both sides when the solution is a negative number
* Solve linear equations with the unknown on both sides when the equation involves brackets
* Recognise that the point of intersection of two graphs corresponds to the solution of a connected equation
* Check the solution to an equation by substitution
* Understand the concept of simultaneous equations
* Find approximate solutions to simultaneous equations using a graph
* Understand the concept of solving simultaneous equations by elimination\*
* Solve two linear simultaneous equations in two variables in very simple cases (no multiplication required)
* Solve two linear simultaneous equations in two variables in simple cases (multiplication of one equation only required)
* Derive and solve two simultaneous equations
 | KM: [Solving equations](http://kangaroomaths.com/free_resources/teaching/algebra/solving_equations.docx)KM: [Stick on the Maths: Constructing and solving equations](http://kangaroomaths.com/free_resources/teaching/sotm/level6/6alg2_ewb.doc)NRICH: [Think of Two Numbers](http://nrich.maths.org/public/viewer.php?obj_id=1170)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Choose the required inverse operation when solving an equation
* Solve linear equations by balancing when the solution is a whole number or a fraction
 | Algebra, algebraic, algebraicallyUnknown EquationOperationSolveSolutionBracketsSymbolSubstituteGraphPoint of intersection **Notation**The lower case and upper case of a letter should not be used interchangeably when worked with algebraJuxtaposition is used in place of ‘×’. 2a is used rather than a2.Division is written as a fraction | This unit builds on the wok solving linear equations with unknowns on one side in Stage 7. It is essential that pupils are secure with solving these equations before moving onto unknowns on both sides.Encourage pupils to ‘re-present’ the problem using the Bar Model.NCETM: [The Bar Model](https://www.ncetm.org.uk/resources/44568)

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| --- | --- | --- | --- | --- |
| x | x | x | x | 8 |
| x | 14 |

|  |  |  |  |
| --- | --- | --- | --- |
| x | x | x | 8 |
| 14 |

|  |  |  |
| --- | --- | --- |
| x | x | x |
| 6 |

|  |
| --- |
| x |
| 2 |

NCETM: [Algebra](https://www.ncetm.org.uk/resources/43649)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All pupils should solve equations by balancing:*

|  |  |  |
| --- | --- | --- |
| *4x + 8*  | *=* | *14 + x*  |
| *- x* |  | *- x* |
| *3x + 8* | *=* | *14* |
| *- 8* |  | *- 8* |
| *3x* | *=* | *6* |
| *÷ 3* |  | *÷ 3* |
| *x* | *=* | *2* |

 |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me an (one-step, two-step) equation with a solution of -8 (negative, fractional solution). And another. And another …
* Show me a two-step equation that is ‘easy’ to solve. And another. And another …
* What’s the same, what’s different: 2x + 7 = 25, 3x + 7 = x + 25, x + 7 = 7 – x, 4x + 14 = 50 ?
* Convince me how you could use graphs to find solutions, or estimates, for equations.
 |  | * Some pupils may think that you always have to manipulate the equation to have the unknowns on the LHS of the equal sign, for example 2x – 3 = 6x + 6
* Some pupils think if 4x = 2 then x = 2.
* When solving equations of the form 2x – 8 = 4 – x, some pupils may subtract ‘x’ from both sides.
