

Head Start to A-Level Physics

Work through this book, completing the questions from the bottom of each page.

Answers are provided at the back.

If you need any help with any of it and want any more information, please get in touch with Mr Read (jread@ems.bhcet.org.uk)

Bridging the gap between GCSE and A-Level

Head Start to A-Level Physics

A-Level Physics is a **big step up** from GCSE... no doubt about that. But don't worry — this CGP book has been lovingly made to help you hit the ground running at the start of your A-Level (or AS-Level) course.

It recaps everything you'll need to remember from GCSE, and introduces some of the crucial concepts you'll meet at A-Level. For every topic, there are crystal-clear study notes and plenty of practice questions to test your skills.

What CGP is all about

Our sole aim here at CGP is to produce the highest quality books - carefully written, immaculately presented and dangerously close to being funny. Then we work our socks off to get them out to you - at the cheapest possible prices.

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SYMBOLS AND UNITS

Symbols and Units

At A-Level, you're expected to use standard scientific notation. This means using conventional symbols and units, and writing very large and very small numbers in standard form.

The table below lists the different quantities you'll come across in this book, with their standard symbols and units:

At A-Level, units like m/s are written ms^{-1} . This is just index notation. (If it doesn't make sense to you, look up 'rules of indices' in a maths book.)

Standard form lets us write very big or very small numbers in a more convenient way. It looks like this:

For example:

53100 can be written as 5.31×10^4 , and 2.5×10^{-3} is the same as 0.0025.

You might also see large or small numbers given in units with these prefixes:

Make sure you give your answers to questions to a sensible number of significant figures. An easy way to do this is by always rounding your answers to the same number of significant figures as the given data value you've used in the calculation with the least significant figures. Then write the number of significant figures you've rounded your answer to: e.g. $2 \div 3.5 = 0.571... = 0.6$ (to 1 s.f.) $(2 \text{ is to } 1 \text{ s.f., } 3.5 \text{ is to } 2 \text{ s.f., so the answer needs to be given to } 1 \text{ s.f.)}$

S_{FCTION} 1 $-$ Forces and Motion

Speed, Displacement and Velocity

Distance. Time and Speed are all Related

Points A and B are separated by a distance in metres. Now imagine a spider walking from A to B — you can measure the **time** it takes, in **seconds**, for it to travel this distance.

You can then work out the spider's **average speed** between A and B using this **equation**:

speed (in metres per second) = distance travelled (in metres) \div time taken (in seconds)

B

This is a very useful equation, but it does have a couple of *limitations*:

- 1) It only tells you the average speed. The spider could vary its speed from fast to slow and even go **backwards**. So long as it gets from A to B in the same time you get the same answer.
- 2) We assume that the spider takes the **shortest possible path** between the two points (a straight line), rather than **meandering** around.

Displacement is a Vector Quantity

To get from point A to point B you need to know what **direction** to travel in $-$ just knowing the distance you need to travel isn't enough.

This information, distance plus direction, is known as the displacement from A to B and has the symbol s . It's a **vector** quantity — **all** vector quantities have both a **size** and a **direction**.

There is a Relationship Between Displacement and Velocity

Velocity is another vector quantity $-$ velocity is the speed and direction of an object. The **velocity** of an object is given by the following equation:

velocity (in metres per second) = **displacement** (in metres) \div **time taken** (in seconds)

Or, in symbols: $v = \frac{s}{4}$

This equation is very similar to the one relating speed and distance. except that it includes information about the direction of motion.

Displacement's in a relationship with velocity now, it's so over time...

- 1) An athlete runs a 1500 m race in a time of 210 seconds. What is his average speed?
- 2) The speed of light is 3.0×10^8 ms⁻¹. If it takes light from the Sun 8.3 minutes to reach us, what is the distance from the Earth to the Sun?
- 3) A snail crawls at a speed of 0.24 centimetres per second. How long does it take the snail to travel 1.5 metres?
- 4) How long does it take a train travelling with a velocity of 50 ms⁻¹ north to travel 1 km?
- 5) If someone has a velocity of 7.50 ms⁻¹ south, what is their displacement after 15.0 seconds?

Drawing Displacements and Velocities

You can use Scale Drawings to Represent Displacement

The simplest way to draw a vector is to draw an **arrow**. So for a displacement vector the length of the arrow tells you the distance, and the way the arrow points shows you the direction.

You can do this even for very large displacements so long as you scale down. Whenever you do a scale drawing, make sure you **state the scale** you are using.

You can also Represent Velocities with Arrows

Velocity is a **vector**, so you can **draw arrows** to show velocities too. This time, the **longer** the arrow, the greater the speed of the object. A typical scale might be 1 cm to 1 ms^{-1} .

Drawing displacements - not about leaving your sketchbook at home...

- 1) Draw arrows representing the following displacements to the given scale:
	- a) 12 m to the right (1 cm to 2 m)
	- b) 110 miles at a bearing of 270° (1 cm to 20 miles)
- 2) Draw an arrow to represent each velocity to the given scale. Take north to be up the page.
	- a) 60 ms^{-1} to the south-east (1 cm to 15 ms^{-1})
	- b) 120 miles per hour to the west (1 cm to 30 miles per hour)

Combining Displacements and Velocities

You can use Arrows to Add or Subtract Two Vectors...

To add two velocity or displacement vectors, you can't simply add together the two distances as this doesn't account for the different directions of the vectors. What you do is:

- 1) Draw arrows representing the two vectors.
- 2) Place the arrows one after the other "tip-to-tail".
- 3) Draw a third arrow from start to finish. This is your resultant vector.

2) Initial velocity = 1.0 ms⁻¹ west and final velocity = 3.0 ms⁻¹ north. Find the size of Δv .

Resolving Vectors

You can Split a Vector into Horizontal and Vertical Components

- 1) Vectors like velocity and displacement can be split into components.
- 2) This is basically the opposite of finding the resultant you start from the resultant vector and split it into two separate vectors at right angles to each other.
- 3) Together these two components have the same effect as the original vector.
- 4) To find the components of a vector, v , you need to use **trigonometry**:

Resolving is dead useful because the two components of a vector don't affect each other. This means you can deal with the two directions completely separately.

- If you throw a ball diagonally up and to the right...
- Only the vertical component of the velocity is affected by gravity (see page 7).
- You can calculate the ball's vertical velocity (which will be affected by gravity).
- And you can calculate the ball's horizontal velocity (which won't be affected by gravity).

EXAMPLE: A helium balloon is floating away on the wind. It is travelling at 4.3 ms⁻¹ at an angle of 37° to the horizontal. What are the vertical and horizontal components of its velocity? It's useful to start off by drawing a diagram:

Horizontal velocity = v_r = $v \cos \theta$ = 4.3 $\times \cos 37$ $= 3.434... = 3.4$ ms⁻¹ (to 2 s.f.) Vertical velocity = v_v = v sin θ = 4.3 \times sin 37 $= 2.587... = 2.6$ ms⁻¹ (to 2 s.f.)

Solve these questions by re-solving the vectors...

