



Devonshire Primary Academy

Concrete/Pictorial/Abstract



Maths Calculation Policy 2026/27

This updated calculation policy is informed by the National Curriculum, the Devonshire Primary Academy Maths Curriculum Review, the Maths Progression Document, the 2026-2027 Long Term Plans, the Reasoning Road Map, NCETM Teaching for Mastery guidance and Oak National Academy primary mathematics materials. It is a working document and will be reviewed as curriculum guidance and school priorities develop. It provides teachers with a consistent set of models, vocabulary, representations and stem sentences to support pupils in developing secure, flexible and connected understanding of number and calculation.

Recommended practice delivering a mastery approach

True mastery aims to develop all children's mathematical understanding at the same pace. As much as possible, children should be accessing the same learning. Differentiation should primarily be through support, scaffolding and deepening, not through task.

Consistency in language is essential for pupils to understand the concepts presented in mathematics. If other, 'child-friendly' terminology is used, this must be alongside the current terminology recommended by maths specialists. Using this will support children with their examinations and throughout secondary school.

Concrete, pictorial, abstract (CPA) concepts should not be confused as differentiation for lower, middle, higher attaining children. CPA is an approach to be used with the whole class and teachers should promote each area as equally valid. Manipulatives must not be presented as a resource to support the less confident or lower attaining pupils. The abstract should run alongside the concrete and pictorial stage as this enables pupils to better understand mathematical statements and concepts. Real things and structured images enable children to understand the abstract. The concrete and the images are a means for children to understand the symbolic so it's important to move between all modes to allow children to make connections. Morgan, D. (2016)

Used well, manipulatives can enable pupils to inquire themselves- becoming independent learners and thinkers. They can also provide a common language with which to communicate cognitive models for abstract ideas. Drury, H. (2015)

Children aged seven to ten years old work in primarily concrete ways and that the abstract notions of mathematics may only be accessible to them through embodiment in practical resources. Jean Piaget's (1951)

Real things and structured images enable children to understand the abstract. The concrete and the images are a means for children to understand the symbolic so it's important to move between all modes to allow children to make connections. Morgan, D. (2016)

The abstract should run alongside the concrete and pictorial stage as this enables pupils to better understand mathematical statements and concepts.

At Devonshire, calculation is taught through the Five Big Ideas of Teaching for Mastery: Coherence, Representation and Structure, Mathematical Thinking, Fluency and Variation. Learning is broken into small connected steps so pupils know more, remember more and can explain why methods work, not just how to carry them out.



Our overall aim is that when the children leave Devonshire Primary Academy, they:

- Have a secure knowledge of number facts and a good understanding of the four operations.
- Are able to use this knowledge and understanding to carry out calculations mentally and to apply general strategies when using one-digit and two-digit numbers and particular strategies to special cases involving bigger numbers.
- Make use of diagrams and informal notes to help record stages and part answers when using mental methods that generate more information than can be kept in their heads.

2026/27 Curriculum alignment update

This policy now works alongside Devonshire's new mathematics documentation so that calculation methods are not taught as isolated procedures. Teachers should use the policy with the Long Term Plans, Maths Progression Document, Reasoning Road Map, National Curriculum, NCETM materials and Oak National Academy units/teaching guides when planning.

Key curriculum priorities reflected in this policy

- KS1 number foundations: daily practice of number bonds, number composition, additive structures and mental strategies before rushing into written methods.
- Clear progression: pupils move from counting and composition, to additive thinking, then into multiplicative thinking and efficient formal methods.
- Multiplicative reasoning in KS2: multiplication and division must include arrays, grouping, scaling, factors, multiples, efficient methods and problem-solving contexts.
- Reasoning and problem solving: pupils should explain, justify, compare strategies, check using inverse operations and apply methods in unfamiliar contexts.
- Fluency with understanding: retrieval should build automaticity while maintaining conceptual understanding through representations, stem sentences and variation.

How teachers should use this policy

- Use concrete, pictorial and abstract representations with the whole class. CPA is not a lower-attaining scaffold; it is a teaching approach for all pupils.
- Keep mathematical language consistent across year groups. Use the stem sentences and key vocabulary in lessons, retrieval, interventions and displays.
- Select representations that expose structure: ten frames, number lines, part-whole models, bar models, place value charts, arrays, counters and base-ten resources.
- Plan from the year group LTP. Use the NCETM unit links, Oak unit links and teaching guides listed in the LTP to support small-step planning.
- Ensure pupils move flexibly between mental strategies, jottings, diagrams and formal written methods, choosing efficient methods and explaining their choices.

Progression overview for calculation

- EYFS and Reception: subitising, counting, composition, practical combining, separating, sharing and early mathematical talk.
- Year 1 and Year 2: number bonds, facts within 10 and 20, bridging 10, place value, two-digit addition/subtraction using CPA, equal groups, arrays, 2/5/10 facts, sharing and grouping.
- Year 3 and Year 4: secure place value to 1,000/10,000, mental strategies, column addition/subtraction, 3/4/8 and 12 x 12 multiplication facts, short multiplication and division through understanding.
- Year 5 and Year 6: efficient methods with whole numbers and decimals, long multiplication, short and long division, interpreting remainders, order of operations, estimation and inverse checking in multi-step contexts.

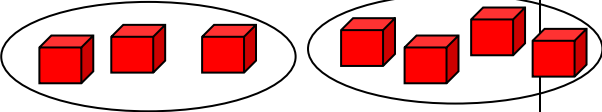
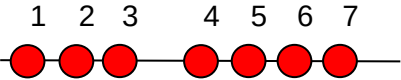
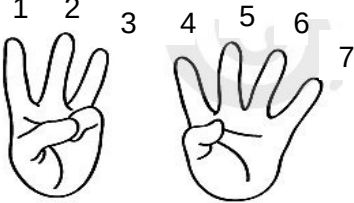
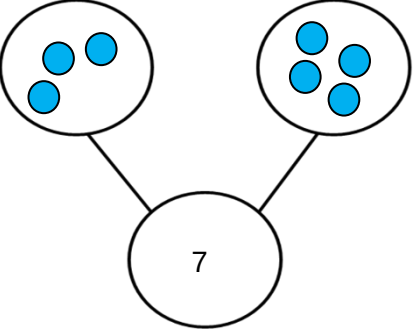
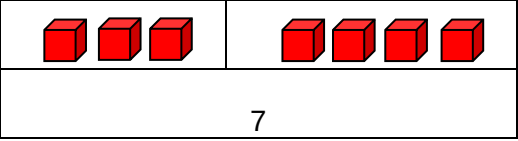
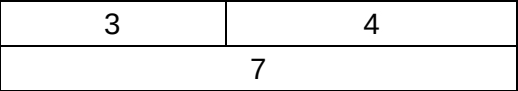
Planning and reference links

- NCETM Teaching for Mastery and Primary Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/>
- Oak National Academy Primary Maths curriculum units and teaching resources: <https://www.thenational.academy/teachers/curriculum/maths-primary/units>
- Devonshire documents: Maths Curriculum Review, Maths Progression Document, Reasoning Road Map, 2026-2027 Long Term Plans and year group curriculum overviews.