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| *[Calculating space](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5C2015%2016%20Area%5C%5CSchemes%20of%20Work%5C%5CMaths%20Links%20Topics%5C%5CStage%208%20Calculating%20Space.xlsx)* | [Stage 9\*](file:///%5C%5Csweep%5Cteacher%24%5Cmaths%5CTeaching%20Plans%20%28Linked%29%5C2017%2018%20Teaching%20Plans%20and%20SOW%5CSchemes%20Of%20Work%5CKS3%20Stages%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Measurement and mensuration progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_GeometryMeasurementMensuration.xlsx) |
| * **compare lengths, areas and volumes using ratio notation (8\*)**
* **calculate perimeters of 2D shapes, including circles (8\*)**
* **know the formulae: circumference of a circle = 2πr = πd, area of a circle = πr² (8\*)**
* **calculate areas of circles and composite shapes (8\*)**
* **know the formulae for: Pythagoras’ theorem, a² + b² = c², and apply it to find lengths in right-angled triangles in two dimensional figures (8\*, 9\*)**
* **apply angle facts, triangle congruence, similarity and properties of quadrilaterals to derive results about angles and sides, including Pythagoras’ Theorem, and use known results to obtain simple proofs (8\*,9\*)**
* **know and apply formulae to calculate volume of right prisms (including cylinders) (8\*)**
* **calculate exactly with multiples of pi (KS4)**
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| SKILLS |  | Suggested resources  |
| * Know the vocabulary of circles
* Know that the number π (pi) = 3.1415926535…
* Recall π to two decimal places
* Know the formula circumference of a circle = 2πr = πd
* Calculate the circumference of a circle when radius (diameter) is given
* Calculate the radius (diameter) of a circle when the circumference is known
* Calculate the perimeter of composite shapes that include sections of a circle
* Know the formula area of a circle = πr²
* Calculate the area of a circle when radius (diameter) is given
* Calculate the radius (diameter) of a circle when the area is known
* Calculate the area of composite shapes that include sections of a circle
 | * Know the formula for finding the volume of a right prism (cylinder)
* Calculate the volume of a right prism (cylinder)
* Know the vocabulary of circles
* Know how to find arc length
* Calculate the arc length of a sector when radius is given
* Know how to find the area of a sector
* Calculate the area of a sector when radius is given
* Calculate the angle of a sector when the arc length and radius are known
* Know how to find the surface area of a right prism (cylinder)
* Calculate the surface area of a right prism (cylinder)
 | KM: [Circle connections](http://kangaroomaths.com/free_resources/teaching/geometry/circle_connections.docx)KM: [Circle problems](http://kangaroomaths.com/free_resources/teaching/geometry/circle_problems.docx)KM: [Maths to Infinity: Area and Volume](http://www.kangaroomaths.com/free_resources/infinity/area_volume.xlsm)KM: [Stick on the Maths: Circumference and area of a circle](http://www.kangaroomaths.com/free_resources/teaching/sotm/level6/6ssm10_ewb.doc)KM: [Stick on the Maths: Right prisms](http://www.kangaroomaths.com/free_resources/teaching/sotm/level7/7ssm2_ewb.doc)NRICH: [Blue and White](http://nrich.maths.org/809)NRICH: [Efficient Cutting](http://nrich.maths.org/public/viewer.php?obj_id=2664&refpage=titlesearch.php) NRICH: [Cola Can](http://nrich.maths.org/public/viewer.php?obj_id=5888)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Know how to use formulae to find the area of rectangles, parallelograms, triangles and trapezia
* Know how to find the area of compound shapes
 | CircleCentreRadius, diameter, chord, circumferencePi(Right) prismCross-sectionCylinderPolygon, polygonalSolid**Notation**πAbbreviations of units in the metric system: km, m, cm, mm, mm2, cm2, m2, km2, mm3, cm3, km3 | C = πd can be established by investigating the ratio of the circumference to the diameter of circular objects (wheel, clock, tins, glue sticks, etc.) Pupils need to understand this formula in order to derive A = πr².A prism is a solid with constant polygonal cross-section. A right prism is a prism with a cross-section that is perpendicular to the ‘length’.NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***The area of a circle is derived by cutting a circle into many identical sectors and approximating a parallelogram**Every classroom has a set of* [*area posters*](http://kangaroomaths.com/free_resources/display/areas.pdf) *on the wall* *The formula for the volume of a prism is ‘area of cross-section × length’ even if the orientation of the solid suggests that height is required**Pupils use area of a trapezium =* $\frac{\left(a+b\right)h}{2}$ *and area of a triangle = area =* $\frac{bh}{2}$ |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Convince me C = 2πr = πd.
* What is wrong with this statement? How can you correct it?