- 1) A rugby ball is moving at 12 ms^{-1} at an angle of 68 \degree to the horizontal. Find the horizontal and vertical components of the ball's velocity.
- 2) A plane is travelling at 98 ms⁻¹ at a constant angle as it gains altitude. The horizontal velocity of the plane is 67 ms⁻¹. What is its angle of ascent?
- 3) A hot air balloon descends at a velocity of 5.9 ms^{-1} at an angle of 23° to the horizontal. How long does it take the balloon to descend 150 m?

 $v \sin \theta$

Acceleration

Acceleration - the Change in Velocity Every Second

Acceleration is the rate of change of velocity. Like velocity, it is a vector quantity (it has a size and a direction). It is measured in **metres per second squared** ($ms⁻²$).

Acceleration (in metres per second²) = $\frac{\text{change in velocity}}{\text{in meters per second}}$

So:

final velocity - initial velocity $Acceleration =$ time taken

Or in symbols:

 $a = \frac{v - u}{t} = \frac{\Delta v}{t}$ where *u* is the union vertex the change in velocity. where u is the initial velocity, v is the final velocity

You'll often only need to think about velocities in one dimension, say left to right. But you still need to recognise the **difference** between velocities from right to left and velocities from left to right.

Choose a direction to be positive - below, we'll use right. All velocities in this direction will from now on be positive, and all those in the **opposite direction** (left) will be **negative**. Deceleration is negative acceleration and acts in the opposite direction to motion.

EXAMPLE: A car starts off moving to the right at 15.0 metres per second. After 30.0 seconds it is moving to the left at 5.25 metres per second. What was its acceleration during this time?

 $u = 15.0$ ms⁻¹ to the right = +15.0 ms⁻¹ $v = 5.25$ ms⁻¹ to the left = -5.25 ms⁻¹ So, $a = \frac{v - u}{t} = \frac{-5.25 - 15.0}{30.0} = \frac{-20.25}{30.0} = -0.675$ ms⁻² (The acceleration is negative so it's to the left.)

EXAMPLE: A dinosaur accelerates from rest at 4.00 ms^{-2} to the right. If its final velocity is 25.0 ms⁻¹ to the right, how long does it accelerate for?

 $u = 0.00$ ms⁻¹ $v = 25.0$ ms⁻¹ to the right = +25.0 ms⁻¹ $a = \frac{v - u}{t}$, multiplying both sides by t gives $a \times t = v - u$, and then dividing both sides by a gives $t = \frac{v - u}{a}$. So, $t = \frac{25.0 - 0}{4.00} = 6.25$ s

A seller rating is the key thing to check when buying a car online...

- 1) A train has an initial velocity of 12.8 ms⁻¹ to the left. After 22.0 seconds it is moving to the right at 18.3 ms⁻¹. What was its average acceleration during this time?
- 2) A ship accelerates at a uniform rate of 0.18 ms⁻² east. If its initial velocity is 1.5 ms⁻¹ east and its final velocity is 4.5 ms⁻¹ in the same direction, how long has it been accelerating for?
- 3) A rabbit is hopping at a constant speed when he begins decelerating at a rate of 0.41 ms⁻². What was the rabbit's initial hopping speed if it takes him 3.7 seconds to come to a stop?

Acceleration Due To Gravity

The Acceleration Due to Gravity is a

When an object is dropped, it accelerates downwards at a constant rate of roughly 9.81 ms^{-2} . This is the **acceleration due to gravity** and it has the symbol **g**.

It usually seems sensible to take the upward direction as positive and down as negative, making the acceleration due to gravity -9.81 ms⁻².

EXAMPLE: What is the vertical velocity of a skydiver 5.25 seconds after she jumps out of a plane that is travelling at a constant altitude? (Ignore air resistance and horizontal motion.) $u = 0$ $a = -9.81$ ms⁻² You can rearrange $a = \frac{V - U}{t}$ to give $v = u + (a \times t)$.

So $v = 0 + (-9.81 \times 5.25)$ $= 0 - 51.5025$ $=-51.5025 = 51.5$ ms⁻¹ down (to 3 s.f.)

EXAMPLE: A diver jumps up off a springboard. After 2.50 seconds he hits the water travelling downwards at 18.0 ms⁻¹. What was his initial vertical velocity? (Ignore air resistance and horizontal motion.)

 $v = 18.0$ ms⁻¹ down = -18.0 ms⁻¹ $a = -9.81$ ms⁻² You can rearrange $a = \frac{V-U}{t}$ to give $u = v - (a \times t)$. So, $u = -18.0 - (-9.81 \times 2.50)$ $=-18.0 - (-24.525)$ $=-18.0 + 24.525$ $= 6.525 = 6.53$ ms⁻¹ upwards (to 3 s.f.)

This isn't falling, it's learning with style...

You can ignore air resistance in these questions. Hint — drawing a little diagram can help.

- 1) An apple falls from a tree and hits the ground at 4.9 ms⁻¹. For how long was it falling?
- 2) A stone is thrown straight downwards. It hits the ground at 26.5 ms⁻¹ after 2.15 seconds. What velocity was it thrown at?
- 3) A metal rod falls from a stationary helicopter. What velocity does it hit the ground at, 10.0 seconds later?
- 4) A sandbag is dropped from a stationary hot-air balloon. It hits the ground at a velocity of 24.5 metres per second. How long was it falling for?
- 5) A ball is thrown straight upwards. After 1.90 seconds it is moving downwards at 10.7 ms⁻¹ and is caught. With what velocity was it thrown?

 $\mathbb{C}^{\mathbb{C}}$

Displacement-Time Graphs

EXAMPLE: The displacement-time graph below shows a motorcyclist accelerating to a constant speed, braking and then riding a short distance in the opposite direction. You can read the following directly off the graph: 1) He took 10 s to accelerate to full speed and he travelled 100 m in that time. 400 2) He travelled at a constant velocity for the next $\widehat{\epsilon}$ 350 10 s and he travelled 200 m in that time. 300 Displacement i $250 -$ 3) He took 5 s to decelerate (by braking) 200 and stop. He travelled 50 m in that time. 150 4) He remained stationary for 5 s at a 100 displacement of 350 m from his starting point. 50 Ω 5) He accelerated in the opposite direction for 5 s. à ۰'n is $\dot{20}$ 25 30° 35 Time (s) You can work out three more details of the motorcyclist's journey: 1) The value of the constant velocity he travelled at between 10 and 20 seconds. velocity = gradient = $\frac{\text{change in displacement}}{\text{change in time}} = \frac{300 - 100}{20 - 10} = \frac{200}{10} = 20 \text{ ms}^{-1}$ 2) His average velocity for the whole journey - found by dividing his overall change in displacement by the journey time. $\text{average velocity} = \frac{\text{final displacement} - \text{initial displacement}}{\text{total time taken}}$ $=\frac{250-0}{35}=\frac{250}{35}=7.142...=7.1$ ms⁻¹ (to 2 s.f.) 3) His average speed for the whole journey - found by dividing his total distance travelled by the journey time. The total distance is the distance travelled in the positive direction (350 m) plus the distance travelled in the negative direction (100 m). average speed = $\frac{\text{total distance travelled}}{\text{total time taken}} = \frac{350 + 100}{35} = 12.85... = 13 \text{ ms}^{-1}$ (to 2 s.f.) Displacements - pretty lousy work experience if you ask me... 1) The displacement-time graph below shows the displacement of a racing car from the start line. a) Is the car accelerating or decelerating between 1 s and 2 s? 200 b) Describe the motion of the Displacement (m) 160 car between 3 s and 6 s. c) What is the velocity of the 120 car between 8 s and 10 s? 80 d) What is the car's average velocity for the entire journey? 40

0

e) What is the car's average speed for the entire journey?

