

If you were interested in the maths...

The number of possible combinations can be worked out using factorials.

If we only have 1 card: A. There is only one way we can put it in order.

If we have two cards A and B, there are two different ways - AB or BA.

With three cards, A, B and C there are six different ways - ABC, ACB, BAC, BCA, CAB, CBA

So, for 1 card it is 1. For two cards it is $2 \times 1 = 2$. For three cards it is $3 \times 2 \times 1 = 6$. As mathematicians we write $3 \times 2 \times 1$ as $3!$ The ! sign is called a factorial.

So, 4 cards is $4! = 24$ ways. 5 cards is $5! = 120$ ways. 6 cards is $6!$ ways = 720 ways.

As you introduce more cards, it starts to get very big very quickly.

If there were 10 cards, $10!$ is 3,628,800. For 13 cards, $13!$ is 6,227,020,800.

The number of ways you can arrange 20 cards is 2,432,902,008,176,640,000. That's two and a half billion billion.

So our 52 cards in a pack?

The number of combinations is $52 \times 51 \times 50 \times 49 \times 48 \dots \times 4 \times 3 \times 2 \times 1$ which is:

80,658,175,170,943,878,571,660,636, 856,403,766,975,289,505,440,
883,277,824,000,000,000,000

To put this in perspective, the dinosaurs died out 65,000,000 years ago, and the age of the earth is just 4,500,000,000 years. Now suppose everybody in the world was to arrange packs of cards at the rate of one per second, it would take 600,000,000,000,000,000,000,000,000,000,000,000,000,000,000,000,000,000,000 years to get all the combinations! That's why you're VERY unlikely ever to shuffle a pack of cards the same way twice.