The area of a circle with radius 7 cm is approximately 441 cm2 because (3 × 7)2 = 441.* Convince me the area of a semi-circle = $\frac{πd^{2}}{4}$
* Name a right prism. And another. And another …
* Convince me that a cylinder is not a prism
 |  | * Some pupils will work out (π × radius)2 when finding the area of a circle
* Some pupils may use the sloping height when finding cross-sectional areas that are parallelograms, triangles or trapezia
* Some pupils may think that the area of a triangle = base × height
* Some pupils may think that you multiply all the numbers to find the volume of a prism
* Some pupils may confuse the concepts of surface area and volume
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| Algebraic proficiency: visualising | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *9 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Algebra progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Algebra.xlsx) |
| * **identify and interpret gradients and intercepts of linear functions graphically and algebraically (8\*, 9\*)**
* **recognise, sketch and interpret graphs of linear functions and simple quadratic functions (8\*, 9\*)**
* **interpret graphs and graphs of non-standard (*piece-wise linear)* functions in real contexts, to find approximate solutions to problems such as simple kinematic problems involving distance and speed (KS4 (9\*))**
* **use the form *y = mx + c* to identify parallel lines (KS4)**
* **interpret the gradient of a straight line graph as a rate of change (8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS |  | Suggested resources  |
| * Know that graphs of functions of the form y = mx + c, x ± y = c and ax ± by = c are linear
* Plot graphs of functions of the form y = mx + c (x ± y = c, ax ± by = c)
* Understand the concept of the gradient of a straight line
* Find the gradient of a straight line on a unit grid
* Find the y-intercept of a straight line
* Sketch a linear graph
* Distinguish between a linear and quadratic graph
* Plot graphs of quadratic functions of the form y = x2 ± c
* Sketch a simple quadratic graphPlot and interpret linear graphs
* Plot and quadratic graphs
* Model real situations using linear graphs
 | * Plot and interpret graphs of piece-wise linear functions in real contexts
* Plot and interpret distance-time graphs (speed-time graphs)
* Find approximate solutions to kinematic problems involving distance and speed
* Use the form y = mx + cto identify parallel lines
* Rearrange an equation into the form y = mx + c
* Find the equation of a line through one point with a given gradient
* Find the equation of a line through two given points
* Interpret the gradient of a straight line graph as a rate of change
 | KM: [Matching graphs](http://kangaroomaths.com/free_resources/teaching/algebra/matching_graphs.docx)KM: [Autograph 1](http://kangaroomaths.com/free_resources/teaching/algebra/autograph1.docx)KM: [Autograph 2](http://kangaroomaths.com/free_resources/teaching/algebra/autograph2.docx)KM: [The hare and the tortoise](http://kangaroomaths.com/free_resources/teaching/algebra/hare_tortoise.docx)**Learning review**KM: [8M11 BAM Task](http://kangaroomaths.com/free_resources/assessment/BAM/8M11_BAM.pdf) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Use coordinates in all four quadrants
* Write the equation of a line parallel to the x-axis or the y-axis
* Draw a line parallel to the x-axis or the y-axis given its equation
* Identify the lines y = x and y = -x
* Draw the lines y = x and y = -x
* Substitute positive and negative numbers into formulae
 | PlotEquation (of a graph)FunctionFormulaLinearCoordinate planeGradienty-interceptSubstituteQuadraticPiece-wise linearModelKinematic, Speed, Distance**Notation***y* = *mx* + *c* | When plotting graphs of functions of the form y = mx + c a table of values can be useful. Note that negative number inputs can cause difficulties. Pupils should be aware that the values they have found for linear functions should correspond to a straight line.NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Pupils are taught to use positive numbers wherever possible to reduce potential difficulties with substitution of negative numbers**Students plot points with a ‘x’ and not ‘‘**Students draw graphs in pencil**All pupils use dynamic geometry software to explore graphs of functions* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Draw a distance-time graph of your journey to school. Explain the key features.
* Show me a point on this line (e.g. y = 2x + 1). And another, and another …
* (Given an appropriate distance-time graph) convince me that Kenny is stationary between 10: 00 a.m. and 10:45 a.m.
 |  | * When plotting linear graphs some pupils may draw a line segment that stops at the two most extreme points plotted
* Some pupils may think that a sketch is a very rough drawing. It should still identify key features, and look neat, but will not be drawn to scale
* Some pupils may think that a positive gradient on a distance-time graph corresponds to a section of the journey that is uphill
* Some pupils may think that the graph y = x2 + c is the graph of y = x2 translated horizontally.