 \ddot{a} 6 8 ġ Time (s)

10 11 12 13 14

9

Velocity-Time Graphs

You can Draw Graphs to Show the Velocity of an Object

You can also draw graphs that show the velocity of an object moving in one dimension.

You can use a velocity-time graph to calculate two things:

- 1) The **distance** the object has moved.
- 2) The acceleration

The Area Under the Line is the Distance Travelled

To find the distance an object travels between two times:

- 1) Draw vertical lines up from the horizontal axis at the two times.
- 2) Work out the area of the shape formed by these lines.
- 3) When you work out the area, you're multiplying time (the horizontal length) by average speed (the average vertical length), so the result is a distance.
- 4) You can work out the area in two ways:
	- Divide the shape into trapeziums, triangles, and/or rectangles and add up the area of each one.

• Or work out how many metres **each grid square** on the graph is worth, then **multiply** by the number of squares under the line. For squares cut by a diagonal part of the line, you'll need to **estimate** the **fraction** of the square that's under the line.

Velocity-Time Graphs

The Gradient of the Line is the Acceleration

The acceleration of an object travelling in one dimension (see page 6) is given by:

Acceleration (in ms⁻²) = $\frac{\text{change in velocity (in ms⁻²)}{\text{time taken (in s)}}$

This is just the gradient of a velocity-time graph. This means that a velocity-time graph of an object's motion has a **negative gradient** when an object is **slowing down** (decelerating).

b) Calculate the total distance travelled shown by each graph.

Adding and Resolving Forces

The Resultant Force is the Sum of All the Forces

- 1) Force is a vector, just like displacement or velocity.
- 2) When more than one force acts on a body, you can add them together in just the same way as you add displacements or velocities.
- 3) You find the resultant force by putting the arrows "tip-to-tail".
- 4) If the resultant force is zero, the forces are balanced.
- 5) If there's a resultant force, the forces are **unbalanced** and there's a **net force** on the object.

You can Resolve Forces just like Other Vectors

- 1) Forces can be in any direction, so they're not always at right angles to each other. This is sometimes a bit awkward for calculations.
- 2) To make an 'awkward' force easier to deal with, you can think of it as two separate forces, acting at right angles to each other. Forces are vectors, so you just use the method on $p.5$.

$F_H = F \cos \theta$ and $F_V = F \sin \theta$

1) Work out the resultant forces on these objects. Are the forces are balanced or unbalanced?

the horizontal. What is the vertical component of the force?

$Section 1 -$ FORCES AND MOTION

Forces and Acceleration

Here are some Examples of Newton's Second Law

EXAMPLE: A car of mass 1250 kg accelerates uniformly from rest to 15 ms⁻¹ in 25 s. What is the resultant force accelerating it?

 $v = 15$ ms⁻¹, $u = 0$ ms⁻¹, $t = 25$ s $a = \frac{v - u}{t}$, so $a = \frac{15 - 0}{25} = 0.60$ ms⁻² Then $F = m \times a = 1250 \times 0.60 = 750$ N

EXAMPLE: A cyclist applies a braking force of 150 N to come to a stop from a speed of 2.5 ms⁻¹ in 2.3 s. What is the total mass of the cyclist and their bike?

 $v = 0$ ms⁻¹, $u = 2.5$ ms⁻¹, $t = 2.3$ s Again $a = \frac{v - u}{t} = \frac{0 - 2.5}{2.3} = -1.086...$ ms⁻²

The acceleration is negative because the cyclist is slowing down $-$ the acceleration and the resultant force are in the opposite direction to the cyclist's motion.

Then
$$
m = \frac{F}{a} = \frac{-150}{-1.086} = 138 = 140
$$
 kg (to 2 s.f.)

(This answer is rounded to 2 s.f. to match the data in the question $-$ see page 1.)

Newton's Third Law - Forces have an Equal, Opposite Reaction

Newton's Third Law says that:

Each force has an equal and opposite reaction force.

This means that if object A exerts a force on object B, then object B must exert an **equal but** opposite force on object A.

For example — when you are **standing up**, you exert a force (your weight) on the floor and the floor pushes back with a force of the same size in the opposite direction. If it didn't you'd just fall through the floor...

Newton was awful at times tables - he was only interested in fours...

- 1) A car pulls a caravan of mass 840 kg. If the car accelerates at 0.50 ms⁻², what force will the caravan experience?
- 2) An apple of mass 0.120 kg falls with an acceleration of 9.81 ms^{-2} . What is the gravitational force pulling it down (its weight)?
- 3) An arrow of mass 0.5 kg is shot from a bow. If the force from the bow-string is 250 N, what is the initial acceleration of the arrow?
- 4) What is the mass of a ship if a force of 55000 N produces an acceleration of 0.275 ms⁻²?
- 5) A train of mass 15 000 kg accelerates from rest for 25 s. If the total force from the engines is 8600 N, what is the train's final velocity?

S_{FCTION} 2 $-$ ENFRGY

Kinetic Energy

Moving Things Have Kinetic Energy

Energy is a curious thing. You can't pick it up and look at it.

One thing's for certain though $-$ if you're **moving** then you have energy.

This movement energy is more properly known as **kinetic energy**,

and there's a formula for working it out:

If a body of mass m (in kilograms) is moving with speed v (in metres per second) then its **kinetic energy** (in joules) is given by:

kinetic energy = $\frac{1}{2} \times$ mass \times speed²

Or, in symbols:

 $E_{\iota} = \frac{1}{2} \times m \times v^2$

Have a look at the following examples, and then try the questions after them.

EXAMPLE: A car of mass 1000 kg is travelling with a speed of 20 ms⁻¹. What is its kinetic energy?

 $E_k = \frac{1}{2} \times m \times v^2$, so $E_k = \frac{1}{2} \times 1000 \times 20^2$ $=$ $\frac{1}{2} \times 1000 \times 400 = 200000 = 2 \times 10^5$

EXAMPLE: A ball has a speed of 2.5 ms⁻¹ and has kinetic energy equal to 0.75 J. What is the mass of the ball?

 $E_{\nu} = \frac{1}{2} \times m \times v^2$ Multiplying both sides by 2 gives $2 \times E_k = m \times v^2$, then dividing both sides by v^2 gives $\frac{2 \times E_k}{2} = m$,

so $m = \frac{2 \times E_k}{v^2} = \frac{2 \times 0.75}{2.5 \times 2.5} = \frac{1.5}{6.25} = 0.24$ kg

$m = 0.015$ kg E_{1} = 1200 J

 $E_{1} = 0.75$ J

 > 2.5 ms⁻¹

Kinetic energy — what you need lots of when you're late for the bus...

