

## Durham Johnston

 Mathematics Department
## An introduction to

## A Level Mathematics.

Notes

## An introduction to A level mathematics at DJCS.

Thank you for choosing to study Mathematics at Durham Johnston. We follow the new OCR linear specification, Mathematics A - H230/H240 and Further Mathematics A - H235/H245.

All mathematics students at Durham Johnston will sit AS mathematics exams at the end of Year 12. If you also opt for further maths you will sit AS exams in further maths too.

Algebra is the language of mathematics and your success in the examinations next year is dependent upon your fluency in basic number work and in algebraic manipulation as well as your ability to write clear, coherent and detailed solutions to problems. You must be willing to perfect a range of skills that you have already met at GCSE such as simplifying surds, working with indices and rearranging formulae.

In week 2 of your course you will take a basic algebra test. The pass mark for this test is $60 \%$. If you do not pass this test you will be interviewed by the Subject Leader, to discuss your next steps and your parent/guardian will be informed. You will be given a programme of additional work to complete and you will take a second test immediately after the October half term holiday. This second test will take place at the end of a school day.

A mock test is provided in this booklet.
It is important to cultivate good study skills from the very beginning of your course. Organise your notes and examples in a folder and make sure that you take an active part in every lesson. Complete every set task and meet deadlines. You must persevere when the going gets tough and take action when you need help. The teachers in the mathematics department at Durham Johnston are very experienced and are always willing to provide support and guidance.

Mrs Urwin
Subject Leader for Mathematics

## Calculators and Computers

The current linear A level specifications all require an advanced calculator with built-in statistical distribution functions. The calculator you used for GCSE and the "advanced" calculators available in the shops will often not be good enough. There are two current non-graphical calculators that are suitable. The Casio Fx-991 Classwiz is our preferred calculator. The new model is the Fx-991CW Classwiz, which is the replacement for the Fx991EX Classwiz (The 991EX may still be available in some places, or available second hand). Other calculators that have the necessary built-in statistical distributions are the TI-30X Pro and most graphical calculators. If you wait until September you will be able to buy a Casio Fx-991 Classwiz through the school. Also check the supermarket "back to school" displays. They had the Classwiz for sale earlier in 2023, but in very small quantities.


You should also have the facility to draw graphs and manipulate statistical data to aid your learning throughout the course. There's no need to purchase expensive equipment or software for this. We recommend the excellent and free Geogebra. You should download their graphing calculator app to your phone/tablet (iOS or Android) and install Geogebra Classic on your Windows machine or Mac.

## Further help

- The exam board, OCR, provides a very useful bridging guide. This contains detailed examples and exercises for you to work through. It can be found on the website at http://www.ocr.org.uk/lmages/373371-bridging-the-gap-between-gcse-and-as-a-level-mathematics-a-student-guide.docx .
- A very useful source of help is Khan Academy www.khanacademy.org

You will need to register and create a username and password.

- You may also find the following books useful:

| Head Start to A-Level Maths | AlphaWorkbooks |
| :--- | :--- |
| Published by CGP Workbooks | Preparation for AS/A level Mathematics |
| ISBN: 9781782947929 | Available from |
| $£ 5.95$ | www.alphaworkbooks.co.uk |
|  | $£ 3.99$ |
|  | The Mathematics Department has a supply |
|  | of these books available for $£ 2.00$ each |
|  |  |

## Suggested Reading List

Alex's Adventures in Numberland by Alex Bellos
Professor Stewart's Cabinet of Mathematical Curiosities by Ian Stewart
Fermat's Last Theorem by Simon Singh
The Num8er My5teries by Marcus du Sautoy
How Many Socks Make a Pair? Surprisingly Interesting Maths by Rob Eastway
The Curious Incident of the Dog in the Night-time by Mark Haddon
The Penguin Dictionary of Curious \& Interesting Numbers by David Wells
The Code Book by Simon Singh
50 Mathematical Ideas You Really Need to Know by Tony Crilly
Gödel's Proof by Ernest Nagel and James R. Newman
Gödel, Escher, Bach: An Eternal Golden Braid by Douglas R. Hofstadter
The Pleasures of Counting by T. W. Körner

## How to be a successful mathematics student

| Don't expect the teacher to notice you are <br> stuck - ask for help. | Take an active role in your learning. <br> Those who get highest marks are often those <br> who ask lots of questions and discuss their <br> work with others. |
| :--- | :--- |
| Set work out in exactly the same way as your <br> teacher does - there is always a good reason <br> for this. | Write equals signs underneath each other. <br> Remember to answer the question and say <br> what it is you've calculated. |
| Be intrigued if you're wrong - work out why. | Mathematicians are people who don't <br> necessarily get the right answer straight away <br> - but they are interested in why their answer is <br> wrong and they PERSEVERE to correct it. <br> Mathematics is about trial and improvement <br> - not right and wrong. |
| If you can't explain something to someone <br> else, you're not sure enough - do more work <br> on it. | EXPECT to have to work at something and for <br> it to take several goes. This may feel different <br> to GCSE where perhaps you didn't have to. |
| Mark your own work using the answers in the | Using the answer to help you to understand <br> isn't cheating. <br> When handing in work, tick the work that is <br> correct, make corrections when you can and <br> annotate any remaining wrong answers to |
| help your teacher to see where you are |  |
| having difficulties. |  |

## DJCS Mathematics Department

GCSE to AS induction - practice exercise.

1. Evaluate

$$
10^{2} \quad 64^{1 / 2} \quad 8^{-4 / 3}
$$

2. Express as a power of 3

$$
3^{2} \times 3^{5} \quad 3^{10} \div 3^{2} \quad\left(3^{2}\right)^{3} \quad 3^{2} \times 9^{4}
$$

3. The points A, B and C have the following coordinates: $\mathrm{A}(7,5), \mathrm{B}(3,-3)$ and $\mathrm{C}(-1,9)$.

- Find the gradient of $\mathrm{AB}, \mathrm{BC}$ and CA .
- What type of triangle is triangle ABC ?
- Find the area of triangle ABC
- Find the equation of the line parallel to AB , passing through the point $\mathrm{D}(1,4)$

4. Expand and simplify:

- $(5 x+3)^{2}+(3 x+1)^{2}$
- $(5 x+3)^{2}-(3 x+1)^{2}$
- $3(5 x+3)^{2}+2(3 x+1)^{2}$
- $3(5 x+3)^{2}-2(3 x+1)^{2}$

5. Simplify

$$
\begin{array}{lllll}
\sqrt{75} & \sqrt{72} & \sqrt{48} & \sqrt{80} & \sqrt{98}
\end{array}
$$

6. Express in the form $a \sqrt{b}$

$$
\sqrt{75}+\sqrt{48} \quad \sqrt{98}-\sqrt{72}
$$

7. Rationalise
$\frac{10}{\sqrt{5}}$
$\frac{12}{\sqrt{3}}$
$\frac{4}{1+\sqrt{7}}$
$\frac{42}{5-\sqrt{2}}$
$\frac{10}{2-\sqrt{3}}$
8. Solve the following, leaving your answers in surd form where necessary.

- $x^{2}+x-12=0$
- $2 x^{2}+5 x-3=0$
- $16-x^{2}=0$
- $3 x^{2}+10 x-5=0$

9. Solve the following inequalities

- $2 x+10 \leq 17$
- $x^{2}+x-12 \leq 0$
- $2 x^{2}+5 x-3 \geq 0$