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| Understanding risk II | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *6 hours* |
| **KNOWLEDGE*** **enumerate sets and combinations of sets systematically, using tree diagrams (KS4 (9\*))**
 | **The Big Picture**: [Probability progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Probability.xlsx) |
| * **apply systematic listing strategies (8\*)**
* **record describe and analyse the frequency of outcomes of probability experiments using frequency trees (7\*,8\*)**
* **enumerate sets and combinations of sets systematically, using tables, grids and Venn diagrams (8\*,9\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * List outcomes of combined events using a tree diagram
* Label a tree diagram with probabilities
* Label a tree diagram with probabilities when events are dependent
* Use a tree diagram to calculate probabilities of independent combined events
* Use a tree diagram to calculate probabilities of dependent combined events
* List all elements in a combination of sets using a Venn diagram
* List outcomes of an event systematically
* Use a table to list all outcomes of an event
 | * List outcomes of an event using a grid (two-way table)
* Use frequency trees to record outcomes of probability experiments
* Make conclusions about probabilities based on frequency trees
* Construct theoretical possibility spaces for combined experiments with equally likely outcomes
* Calculate probabilities using a possibility space
* Use theoretical probability to calculate expected outcomes
* Use experimental probability to calculate expected outcomes
 | KM: [Sample spaces](http://kangaroomaths.com/free_resources/teaching/statistics/sample_spaces.docx)KM: [Race game](http://kangaroomaths.com/free_resources/teaching/statistics/race_game.docx)**Learning review=**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Convert between fractions, decimals and percentages
* Understand the use of the 0-1 scale to measure probability
* Work out theoretical probabilities for events with equally likely outcomes
* Know how to represent a probability
* Know that the sum of probabilities for all outcomes is 1
 | OutcomeEventExperiment, Combined experimentFrequency treeEnumerateSetVenn diagramPossibility space, sample spaceEqually likely outcomesTheoretical probabilityRandomBias, FairnessRelative frequency**Notation**P(A) for the probability of event AProbabilities are expressed as fractions, decimals or percentage. They should not be expressed as ratios (which represent odds) or as words | The Venn diagram was invented by John Venn (1834 – 1923)NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All students are taught to use ‘DIME’ probability recording charts**All classes carry out the ‘race game’ as a simulated horse race with horses numbered 1 to 12* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me a way of listing all outcomes when two coins are flipped
* Convince me that there are more than 12 outcomes when two six-sided dice are rolled
* Convince me that 7 is the most likely total when two dice are rolled
 |  | * Some students may think that there are only three outcomes when two coins are flipped, or that there are only six outcomes when three coins are flipped
* Some students may think that there are 12 unique outcomes when two dice are rolled
* Some students may think that there are 12 possible totals when two dice are rolled
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| Presentation of data | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *6 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Statistics progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Statistics.xlsx) |
| * **interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate graphical representation involving discrete, continuous and grouped data (8\*)**
* **use and interpret scatter graphs of bivariate data (8\*)**
* **recognise correlation (8\*)**
* **draw estimated lines of best fit; make predictions (8\*)**
* **know correlation does not indicate causation; interpolate and extrapolate apparent trends whilst knowing the dangers of so doing (8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Know the meaning of continuous data
* Interpret a grouped frequency table for continuous data
* Construct a grouped frequency table for continuous data
* Construct histograms for grouped data with equal class intervals
* Interpret histograms for grouped data with equal class intervals
* Construct and use the horizontal axis of a histogram correctly
* Plot a scatter diagram of bivariate data
* Understand the meaning of ‘correlation’
* Interpret a scatter diagram using understanding of correlation
* Understand that correlation does not indicate causation
* Interpret a scatter diagram using understanding of correlation
* Construct a line of best fit on a scatter diagram
* Use a line of best fit to estimate values
* Know when it is appropriate to use a line of best fit to estimate values
 | KM: Make a ‘human’ scatter graph by asking pupils to stand at different points on a giant set of axes.KM: [Gathering data](http://kangaroomaths.com/free_resources/teaching/statistics/gathering_data.docx)KM: [Spreadsheet statistics](http://kangaroomaths.com/free_resources/teaching/statistics/spreadsheet_statistics.docx)KM: [Stick on the Maths HD2: Selecting and constructing graphs and charts](http://www.kangaroomaths.com/free_resources/teaching/sotm/level6/6hd2_ewb.doc)KM: [Stick on the Maths HD3: Working with grouped data](http://www.kangaroomaths.com/free_resources/teaching/sotm/level7/7hd3_ewb.doc)**Learning review*** [www.diagnosticquestions.com](http://www.diagnosticquestions.com)
 |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Know the meaning of discrete data
* Interpret and construct frequency tables
* Construct and interpret pictograms, bar charts, pie charts, tables and vertical line charts
 | DataCategorical data, Discrete dataContinuous data, Grouped dataTable, Frequency tableFrequencyHistogramScale, GraphAxis, axesScatter graph (scatter diagram, scattergram, scatter plot)Bivariate data(Linear) CorrelationPositive correlation, Negative correlation**Notation**Correct use of inequality symbols when labeling groups in a frequency table | The word histogram is often misused and an internet search of the word will usually reveal a majority of non-histograms. The correct definition is ‘a diagram made of rectangles whose areas are proportional to the frequency of the group’. If the class widths are equal, as they are in this unit of work, then the vertical axis shows the frequency. It is only later that pupils need to be introduced to unequal class widths and frequency density.Lines of best fit on scatter diagrams are not introduced until Stage 9, although pupils may well have encountered both lines and curves of best fit in science by this time.NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***All students collect data about their class’s height and armspan when first constructing a scatter diagram* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me a scatter graph with positive (negative, no) correlation. And another. And another.