1) An arrow of mass 0.125 kg is travelling at a speed of 72.0 ms⁻¹. What is its kinetic energy?

- 2) A ship has kinetic energy equal to 5.4×10^7 J when moving at 15 ms⁻¹. What is its mass?
- 3) A snail of mass 57 g has a kinetic energy of 1.0×10^{-6} J. What is its speed?

Gravitational Potential Energy

Gravitational Potential Energy Depends on Height and Mass

When an object falls, its speed increases. As its speed increases, so does its kinetic energy. Where does it get this energy from?

Answer - from the gravitational potential energy it had before it fell:

If a body of mass m (in kilograms) is raised through a height h (in metres). the gravitational potential energy (in joules) it gains is given by: gravitational potential energy = mass \times gravitational field strength \times height

So, in symbols it reads:

 $E_p = m \times g \times h$

The gravitational field strength, g, is the **ratio** of an object's weight to its mass (in newtons per kilogram, Nkg^{-1}).

At the surface of the Earth, g has an approximate value of 9.81 Nkg⁻¹.

EXAMPLE: An 80.0 kilogram person in a lift is raised 45.0 metres. What is the increase in the person's gravitational potential energy?

 $E_o = m \times g \times h$, so $E_o = 80.0 \times 9.81 \times 45.0 = 35316 = 35300$ J (to 3 s.f.)

EXAMPLE: A mass raised 15.0 metres gains gravitational potential energy equal to 50.0 joules. What is that mass?

 $E_p = 50.0 \text{ J}$

 E_p = 29 400 J

 $m = 725$ kg

 $h = 15.0 m$

 $E_p = m \times g \times h$. Dividing both sides by g and h gives $\frac{E_p}{g \times h} = m$,
so $m = \frac{E_p}{g \times h} = \frac{50.0}{9.81 \times 15.0} = 0.3397... = 0.340$ kg (to 3 s.f.)

EXAMPLE: 725 kilograms of bricks are given 29400 joules of gravitational potential energy. Through what height have they been raised?

 $E_p = m \times g \times h$. Dividing both sides by m and g gives $\frac{E_p}{m \times g} = h$, so $h = \frac{E_p}{m \times g} = \frac{29\,400}{725 \times 9.81} = 4.1337... = 4.13$ m (to 3 s.f.)

Liven up your roasts - pour on some graveytational potential energy...

- 1) How much more gravitational potential energy does a 750 kg car have at the top of a 350 m high hill than at the bottom?
- 2) A crate is raised through 7.00 metres and gains 1715 J of gravitational potential energy. What is the mass of the crate?
- 3) A 65.0 kilogram hiker gains 24 700 joules of gravitational potential energy when climbing a small hill. How high have they climbed?

Conservation of Energy

The Conservation of Energy Applies to Falling Bodies

The principle of conservation of energy states that:

"Energy cannot be created or destroyed — it can only be converted into other forms"

So as long as you ignore air resistance...

...for a **falling** object:

kinetic energy gained (in joules) = gravitational potential energy lost (in joules)

... and for an object thrown or catapulted upwards:

gravitational potential energy gained (in joules) = kinetic energy lost (in joules)

This can be very useful in solving problems. Read through the examples and then have a go at the questions afterwards. (In all the questions, you can ignore air resistance.)

EXAMPLE: An apple of mass 0.165 kilograms falls 2.00 metres from a tree. What speed does it hit the ground at? E_n lost = $m \times g \times h$ = 0.165 \times 9.81 \times 2.00 = 3.2373 J Therefore E_k gained = 3.2373 J. $E_k = \frac{1}{2} \times m \times v^2$. $m = 0.165$ kg¹ Rearranging this gives $v = \sqrt{\frac{2 \times E_k}{m}}$, so $v = \sqrt{\frac{2 \times 3.2373}{0.165}} = 6.264...$ $2.00 m$ $= 6.26$ ms⁻¹ (to 3 s.f.) **EXAMPLE:** A model clown of mass 225 grams is fired straight upwards from a cannon at 10.0 metres per second. How high does it get? $h = 2$ $m = 225$ g = 0.225 kg E_k lost = $\frac{1}{2} \times m \times v^2 = \frac{1}{2} \times 0.225 \times 10.0^2 = 11.25$ J $m = 0.225$ kg Therefore, E_p gained = 11.25 J. $E_p = m \times g \times h$. $v = 10.0$ ms Rearranging this gives $h = \frac{E_p}{m \times g}$, so $h = \frac{11.25}{0.225 \times 9.81}$ $= 5.096... = 5.10$ m (to 3 s.f.)

Today I'm practising conservation of energy — I'm staying in bed all day...

- 1) A gymnast jumps vertically upwards from a trampoline with 2850 J of kinetic energy. They climb to a height of 5.10 m. What is the gymnast's mass?
- 2) A book of mass 0.475 kilograms falls off a table top 92.0 centimetres from the floor. What speed is it travelling at when it hits the floor?
- 3) A bullet of mass 0.015 kilograms is fired upwards at 420 ms⁻¹. What height does it reach?

Work

Work - the Amount of Energy Transferred by a Force

When you move an object by applying a force to it, you are doing work (generally against another force) and **transferring energy**. For example:

- 1) Lifting up a box you are doing work against gravity. The energy is transferred to gravitational potential energy.
- 2) Pushing a wheely chair across a room you are doing work against friction. The energy is transferred to heat and kinetic energy.
- 3) **Stretching** a spring you are doing work against the stiffness of the spring. The energy is transferred to elastic potential energy stored in the spring.

The amount of energy (in joules) that a force transfers is called the **work done**. It's given by:

work done by a force $\frac{1}{x}$ size of force $\frac{1}{x}$ distance the object moves in the direction of (in joules) (in newtons) the force while the force is acting (in metres)

Or. in symbols:

 $W = F \times s$

EXAMPLE: A 5.0 newton force pushes a box 3.0 metres in the same direction as the force. What is the work done by the force?

$$
W=F\times s,
$$
 so $W=5.0\times3.0=15$ J

The Force isn't Always in the Same Direction as the Movement

Sometimes the force acts in a different direction to the object's movement.

of motion For example — when you **pull** on a sledge, the force acts diagonally along the rope but the sledge only moves horizontally. So it's only the **horizontal part** of the force that is doing any work. You need to use some trigonometry to find the work done: horizontal force = $F \cos \theta$

 $W = F \cos \theta \times s$ (See page 12 for more about resolving forces.)

EXAMPLE: A 25 newton force to the north-east pushes an object 15 metres in a northerly direction. What is the work done?

N **NF** $\sqrt{25}$ N

direction of force.

angle, θ

F. on sledge

direction

North-east = 045° , so $F \cos \theta = 25 \times \cos 45^\circ = 17.677...$ N So the work done is $W = F \cos \theta \times s = 17.677... \times 15 = 265.165... = 270$ (to 2 s.f.)

Work is F times s, what a way to make a living...