Calculation Policy for Addition

Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as', increase.

Key representations: Base 10, bead strings, multilink, counters, Numicon, bar model, number lines, ten frames, fingers, place value counters, 100 square

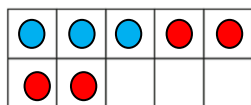
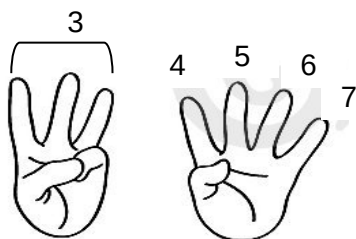
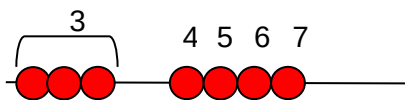
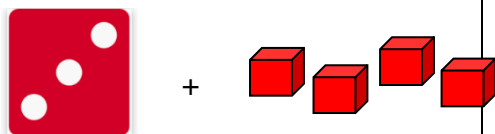
Concrete	Pictorial	Abstract	Stem Sentences
Stage 1: Aggregation-count all all Adding groups to make a whole: $3 + 4 = 7$   	$3 + 4 = 7$   	$3 + 4 = 7$	'__ plus __ is equal to __' '__ is equal to __ plus __' '__ is the sum of __ and __'

1.5

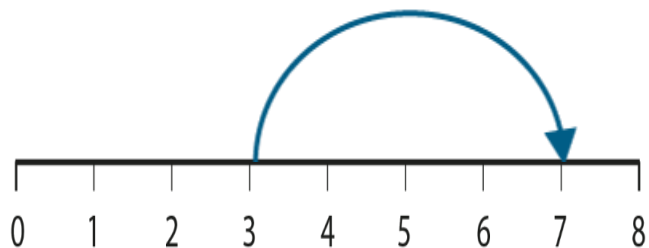
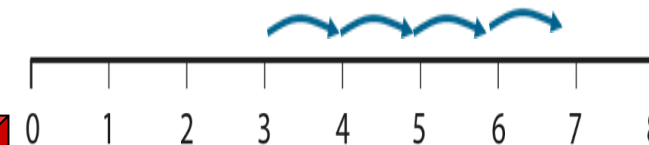
Stage 2: Augmentation- count on

Count on for addition:

$$3 + 4 = 7$$



$$3 + 4 = 7$$



3	4
7	

$$3 + 4 = 7$$

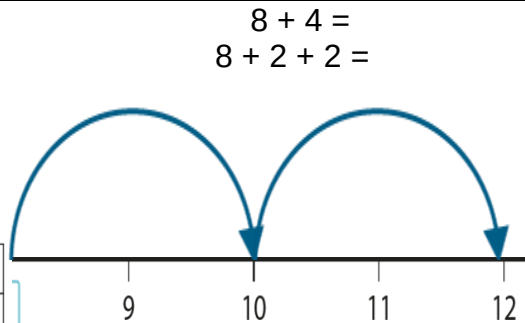
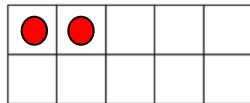
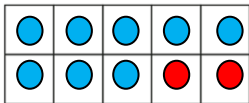
'First... then... now'

'First Jack has 3 sweets, then was given 4 more, now he has 7 sweets'

Stage 3: Bridging through 10:

$$8 + 4 =$$

$$8 + 2 + 2 =$$



8	4
12	

$$8 + 4 =$$

$$8 + 2 + 2 =$$

$$\begin{array}{r} 8 + 4 = \\ \swarrow \quad \searrow \\ 2 \quad 2 \end{array}$$

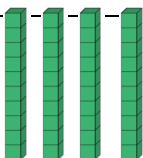
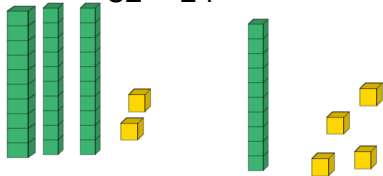
'First I partition the 4-2 plus 2 equals 4.

Then 8 plus 2 is equal to 10.

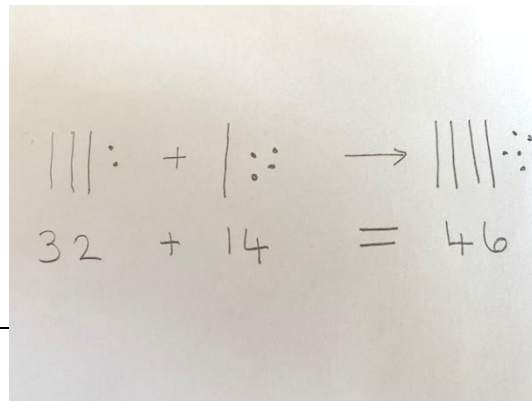
10 plus 2 is equal to 12'

Stage 4: Partitioning and Recombining- to support mental addition

$$32 + 14 =$$



$$32 + 14 =$$



$$32 + 14 =$$

$$30 + 10 = 40$$

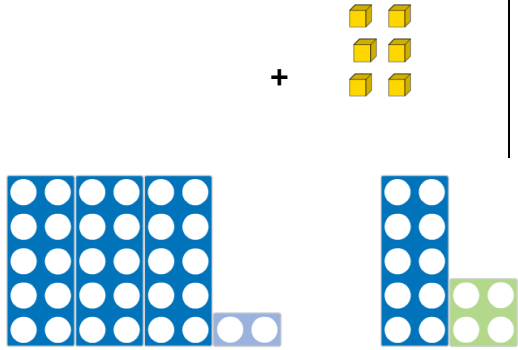
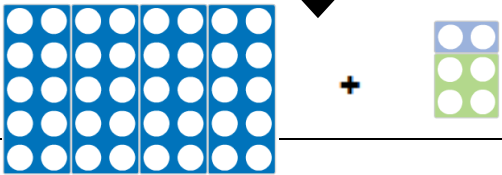
$$2 + 4 = 6$$

$$40 + 6 = 46$$

'First, I add the tens.
3 tens and 1 ten is equal to 4 tens.'

Then I add the ones.
2 ones and 4 ones is equal to 6 ones.

4 tens and 6 ones is equal to 46.