* Show me a histogram. And another. And another.
* Kenny thinks that histogram is just a ‘fancy’ name for a bar chart. Do you agree with Kenny? Explain your answer.
* What’s the same and what’s different: histogram, scatter diagram, bar chart, pie chart?
* Always/Sometimes/Never: A scatter graph
 |  | * Some pupils may label the bar of a histogram rather than the boundaries of the bars
* Some pupils may leave gaps between the bars in a histogram
* Some pupils may misuse the inequality symbols when working with a grouped frequency table
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| Measuring data | [Stage 9\*](%5C%5C%5C%5Csweep%5C%5Cteacher%24%5C%5Cmaths%5C%5CTeaching%20Plans%20%28Linked%29%5C%5C2017%2018%20Teaching%20Plans%20and%20SOW%5C%5CSchemes%20Of%20Work%5C%5CKS3%20Stages%5C%5CSt9%20Star_sow.docx) | *6 hours* |
| **KNOWLEDGE** | **The Big Picture**: [Statistics progression map](http://kangaroomaths.com/free_resources/planning/KM_MathematicsProgression_Statistics.xlsx) |
| * **interpret, analyse and compare the distributions of data sets from univariate empirical distributions through appropriate measures of central tendency (median, mean, mode and modal class) and spread (range, including consideration of outliers) (7\*, 8\*)**
 |
| [Return to overview](#Overview) |
| SKILLS | Suggested resources  |
| * Find the modal class of set of grouped data
* Find the class containing the median of a set of data
* Find the midpoint of a class
* Calculate an estimate of the mean from a grouped frequency table
* Estimate the range from a grouped frequency table
* Analyse and compare sets of data
* Appreciate the limitations of different statistics (mean, median, mode, range)
* Choose appropriate statistics to describe a set of data
* Justify choice of statistics to describe a set of data
* Investigate averages
 | KM: [Swillions](http://kangaroomaths.com/free_resources/teaching/statistics/swillions.pdf)KM: [Lottery project](http://kangaroomaths.com/free_resources/teaching/statistics/lottery%20project.docx)NRICH: [Half a Minute](http://nrich.maths.org/10999)**Learning review**[www.diagnosticquestions.com](http://www.diagnosticquestions.com) |
| Prerequisites | Mathematical language | Agreed common teaching approahes |
| * Understand the mean, mode and median as measures of typicality (or location)
* Find the mean, median, mode and range of a set of data
* Find the mean, median, mode and range from a frequency table
 | AverageSpreadConsistencyMeanMedianModeRangeStatisticStatisticsApproximate, RoundCalculate an estimateGrouped frequencyMidpoint**Notation**Correct use of inequality symbols when labeling groups in a frequency table | The word ‘average’ is often used synonymously with the mean, but it is only one type of average. In fact, there are several different types of mean (the one in this unit properly being named as the ‘arithmetic mean’). NCETM: [Glossary](https://www.ncetm.org.uk/public/files/17308038/National%2BCurriculum%2BGlossary.pdf)**Common approaches***Every classroom has a set of* [*statistics posters*](http://kangaroomaths.com/free_resources/display/statistics.pdf) *on the wall**All students are taught to use mathematical presentation correctly when calculating and rounding solutions, e.g. (21 + 56 + 35 + 12) ÷ 30 = 124 ÷ 30 = 41.3 to 1 d.p.* |
| Reasoning opportunities and probing questions | Cross Curricular Links | Possible misconceptions |
| * Show me an example of an outlier. And another. And another.
* Convince me why the mean from a grouped set of data is only an estimate.
* What’s the same and what’s different: mean, modal class, median, range?
* Always/Sometimes/Never: A set of grouped data will have one modal class
* Convince me how to estimate the range for grouped data.
 |  | * Some pupils may incorrectly estimate the mean by dividing the total by the numbers of groups rather than the total frequency.
* Some pupils may incorrectly think that there can only be one model class.
* Some pupils may incorrectly estimate the range of grouped data by subtracting the upper bound of the first group from the lower bound of the last group.
 |