Use trigonometry to find the part of the force that

acts in the direction of travel (i.e. north).

1) An upwards force of 25 newtons lifts an object 44 metres. What is the work done?

2) A boy pulls a toy cart 2.5 m along the ground. He applies a force of 17 N at an angle of 35° to the horizontal. How much work does he do?

Work

Work Done = Increase in Gravitational and Kinetic Energy

If a force does work on an object, a few things can happen. For example:

The work done can go entirely into the gravitational potential energy of the object:

EXAMPLE: A force does 74 J of work lifting a 3.0 kg cheese $W = m \times g \times h$ straight up. How high is the cheese lifted?

Work done = increase in gravitational potential energy, so: $W = m \times g \times h$, and so $h = \frac{W}{m \times g}$ $h = \frac{74}{3.0 \times 9.81} = 2.514... = 2.5$ m (to 2 s.f.)

The work done can go entirely into the kinetic energy of the object:

EXAMPLE: The same cheese (of mass 3.0 kg) is pushed horizontally along a frictionless surface with a force of 5.7 N over a distance of 12 m. What is its final speed, assuming it was initially at rest?

Work done = increase in kinetic energy, so:

 $F = 5.7 N$ $W = F \times s = \frac{1}{2} \times m \times v^2$, so $v = \sqrt{2 \times \frac{F \times s}{m}}$ $\mathbf{v} = -\mathbf{i} \times \mathbf{s} = \mathbf{v}_2 \times \mathbf{m} \times \mathbf{v}^2$, so $\mathbf{v} = \sqrt{2 \times \frac{r \times s}{m}}$
 $\mathbf{v} = \sqrt{2 \times \frac{5.7 \times 12}{3.0}} = 6.752... = 6.8 \text{ ms}^{-1}$ (to 2 s.f.) $m = 3.0$ kg $s = 12 m$

The work done can go into increasing both the kinetic and the gravitational energy:

EXAMPLE: The same cheese is fired diagonally upwards from a catapult. At its highest point it has climbed 19 m and is moving horizontally at 12 ms⁻¹. How much work was done on the cheese?

Work done = increase in E_k + increase in $E_{n'}$, so: $F \times s = (\frac{1}{2} \times m \times v^2) + (m \times g \times h)$ $=(\frac{1}{2} \times 3.0 \times 12^2) + (3.0 \times 9.81 \times 19.0)$ $= 775.17 = 780$ J (to 2 s.f.)

 $v = 12$ ms⁻¹ $h = 19 \text{ m}$

Work done? No, you need to answer this question first...

- 1) A constant 125 N force lifts a 5.75 kg rocket vertically upwards. When the rocket reaches a height of 2.50 m the force is removed, but the rocket continues to move upwards. Calculate: a) the work done by the force.
	- b) the gain in gravitational potential energy.
	- c) the gain in kinetic energy.
	- d) the upwards speed of the rocket immediately after the force is removed.

Power

Power - the Work Done Every Second

In mechanical situations, whenever energy is converted, work is being done. For example, when an object is **falling**, the force of gravity is doing work on that object **equal** to the **increase** in **kinetic energy** (ignoring air resistance). The rate at which this work is being done is called the power. You can calculate it using:

power (in watts) = **work done** (in joules) \div **time taken** (in seconds)

Or, in symbols:
$$
P
$$

Power is measured in watts.

A watt is equivalent to one joule of work done per second.

EXAMPLE: If 10 joules of work are done in 2 seconds, what is the power?

 $P = W \div t = 10 \div 2 = 5$ W

EXAMPLE: For how long must a 3.2 kilowatt $(3.2 \times 10^3 \text{ watt})$ engine run to do 480 kilojoules (4.8×10^5) joules) of work?

 $P = W \div t$

Multiplying both sides by t gives: $P \times t = W$ Then dividing both sides by P gives: $t = W \div P$

So, $t = W \div P = \frac{4.8 \times 10^5}{3.2 \times 10^3} = 150$ s

EXAMPLE: A force of 125 newtons pushes a crate 5.2 metres in 2.6 seconds. What is the power? (The motion is in the same direction as the force.)

First you need to find the work done (see page 18):

 $W = F \times s = 125 \times 5.2 = 650$

Then use W to find the power:

 $P = W \div t = 650 \div 2.6 = 250$ W

The power of love ain't that special - it's just a lot of work over time...

1) What is the power output of a motor if it does 250 joules of work in 4.0 seconds?

2) If a lift mechanism works at 14 kilowatts, how long does it take to do 91 kilojoules of work?

3) An engine provides a force of 276 N to push an object 1.25 km in 2.5 minutes. What power is the engine working at?

Power

Power is also **Force** Multiplied By Speed

There's a useful equation you can derive for the work done by a force every second on an object moving at a **constant speed**. Follow through the working in the example below:

Mooving forces with a lot of power - a stampeding herd of cows...

- 1) What is the power delivered by a train engine if its driving force of 1.80×10^5 newtons produces a constant speed of 40.0 metres per second?
- 2) A skydiver is falling at a constant velocity of 45 metres per second. Gravity is doing work on her at a rate of 31 500 joules per second. What is her weight?
- 3) A car is travelling at steady speed. Its engine delivers a power of 5.20×10^4 watts to provide a force of 1650 newtons. What speed is the car travelling at (in metres per second)?

Efficiency – getting on with these questions instead of messing about...

- 1) A motor uses 375 joules of electrical energy in lifting a 12.9 kilogram mass through 2.50 metres. What is its efficiency?
- 2) It takes 1.4 megajoules $(1.4 \times 10^6$ joules) of chemical energy from the petrol in a car engine to accelerate a 560 kilogram car from rest to 25 metres per second on a flat road.
	- a) What is the gain in kinetic energy?
	- b) What is the efficiency of the car?

Forces and Springs

Hooke's Law - Extension is Directly Proportional to Force

1) When you apply a force to an object you can cause it to stretch and deform (change shape).

The spring constant, k , depends on the stiffness of the material that you are stretching. It's measured in newtons per metre (Nm⁻¹).

Forces and Springs

Hooke's Law Stops Working when the Force is Great Enough

There's a limit to the amount of force you can apply to an object for the extension to keep on increasing proportionally.

- 1) The graph shows force against extension for a spring.
- 2) For small forces, force and extension are proportional. So the first part of the graph shows a straight-line relationship between force and extension.
- 3) There is a **maximum force** that the spring can take and still extend proportionally. This is known as the limit of proportionality and is shown on the graph at the point marked P .
- 4) The point marked E is the **elastic limit**. If you increase the force past this point, the spring will be permanently stretched. When the force is removed, the spring will be longer than at the start.

5) Beyond the **elastic limit**, we say that the spring deforms **plastically**.

Work Done can be Stored as Elastic Strain Energy

- 1) When a material is stretched, work has to be done in stretching the material.
- 2) If a deformation is **elastic**, all the work done is **stored** as **elastic strain** energy (also called elastic potential energy) in the material.
- 3) When the stretching force is removed, this stored energy is transferred to other forms $-$ e.g. when an elastic band is stretched and then fired across a room. elastic strain energy is transferred to kinetic energy.
- 4) If a deformation is plastic, work is done to separate atoms, and energy is not stored as strain energy (it's mostly lost as heat).