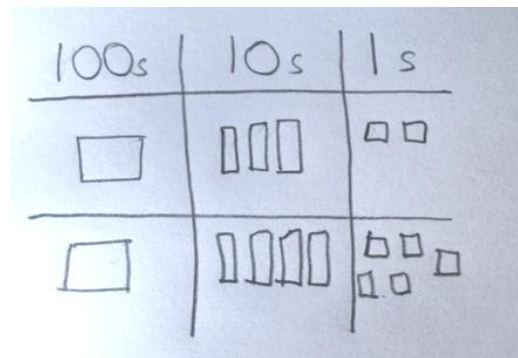
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32	14						
46							
							

Stage 5: Column Addition-no exchange:

132
+145

100s	10s	1s
		
		

100s	10s	1s



$$\begin{array}{r} 132 \\ +145 \\ \hline 277 \end{array}$$

'We line up the ones: 2 ones plus 5 ones equals 7 ones.'

'We line up the tens: 3 tens and 4 tens equals 7 tens.'

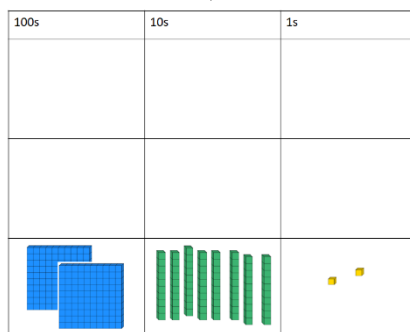
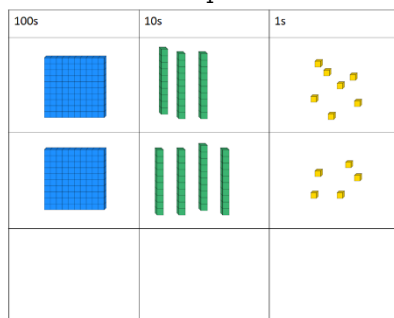
'We line up the hundreds: 1 hundred plus 1 hundred equals 2 hundreds.'

'2 ones plus 5 ones is equal to 7 ones.'

	<table><tr><td>132</td><td>145</td></tr><tr><td colspan="2">?</td></tr></table>	132	145	?			<i>3 tens plus 4 tens is equal to 7 tens.</i> <i>1 hundred plus 1 hundred is equal to 2 hundreds.'</i>	NCE Mast
132	145							
?								
NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/								
Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/								

Stage 6: Column Addition with exchange:

$$\begin{array}{r} 137 \\ +145 \\ \hline 282 \\ \hline 1 \end{array}$$



$$\begin{array}{r} 137 \\ +145 \\ \hline 282 \\ \hline 1 \end{array}$$

137	145
?	

$$\begin{array}{r} 137 \\ +145 \\ \hline 282 \\ \hline 1 \end{array}$$

'If the column sum is equal to 10 or more, we must regroup.'

'7 ones plus 5 ones is equal to 12 ones.'

I regroup 12 ones into 1 ten and 2 ones and place the 10 in the tens column.

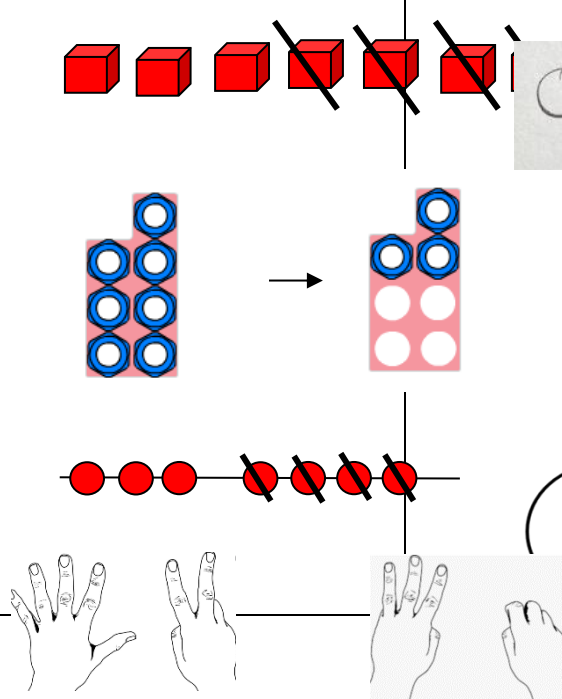
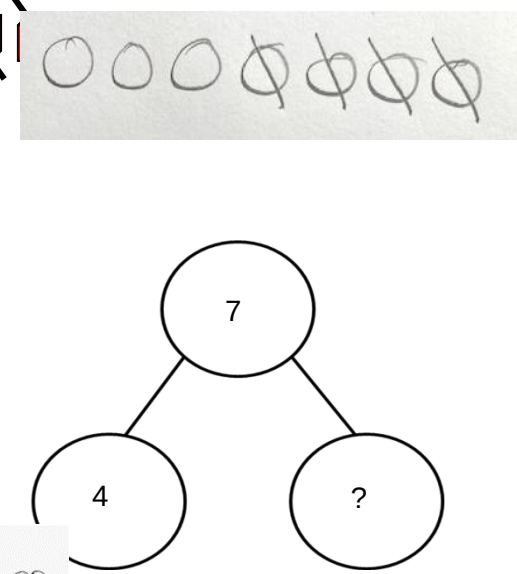
3 tens plus 4 tens plus 1 ten is equal to 8 tens.

1 hundred plus 1 hundred is equal to 2 hundreds.'

Calculation Policy for Subtraction

Key language: subtract, less, fewer, takeaway, difference, leave, minus, decrease

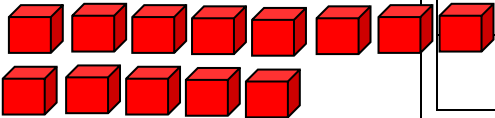
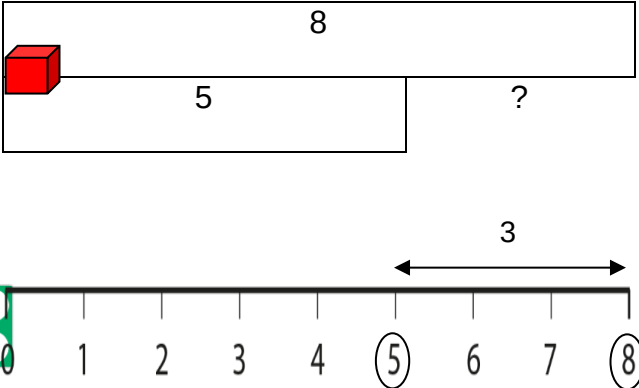
Key representations: Base 10, bead strings, multilink, counters, Numicon, bar model, number lines, ten frames, fingers, place value counters, 100 square

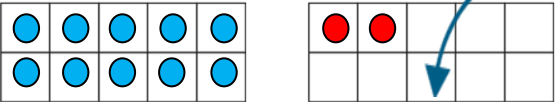
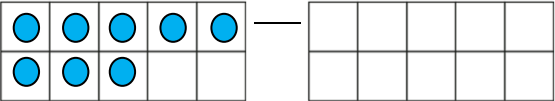
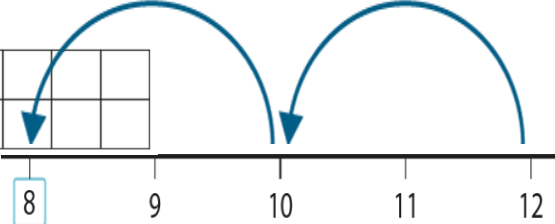
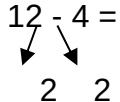
Concrete	Pictorial	Abstract	Stem Sentences
Stage 1: Reduction: Take away $7 - 4 = 3$ 	$7 - 4 = 3$ 	$7 - 4 = 3$	<i>'First... then... now'</i> <i>'First Jack had 7 sweets. Then he ate 4. Now he has 3 sweets left. 7 minus 4 equals 3.'</i>

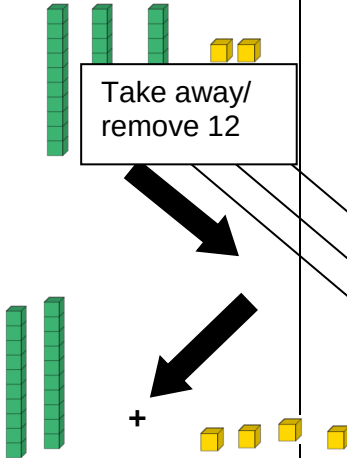
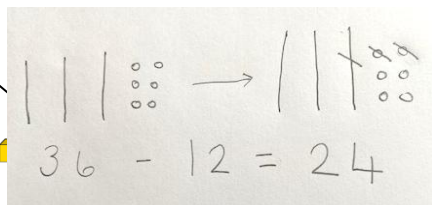
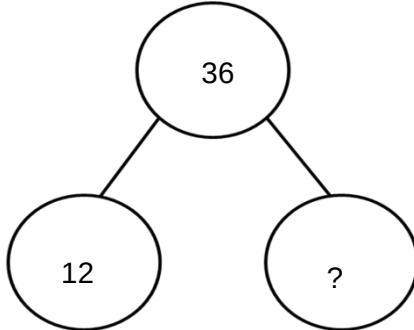
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NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

Stage 2: Count back $7 - 4 = 3$	$7 - 4 = 3$	$7 - 4 = 3$	<i>'Count back 4 from 7.'</i>
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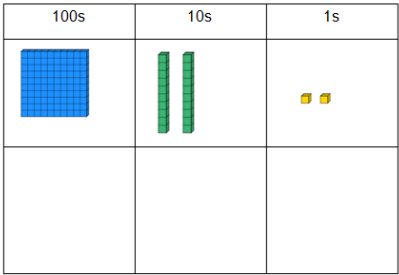
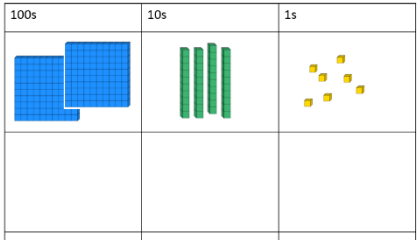
Stage 3: Comparison: Finding the difference $8 - 5 = 3$  	$8 - 5 = 3$ 	$8 - 5 = 3$	<i>'The difference between 8 and 5 is 3.'</i> <i>'The difference between 5 and 8 is 3.'</i> <i>'3 is the difference between 8 and 5.'</i>
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NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/resources/50640 Stage 4: Bridging through 10-to support mental subtraction $12 - 4 =$ $12 - 2 - 2 =$  	$12 - 4 =$ $12 - 2 - 2 =$ 	$12 - 4 =$ $12 - 2 - 2 =$ 	<i>'First I use my knowledge of place value to decide what needs to be subtracted from 12 to make a multiple of 10.'</i> <i>I partition 4 into 2 and 2.</i> <i>Then 12 minus 2 is equal to 10.</i> <i>I use my knowledge of number bonds to 10 to calculate 10 minus 2.</i> <i>10 minus 2 is equal to 8.</i> <i>So 12 minus 4 is equal to 8.'</i>
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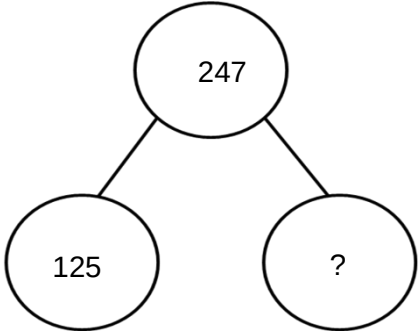
	<table><tr><td colspan="2">12</td></tr><tr><td>4</td><td>?</td></tr></table>	12		4	?		
12							
4	?						
NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/							
1.11							
Stage 5: Partitioning and Recombining- to support mental subtraction 36 - 12 = 	36 - 12 =  <table><tr><td colspan="2">36</td></tr><tr><td>12</td><td>?</td></tr></table>	36		12	?	36 - 12 = 30 - 10 = 20 6 - 2 = 4 20 + 4 = 24	<i>'First, I subtract the tens. 3 tens minus 1 ten is equal to 2 tens.</i> <i>Then I subtract the ones. 6 ones minus 2 ones is equal to 4 ones.</i> <i>2 tens and 4 ones is equal to 24.'</i>
36							
12	?						

Stage 6: Column Subtraction-no exchange:

$$\begin{array}{r} 247 \\ - 125 \\ \hline \end{array}$$



Take away/
remove 125



247	
125	?

$$\begin{array}{r} 247 \\ - 125 \\ \hline 122 \end{array}$$

'We line up the ones: 7 ones minus 5 ones equals 2 ones.'

We line up the tens: 4 tens minus 2 tens equals 2 tens.

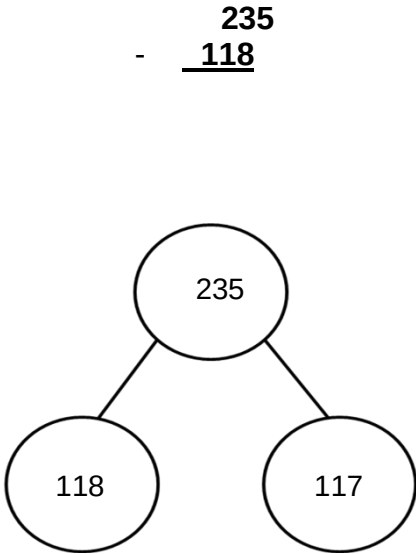
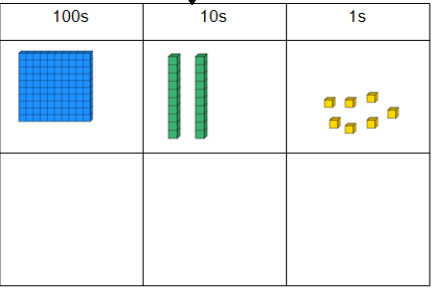
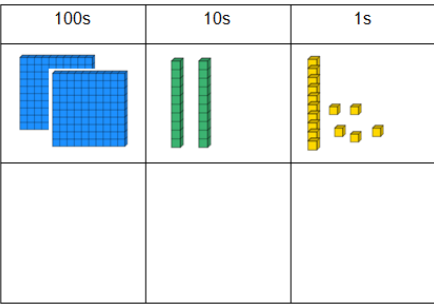
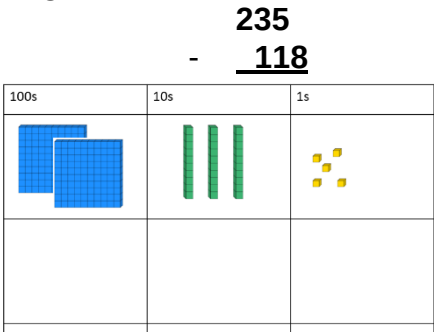
We line up the hundreds: 2 hundreds minus 1 hundred equals 1 hundred.'