Spring into action - force yourself to learn all this...

- 1) A force applied to a spring with spring constant 64.1 Nm⁻¹ causes it to extend by 24.5 cm. What was the force applied to the spring?
- 2) A pile of bricks is hung off a spring with spring constant 84.0 Nm^{-1} . The bricks apply a force of 378 N on the spring. How much does the spring extend by?
- 3) The mass limit for each bag taken on a flight with Cheapskate Airways is 9.0 kg. The mass of each bag is measured by attaching the bag to a spring.
	- a) A bag of mass 7.4 kg extends the spring by 8.4 cm. What is the spring constant?
	- b) The first bag is removed and another bag is attached to the spring. The spring extends by 9.5 cm. Can this bag be taken on the flight?
- 4) a) What is meant by the limit of proportionality?
	- b) Why might a spring not return to its original length after having been stretched and then released?

 $Section 3 - MATERIAIS$

Current and Potential Difference

Electric Current — the Rate of Flow of Charge Around a Circuit

- 1) In a circuit, negatively-charged electrons flow from the **negative** end of a battery to the **positive** end.
- 2) This flow of charge is called an electric current.
- 3) However, you can also think of current as a flow of positive charge in the other direction, from positive to negative. This is called conventional current.

The electric current at a point in the wire is defined as:

current (in amperes, A) =
$$
\frac{\text{the amount of charge passing the point (in coulombs, C)}}{\text{the time it takes for the charge to pass (in seconds, s)}}
$$

Or, in symbols:

EXAMPLE: 585 C of charge passes a point in a circuit in 45.0 s. What is the current at this point?

$$
I = \frac{Q}{t}
$$
, so $I = \frac{585}{45.0} = 13.0$ A

Potential Difference (Voltage) - the Energy Per Unit Charge

- 1) In all circuits, energy is transferred from the power supply to the components.
- 2) The power supply does work on the charged particles. which carry this energy around the circuit.
- 3) The potential difference across a component is defined as the work done (or energy transferred) **per coulomb** of charge moved through the component.

work done (in joules, I) Potential difference across component (in volts, V) = charge moved (in coulombs, C)

 $V = \frac{W}{Q}$

In symbols:

EXAMPLE: A component does 10.8 J of work for every 2.70 C that passes through it. What is the potential difference across the component?

$$
V = \frac{W}{Q}
$$
, so $V = \frac{10.8}{2.70} =$ **4.00 V**

Physicists love camping trips - they get to study po-tent-ial difference...

- 1) How long does it take to transfer 12 C of charge if the average current is 3.0 A?
- 2) The potential difference across a bulb is 1.5 V. How much work is done to pass 9.2 C through the bulb?
- 3) A motor runs for 275 seconds and does 9540 I of work. If the current in the circuit is 3.80 A, what is the potential difference across the motor?

Current in Electric Circuits

Current flows this wav

Charge is Always Conserved in Circuits

- 1) As charge flows through a circuit, it doesn't get used up or lost.
- 2) You can easily build a circuit in which the electric current can be split between two wires - two lamps connected in parallel is a good example.
- 3) Because charge is conserved in circuits, whatever charge flows into a junction will flow out again.
- 4) Since current is rate of flow of charge, it follows that whatever current flows into a junction is the same as the current flowing out of it.

the sum of the currents going into the junction $=$ the sum of the currents going out

This is Kirchhoff's first law. It means that the current is the same everywhere in a series circuit, and is shared between the branches of a parallel circuit.

5) N.B. - current arrows on circuit diagrams normally show the direction of flow of **conventional current** (see p.25).

EXAMPLE: Use Kirchoff's first law to find the unknown current I_1 .

EXAMPLE: Calculate the missing currents, I_1 and I_2 , in this circuit.

Conserve charge - make nature reserves for circuit boards...

26

Potential Difference in Electric Circuits

Energy is Always Conserved in Circuits

- 1) Energy is given to charged particles by the power supply and taken off them by the components in the circuit.
- 2) Since energy is conserved, the amount of energy one coulomb of charge loses when going around the circuit must be **equal to** the energy it's **given** by the power supply.
- 3) This must be true **regardless** of the **route** the charge takes around the circuit. This means that:

For any closed loop in a circuit, the sum of the potential differences across the components equals the potential difference of the power supply.

This Kirchhoff's second law. It means that:

- In a **series circuit**, the potential difference of the power supply is split between all the components.
- In a **parallel circuit**, each **loop** has the same potential difference as the power supply.

- - a) the voltage across the motor, V_{M} . b) the voltage across the loudspeaker, V_c .
	-
- 2) A third loop containing two filament lamps is added to the circuit in parallel with the first two loops. What is the sum of the voltages of the two filament lamps?

 S_{ECTION} 4 - Electricity

Resistance

Resistance - The Ratio of Potential Difference to Current

- 1) If there's a potential difference across a component a current will flow through it.
- 2) Usually, as the **potential difference** is **increased** the **current increases** this makes sense if you think of the potential difference as a kind of force **pushing** the charged particles.
- 3) You can link current and potential difference by defining "resistance":

potential difference across component (in volts, V) Resistance of component (in ohms, Ω) = current passing through component (in amps, A)

 $R = \frac{V}{A}$

Or. in symbols:

 $V = I \times R$ Multiplying both sides by I gives:

- 4) Components with a **low resistance** allow a **large** current to flow through them. while components with a high resistance allow only a small current.
- 5) The resistance isn't always constant though it can take different values as the current and voltage change, or it can change with conditions like temperature and light level.

EXAMPLE: If a potential difference of 12 V across a component causes a current of 1.0 mA to flow through it, what is the resistance of the component?

$$
R = \frac{V}{I}
$$
, so $R = \frac{12}{1.0 \times 10^{-3}} = 12\ 000\ \Omega$, or 12 k Ω

EXAMPLE: What potential difference must be applied across a lamp with a resistance of 200 Ω in order for a current of 0.2 A to flow through it?

 $V = I \times R$, so $V = 0.2 \times 200 = 40 V$

EXAMPLE: What current will flow through an 850 Ω resistor if a potential difference of 6.3 V is applied across it?

$$
V = I \times R
$$
. Dividing both sides by *R* gives $I = \frac{V}{R'}$,
so $I = \frac{6.3}{850} = 0.007411...$ = **0.0074 A** (or 7.4 mA) (**to 2 s.f.**)

Ohm my, look at that - more questions to do...

- 1) If a current of 2.5 amps flows through a component with a resistance of 15 ohms, what is the potential difference across the component?
- 2) What current will flow through a 2500 Ω resistor if the voltage across it is 6.0 volts?
- 3) What is the resistance of a component if 1.5 volts drives a current of 0.024 amps through it?

I-V Graphs

Ohm's Law Savs Potential Difference is Proportional to Current

- 1) An $I-V$ graph is a graph of current against potential difference for a component. For any $I-V$ graph, the resistance at a given point is the potential difference divided by the current $(R = \frac{V}{I})$.
- 2) Provided the temperature is constant, the current through an ohmic component (e.g. a resistor) is directly proportional to the potential difference across it ($V \propto I$). This is called Ohm's Law.
- 3) An ohmic component's I-V graph is a straight line, with a gradient equal to $1 \div$ the resistance of the component. The **resistance** (and therefore the **gradient**) is **constant**.
	- So for an ohmic component, **doubling** the potential difference doubles the current.
	- Often external factors, such as temperature, will have a significant effect on resistance, so you need to remember that Ohm's law is only true for components like resistors at constant temperature.
- 4) Sometimes you'll see a graph with negative values for p.d. and current. This just means the current is flowing the other way (so the terminals of the power supply have been switched).

EXAMPLE: Look at the *I-V* graph for a resistor on the right. What is its resistance when the potential difference across it is: a) 10 V, b) 5 V, c) -5 V, d) -10 V?

a) $R = \frac{V}{I} = \frac{10}{1} = 10 \Omega$ b) $R = \frac{V}{I} = \frac{5}{0.5} = 10 \Omega$ c) $R = \frac{V}{I} = \frac{-5}{0.5} = 10 \Omega$ d) $R = \frac{V}{I} = \frac{-10}{1} = 10 \Omega$

The I-V graphs for other components don't have constant gradients. This means the resistance changes with voltage.

Lamp

- 1) As the p.d. across a filament lamp gets larger, the filament gets **hotter** and its resistance increases.
- 2) Diodes only let current flow in one direction. The resistance of a diode is very high in the other direction.

Filament $I(A)$ 1

1) State Ohm's law.

2) Sketch I-V graphs for: a) an ohmic resistor. b) a filament lamp, c) a diode.

 $V(V)$

 $I(A)$

 0.5

 -10 -5 -0.5

Diode $I(A)$ 1

 $V(V)$

Power in Circuits

Power - the Rate of Transfer of Energy

- 1) Components in electrical circuits transfer the **energy** carried by electrons into other forms.
- 2) The work done each second (or the energy transferred each second) is the **power** of a component:

work done (in joules, J) **power** (in watts, W) = time taken (in seconds, s)

> $P = \frac{W}{A}$ Or, in symbols:

This is the same as the equation for mechanical power that you saw on page 20.

EXAMPLE: A lift motor does 3.0×10^5 J of work in a single one-minute journey. At what power is it working?

$$
P = \frac{W}{t}
$$
, so $P = \frac{3.0 \times 10^5}{60} = 5000 \text{ W}$ (or 5 kW)

Calculating Power from Current and Potential Difference

The work done is equal to the potential difference across the component multiplied by the amount of charge that has flowed through it ($W = V \times Q$) — see p.25.

So:
$$
P = \frac{V \times Q}{t}
$$

The amount of charge that flows through a component is equal to the current through it multiplied by the time taken $(Q = I \times t)$ - see p.25 again.

So:
$$
P = \frac{V \times I \times t}{t}
$$

Cancelling the t's gives:

$$
P = V \times I
$$

power (in watts) = **potential difference** (in volts) \times **current** (in amps)

EXAMPLE: If the potential difference across a component is 6 volts and the current through it is 0.50 milliamps $(5.0 \times 10^{-4} \text{ amps})$, at what rate is it doing work?

 $P = V \times I$, so $P = 6 \times 5.0 \times 10^{-4} = 0.003$ W (or 3 mW)

Knowledge is power — make sure you know these power equations...

1) What is the power output of a component if the current through it is 0.12 amps when the potential difference across it is 6.5 volts?

- 2) An electric heater has an operating power of 45 W.
	- a) What current passes through the heater when the potential difference across it is 14 volts?
	- b) How much work does the heater do in 12 seconds?

Power in Circuits

You Can Combine the Equations for Power and Resistance

You can **combine** the last equation for the power of an electrical component, $P = V \times I$, with the **equation** for resistance, $R = \frac{V}{I}$ (see p.28), to create two **more useful** equations.

1) Substitute $V = I \times R$ into $P = V \times I$ to get: $P = I \times R \times I = I^2 R$

power (in watts) = $[current (in amps)]^2 \times resistance (in ohms)$

2) Or substitute $I = \frac{V}{R}$ into $P = V \times I$ to get: $P = V \times \frac{V}{R} = \frac{V^2}{R}$

power (in watts) = $\frac{[potential\,difference\,(in\,volts)]^2}{[potential\,differeac\,S(t))^2}$ resistance (in ohms)

Here are some examples — the key here is choosing the right equation to use. If the question gives you the value of two variables and asks you to find a third, you should choose the equation that relates these three variables. You might have to rearrange it before using it.

EXAMPLE: What is the power output of a component with resistance 100 Ω if the current through it is 0.2 A?

$$
P=I^2R
$$
, so $P=0.2^2\times 100=4$ W

EXAMPLE: Resistors get hotter when a current flows through them. If you double the current through a resistor, what happens to the amount of heat energy produced every second?

It increases by a factor of 4 — this is because the current is squared in the expression for the power (you can substitute some values of I and R in to check this).

EXAMPLE: If a lamp has an operating power of 6.5 W and the potential difference across it is 12 V , what is its resistance?

 $P = \frac{V^2}{R}$, so multiplying both sides by R gives $P \times R = V^2$, and dividing by P gives: $R = \frac{V^2}{P}$, so $R = \frac{12^2}{6.5} = 22.153... = 22 \Omega$ (to 2 s.f.) (This answer is rounded to 2 s.f. to match the data in the question — see page 1.)

Watts up with your watch, Dr Watson? Dunno, but it sure is i²rksome...

- 1) What is the power output of a 2400 Ω component if the current through it is 1.2 A?
- 2) A motor has a resistance of 100 Ω . How much work does it do in 1 minute if it is connected to a $6V$ power supply?
- 3) The current through a 6.0 W lamp is 0.50 A. What is the resistance of the lamp?

S_{FCTION} 5 $-$ Waves

Waves

Waves Transfer Energy Without Transferring Matter

- 1) Waves are **oscillations** that transfer energy like water waves or electromagnetic waves.
- 2) Waves carry energy from one place to another without transferring matter.

Transverse Waves Vibrate at 90° to the Direction of Travel

Transverse waves have vibrations at 90° to the direction of energy transfer and travel. E.g. electromagnetic waves (like light) or shaking a Slinky® spring from side to side.

Longitudinal Waves Vibrate Along the Direction of Travel

Longitudinal waves vibrate in the same direction as the direction of energy transfer and travel. They are made of alternate **compressions** and **rarefactions** of the medium. E.g. sound waves or pushing on the end of a Slinky[®] spring.

Amplitude (A) = the largest possible displacement from the equilibrium position **Wavelength** (λ) = the length of one wave cycle, from crest to crest or trough to trough **Period (T)** = the time taken for a whole cycle (vibration) to complete, or to pass a given point

Transverse waves are terrible singers — they always skip the chorus...

- 1) Sketch a graph of displacement against distance for five full wavelengths of a wave with amplitude 0.01 metres and wavelength 0.02 metres.
- 2) Sketch a graph of displacement against time for three complete oscillations of one part of a wave of amplitude 0.05 metres and time period 0.8 seconds.