'7 ones minus 5 ones is equal to 2 ones.'

4 tens minus 2 tens is equal to 2 tens.

2 hundreds minus 1 hundred is equal to 1 hundred.'

Stage 7: Column Subtraction with exchange:



235	
118	?

NCETM Mastery Professional Development Materials:
<https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>
1.21

235
- 118
117

'5 ones minus 8 ones...we need to exchange 1 ten for 10 ones.

15 ones minus 8 ones is equal to 7 ones.

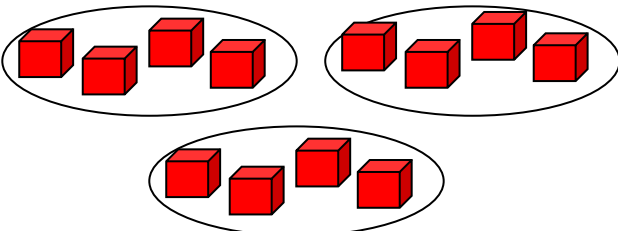
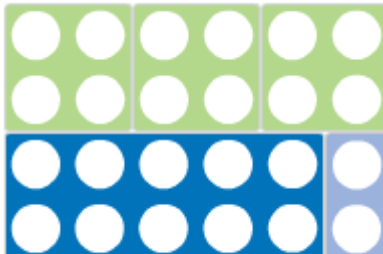
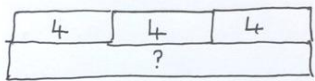
2 tens minus 1 ten is equal to 1 ten.

2 hundreds minus 1 hundred is equal to 1 hundred.'

Calculation Policy for Multiplication

Key language: multiply, times, product, lots of, groups of, multiple, commutative

Key representations: place value counters, base 10, bead strings, multilink, counters, Numicon, bar model, number line

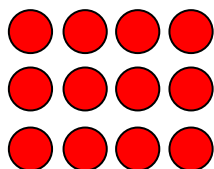
Concrete	Pictorial	Abstract	Stem Sentences
Stage 1: Equal groups: $3 \times 4 = 12$ $4 + 4 + 4 = 12$   	$3 \times 4 = 12$ $4 + 4 + 4 = 12$   	$3 \times 4 = 12$ $4 + 4 + 4 = 12$	'There are __ equal groups.' There are __ in each group. There are __ equal groups of __.' 'If there are __ equal groups, we can use the __ times table.'

NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

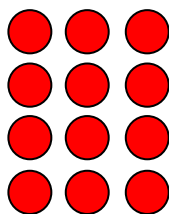
Stage 2: Arrays to show commutativity:

$$3 \times 4 = 4 \times 3$$

$$4 + 4 + 4 = 3 + 3 + 3 + 3$$



=



3 groups of 4 = 4 groups of 3

$3 \times 4 = 4 \times 3$			
$4 + 4 + 4 = 3 + 3 + 3 + 3$			
3	3	3	3
?			
4	4	4	
12			



$$3 \times 4 = 4 \times 3$$

$$4 + 4 + 4 = 3 + 3 + 3 + 3$$

'I can see 3 groups of 4 and I can see 4 groups of 3.'

'3 times 4 can represent 3 groups of 4.'

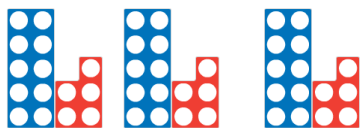
It can also represent 4 times 3.'

'If there are ___ equal groups, we can use the ___ times table.'

NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

Stage 3: Partition to multiply:

$$3 \times 15 =$$



$$3 \times 15 =$$

15	15	15
?		

$$3 \times 15 =$$

$$3 \times 10 = 30$$

$$3 \times 5 = 15$$

'15 is equal to 10 plus 5.'

So 3 times 15 is equal to 3 times 10 plus 3 times 5.'

becomes

3×10 $+$ 3×5

$30 + 15 = 45$

x	10	5
3	30	15

NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

Stage 4: Multiply by 10:

$13 \times 10 =$

100s	10s	1s

$13 \times 10 =$

100s	10s	1s
	1	3
1	3	0

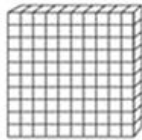
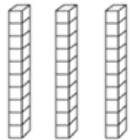
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

13	13	13	13	13	13	13	13	13	13
?									

$13 \times 10 = 130$

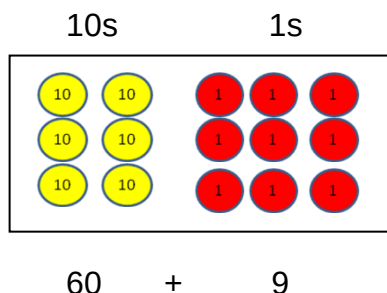
‘__ multiplied by 10 is equal to __.’

‘__ is ten times the size of __.’

					
			NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/		

Stage 5: Short multiplication: 2 digit by 1 digit with no exchange

$$23 \times 3 =$$



$$23 \times 3 =$$

23	23	23
?		

$$23 \times 3 =$$

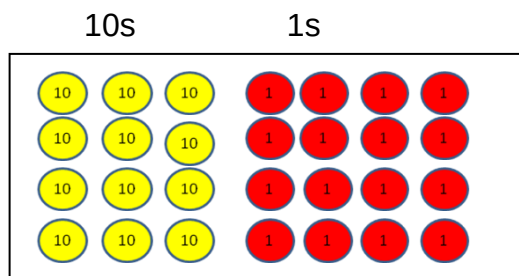
$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

'First we multiply the ones and then we multiply the tens. We add those products together.'

NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

Stage 6: Short multiplication: 2 digit by 1 digit with exchange

$$34 \times 4 =$$



$$34 \times 4 =$$

34	34	34	34
?			

$$34 \times 4 =$$

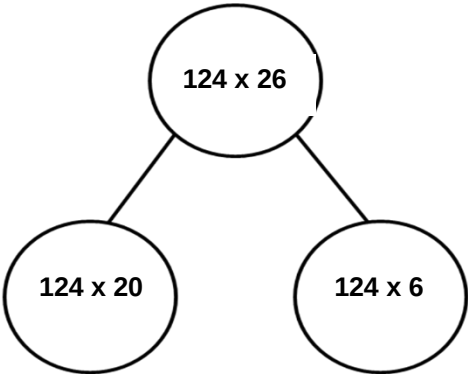
$$\begin{array}{r} 34 \\ \times 4 \\ \hline 16 \\ + \underline{120} \\ \hline 136 \\ \downarrow \end{array}$$

'First we multiply the ones and then we multiply the tens. We add those products together.'

'If there are 10 or more ones, we must regroup the ones into 10s and 1s.'

120 + 16		$\begin{array}{r} 34 \\ \times 4 \\ \hline 136 \\ \hline 1 \end{array}$	
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NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

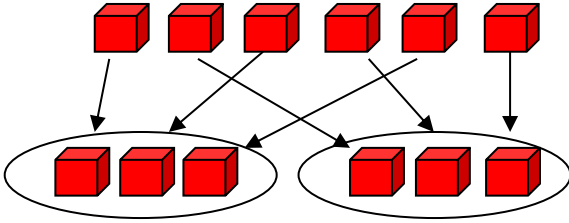
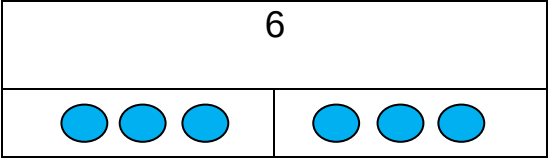
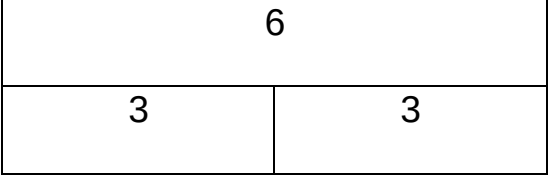
Stage 7: Long multiplication: 3 digit by 2 digit	124 x 26 =  <pre> graph TD A((124 x 26)) --- B((124 x 20)) A --- C((124 x 6)) </pre>	124 x 26 = $\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$	<i>‘If there are 10 or more ones, we must regroup the ones into 10s and 1s.’</i> <i>‘If there are 10 or more hundreds, we must regroup then tens into 100s and 10s.’</i> <i>‘If there are 10 or more hundreds, we must regroup the hundreds into 1000s and 100s.’</i> <i>‘To multiply a three digit number by a two digit number, first multiply by the ones, then multiply by the tens and then add them together.’</i>
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Calculation Policy for Division
- important to make links with Fractions

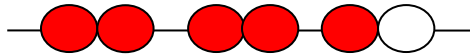
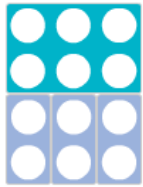
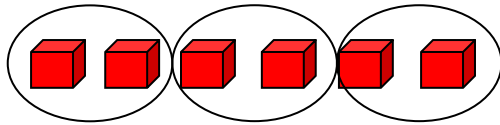
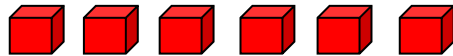
Key language: divide, halve, share, division, factor, remainder, dividend, equal groups of, quotient, divisor

Key representations: place value counters, base 10, bead strings, multilink, counters, Numicon, bar model, number line

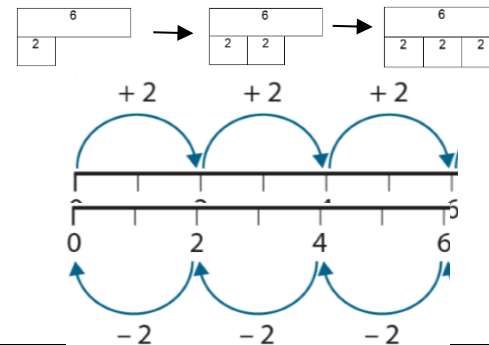
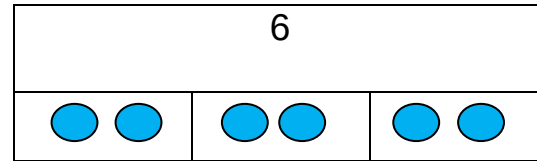
Concrete	Pictorial	Abstract	Stem Sentences
Stage 1: Sharing-Partitive: using a range of discrete concrete objects $6 \div 2 = 3$ 	$6 \div 2 = 3$   	$6 \div 2 = 3$	<i>'6 divided between 2 is equal to 3 each.'</i> <i>'6 shared into 2 equal groups, there are 3 in each group.'</i> <i>'6 is the dividend 2 is the divisor 3 is the quotient.'</i>
NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/			

Stage 2: Grouping-Quotitive: using a range of concrete objects

$$6 \div 2 = 3$$



$$6 \div 2 = 3$$



$$6 \div 2 = 3$$

*'6 is divided into groups of 2.
There are 3 groups.'*

*'6 divided into groups of 2 is
equal to 3.'*

'There are 3 groups of 2 in 6'

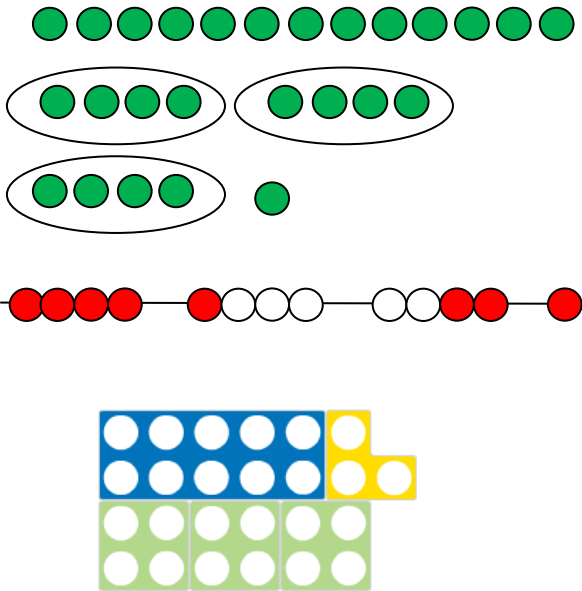
*'6 is the dividend
2 is the divisor
3 is the quotient.'*

*'We can skip count using the
divisor to find the quotient.'*

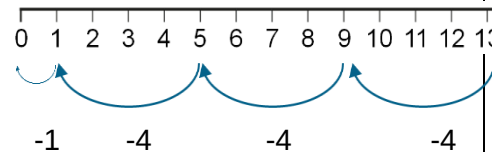
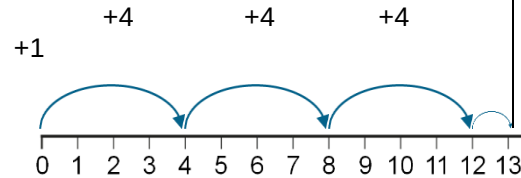
NCETM Mastery Professional Development Materials: <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/>

Stage 3: Grouping-Quotitive: with remainders

$$13 \div 4 =$$



$$13 \div 4 =$$



13		
4	4	4

R1

$$\begin{array}{r} 13 \\ \div 4 \\ = 3 \\ r 1 \end{array}$$

'3 is divided into groups of 4. There are 3 groups and a remainder of 1.'

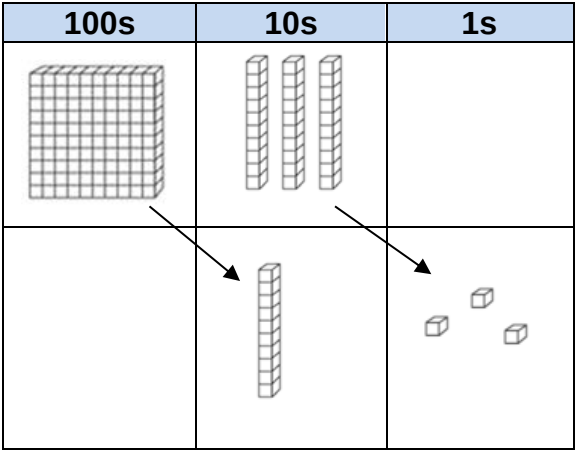
'13 divided into groups of 4 is equal to 3 remainder 1.'

'The remainder is always less than the divisor.'

'If the dividend is not a multiple of the divisor, there is a remainder.'

Stage 4: Divide by 10:

130 ÷ 10 =



130 ÷ 10 =

100s	10s	1s
1	3	0
	1	3

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

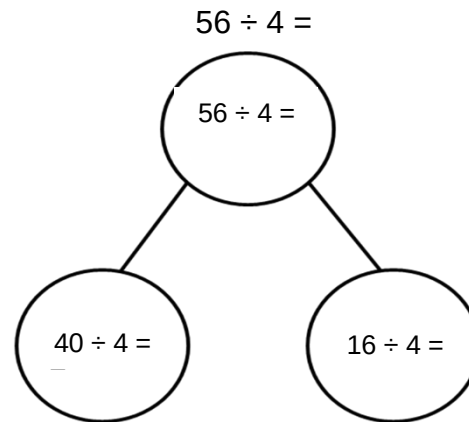
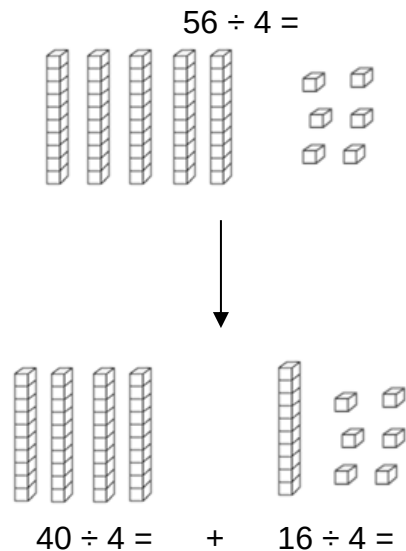
130									
?	?	?	?	?	?	?	?	?	?

130 ÷ 10 = 13

‘__ divided by 10 is equal to __.’

‘__ is ten times smaller than __.’

Stage 5: Partitioning: to support mental calculation
(Only use when the dividend is beyond the twelfth multiple. Before the twelfth multiple, times tables facts should be used).



$$56 \div 4 =$$

Partitive:
'56 is partitioned into 40 and 16.'

'40 divided between 4 is equal to 10 each.'

16 divided between 4 is equal to 4 each.

56 divided between 4 is equal to 1 ten and 4 ones.

Quotitive:
'56 is partitioned into 40 and 16.'

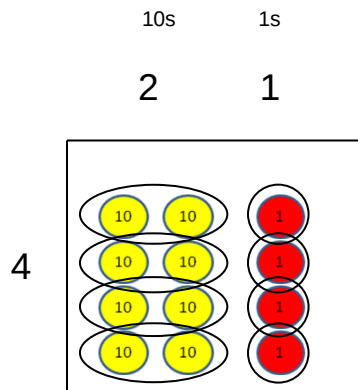
40 is divided into groups of 4. There are 10 groups.'

'16 divided into groups of 4 is equal to 4.'

'There are 14 groups of 4 in 56'

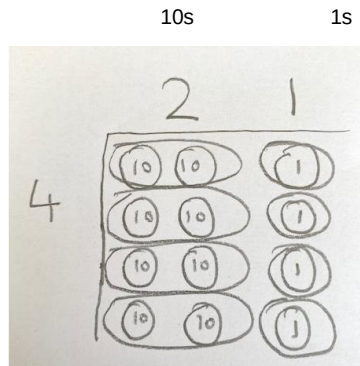
Stage 6: Short division: partitive: 2 digit by 1 digit (with no exchange)
(Only use when the dividend is beyond the twelfth multiple. Before the twelfth multiple, times tables facts should be used).

$$84 \div 4 = \quad 4 \overline{) 84}$$



$$84 \div 4 =$$

$$4 \overline{) 84}$$



84			
?	?	?	?

$$84 \div 4 = 21$$

10s	1s
2	1

$$4 \overline{) 84}$$

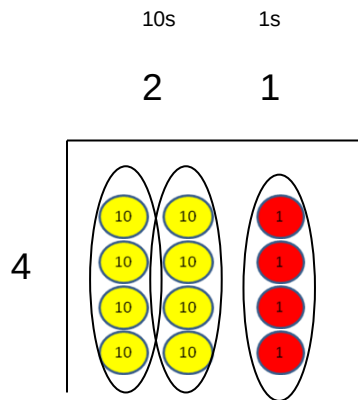
'8 tens divided between 4 is equal to 2 tens each.

4 ones divided between 4 is equal to 1 one each.

8 tens and 4 ones divided between 4 is equal to 2 tens and 1 one, which is 21.

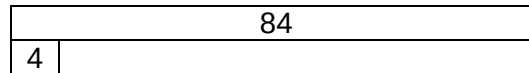
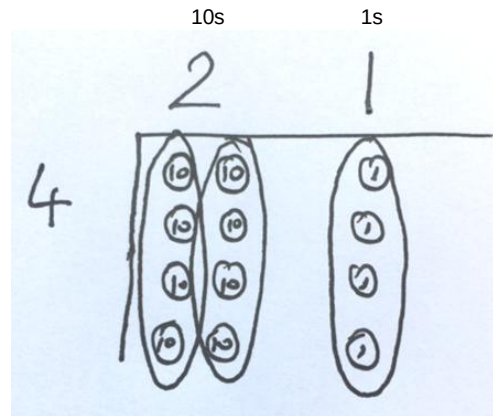
Stage 7: Short division: quotitive 2 digit by 1 digit (with no exchange)
(Only use when the dividend is beyond the twelfth multiple. Before the twelfth multiple, times tables facts should be used).

$$84 \div 4 = \quad 4 \overline{) 84}$$



$$84 \div 4 =$$

$$4 \overline{) 84}$$



$$84 \div 4 = 21$$

10s 1s

2 1

4 $\overline{) 84}$

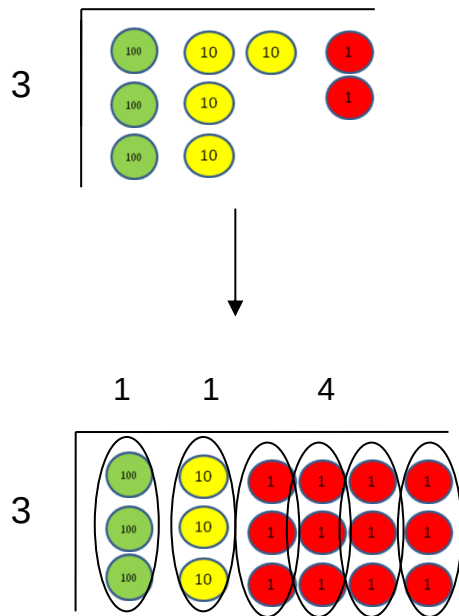
'8 tens are divided into groups of 4. There are 2 groups.'

'4 ones are divided into groups of 4. There is 1 group.'

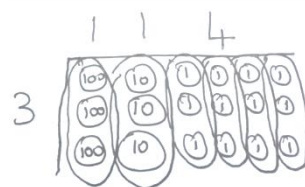
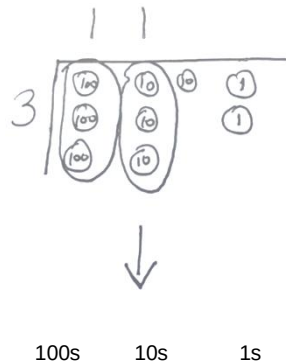
2 groups of ten and 1 one is 21. The quotient is 21.

Stage 8: Short division: quotitive 2 digit by 1 digit (with exchange)
(Only use when the dividend is beyond the twelfth multiple. Before the twelfth multiple, times tables facts should be used).

$$342 \div 3 = 3 \overline{)342}$$



$$342 \div 3 = 3 \overline{)342}$$



$$342 \div 3 = 114$$

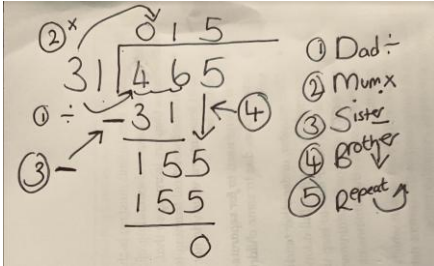
$$\begin{array}{r} 100s \quad 10s \quad 1s \\ 1 \quad 1 \quad 4 \\ 3 \overline{)342} \end{array}$$

'3 hundreds divided by 3 is 1 hundred.

4 tens divided by 3 is 1 group remainder 1 ten.

Exchange 1 ten for 10 ones.

12 ones divided by 3 is equal to 4.'

Stage 9: Formal division: with 2-digit divisors		Short Division $465 \div 31 =$ $\begin{array}{r} 0 \ 1 \ 5 \\ 31 \overline{) 4 \ 6 \ 5} \\ \underline{4 \ 6} \\ 15 \\ \underline{15} \\ 0 \end{array}$ (It may be helpful to write a list of multiples of 31 e.g. 31, 62, 93, 124, 155)	Long Division $465 \div 31 =$ $\begin{array}{r} 0 \ 1 \ 5 \\ 31 \overline{) 4 \ 6 \ 5} \\ \underline{3 \ 1} \\ 1 \ 5 \ 5 \\ \underline{1 \ 5 \ 5} \\ 0 \end{array}$  Get children to make up their own acronyms to help them remember the process.
NCETM Mastery Professional Development Materials: https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/			

Calculation Policy for Reasoning, Greater Depth and Mastery

Key language:

What do we mean by mastery? The essential idea behind mastery is that ALL children need a deep understanding of the mathematics they are learning so that: • Future mathematical learning is built on solid foundations which do not need to be re-taught; • There is no need to for separate catch-up programmes due to some children falling behind; • Children who, under other teaching approaches, can often fall a long way behind, are better able to keep up with their peers, so that gaps in attainment are narrowed whilst the attainment of all is raised. There are generally four ways in which the term mastery is being used in the current debate around raising standards in mathematics.		1.A mastery approach: a set of principles and beliefs. This includes a belief that all pupils are capable of understanding and doing mathematics, given sufficient time. Pupils are neither ‘born with the maths gene’ nor ‘just no good at maths’. With good teaching, appropriate resources, effort and a ‘can do’ attitude all children can achieve in and enjoy mathematics. 2.A mastery curriculum: one set of mathematical concepts and big ideas for all. All pupils need access to these concepts and idea and to the rich connections between them. Mathematics is mathematics and the key ideas and building blocks are important to everyone. 3.Teaching for mastery: a set of pedagogic practices that keep the class working together on the same topic, whilst at the same time addressing the need for all pupils to master the curriculum and for some to gain greater depth of proficiency and understanding. Challenge is provided by going depth and sufficient practice to embed learning.		4.Achieving mastery of particular topics and areas of mathematics. Mastery is not just being able to memorise key facts and procedures and answer test questions accurately and quickly. It involves knowing ‘why’ as well as knowing ‘that’ and knowing ‘how’. It means being able to use apply it in new and unfamiliar situations. Mastery of the curriculum requires that all pupils: • Use mathematical concepts, facts and procedures appropriately, flexibly and fluently; • Recall key number facts with speed and accuracy and use them to calculate and work out unknown facts; • Have sufficient depth of knowledge and understanding to reason and explain mathematical concepts and procedures and use them to solve a variety of problems.	
Key questions: -Odd one out -True or false?	-Would you rather have... -Here is the.. -Tell me about this ... -prove/disprove this statement	-find the mistake -always, sometimes, never -convince me that -how are these linked?	What is the same and what is different? Give me a silly answer to this problem. What makes it silly? What if...? If you know this fact, what else do you know? E.g. if you know: 4 + 6 =10		

- Give me a hard and easy example of a five- digit calculation. -Give me a hard and easy example of a question you could ask about this graph/pie chart etc.	-challenge -agree -Build on -what do you know...		You know: $40+60=100$ $100-40=60$ The sum of 6 and 4 is 10. $4000+600=10,000$ $100,000-60,000=40,000$ If it is 6'o'clock now, in 4 hours it will be 10'o'clock.
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