Frequency and the Wave Equation

Frequency is the Number of Oscillations per Second

If a wave has a **time period** of 0.2 seconds, it takes 0.2 seconds for a point on the wave to complete one full oscillation. So in one second the point will complete 5 full oscillations. The number of oscillations that one point on a wave completes every second is called the **frequency** of the wave. It has the symbol f and is measured in **hertz** (Hz).

So a wave with a time period of 0.2 seconds has a frequency of 5 hertz.

The equation for frequency is:

Frequency =
$$
\frac{1}{\text{time period}}
$$
 or $f = \frac{1}{T}$

EXAMPLE: A wave has a frequency of 350 Hz. What is the period of oscillation of one point on that wave?

$$
T = \frac{1}{f} = \frac{1}{350} = 0.002857... = 0.0029 s (to 2 s.f.)
$$

The Wave Equation Relates Speed, Frequency and Wavelength

For a wave of **frequency** f (in hertz), **wavelength** λ (in metres) and **wave speed** \bf{v} (in metres per second) the wave equation is:

> speed = frequency \times wavelength or $v = f \times \lambda$

EXAMPLE: Sound is a longitudinal wave. If a sound with a frequency of 250 Hz has a wavelength of 1.32 metres in air, what is the speed of sound in air?

 $v = f \times \lambda = 250 \times 1.32 = 330$ ms⁻¹

EXAMPLE: All electromagnetic waves travel at 3.0×10^8 ms⁻¹ in a vacuum. If a radio wave has a wavelength of 1.5 km in a vacuum, what is its frequency?

 $v = f \times \lambda$, so $f = \frac{v}{\lambda} = \frac{3.0 \times 10^8}{1.5 \times 10^3} = 200\ 000\ \text{Hz}$ (or 200 kHz)

Wave equation: lift arm $+$ oscillate hand = pleasant non-vocal greeting...

- 1) A radio wave has a frequency of 6.25×10^5 Hz. What is the time period of the radio wave?
- 2) A sound wave has a time period of 0.0012 s. Find the frequency of the sound.
- 3) A wave along a spring has a frequency of 3.5 Hz and a wavelength of 1.4 m. What is the speed of the wave?
- 4) A wave has time period 7.1 s and is moving at speed 180 ms^{-1} .
	- a) What is the frequency of the wave?
	- b) What is the wavelength of the wave?

Superposition of Waves

Superposition Happens When Two Waves Meet

- 1) If two waves meet (e.g. waves on a rope travelling in opposite directions), their displacements will briefly combine.
- 2) They become one single wave, with a displacement equal to the displacement of each individual wave added together.
- 3) This is called superposition.
- 4) If two crests meet, the heights of the waves are added together and the crest height increases. This is called constructive interference because the amplitude of the superposed waves is larger than the amplitude of the individual waves.
- 5) If the crest of one wave meets the trough of another wave, you subtract the trough **depth** from the crest **height**. So if the crest height is the same as the trough depth they'll cancel out. This is called destructive interference because the amplitude of the superposed waves is smaller than that of the individual waves.
- 6) After combining, the waves then carry on as they were before.

If Waves are In Phase they Interfere Constructively

- 1) Two waves travelling in the same direction are in phase with each other when the peaks of one wave exactly line up with the peaks of the other, and the troughs of one wave exactly line up with the troughs of the other.
- constructive interference 2) If these waves are superposed, they interfere constructively. The combined amplitude of the final wave is equal to the sum of the individual waves.

If Waves are Out of Phase they Interfere Destructively

- 1) Two waves are exactly out of phase if the peaks of one wave line up with the **troughs** of the other (and vice versa).
- 2) If these waves are superposed, they interfere destructively. If the individual waves had the same amplitude originally, they will cancel each other out.

Constructive interference - getting woken up early by noisy builders...

- 1) What is meant by:
	- a) superposition?
	- b) constructive interference?
	- c) destructive interference?
- 2) A wave with an amplitude of 0.67 mm is superposed with an identical wave with the same amplitude. The waves are in phase. What is the amplitude of the superposed wave?
- 3) Two waves, both of amplitude 19.1 m, are exactly out of phase. What is the amplitude of the single wave formed when they superpose?
- 4) A wave with an amplitude of 35 cm is in phase with a 41 cm amplitude wave. The waves meet and constructive interference occurs. What is the amplitude of the combined wave?

In phase.

destructive interference

Reflection and Diffraction

Waves can be Reflected

1) When a wave hits a **boundary** between one medium and another, some (or nearly all) of the wave is reflected back.

- 2) The angle of the **incident** (incoming) wave is called the **angle of incidence**, and the angle of the reflected wave is called the angle of reflection.
- 3) The angles of incidence and reflection are both measured from the normal - an imaginary line running **perpendicular** to the **boundary**.
- 4) The law of reflection says that:

angle of incidence (i) = angle of reflection (r)

Diffraction - Waves Spreading Out

- 1) Waves spread out ('diffract') at the edges when they pass through a gap or pass an object.
- 2) The amount of diffraction depends on the size of the gap relative to the wavelength of the wave. The narrower the gap, or the longer the wavelength, the more the wave spreads out.

Gap the same

Aaximum diffraction

3) A narrow gap is one about the same size as the wavelength of the wave. So whether a gap counts as narrow or not depends on the wave.

- 4) If light is shone at a narrow slit about the same width as the wavelength of the light, the light diffracts.
- 5) The diffracted light forms a diffraction pattern of bright and dark fringes. This pattern is caused by constructive and destructive interference of light waves (see p.34).
	- 6) You get diffraction around the edges of **obstacles** too.
	- 7) The shadow is where the wave is blocked. The wider the obstacle compared to the wavelength, the less diffraction it causes, so the longer the shadow.

Mind the gap between the train and the platform — you might diffract...

- 1) What is the law of reflection?
- 2) Sketch a diagram of a light wave being reflected at an angle by a mirror. Label the incident and reflected waves, the normal, the angle of incidence and the angle of reflection.
- 3) A water wave travels through a gap about as wide as its wavelength. The gap is made slightly larger. How will the amount of diffraction change?
- 4) What happens when light is shone at a slit about the same size as its wavelength?

Refraction

Waves can be Refracted

- 1) Reflection isn't all that happens when a wave meets a boundary. Usually, some of it is refracted too - it passes through the boundary and changes direction.
- 2) Waves travel at different speeds in different media. $E.g.$ \rightarrow electromagnetic waves, like light, usually travel slower in denser media.

If a wave hits a boundary 'face on', it slows down without changing direction.

But if the wave hits at an angle,

this bit slows down first...

...while this bit carries on at the same speed until it meets the boundary. The wave changes direction.

When an electromagnetic wave enters a **denser** medium, it bends **towards** the normal. When one enters a less dense medium, it bends away from the normal.

The Refractive Index is a Ratio of Speeds

The **refractive index** of a medium, n , is the **ratio** of the speed of light in a **vacuum** to the speed of light in that medium. Every transparent material has a refractive index and different materials have different refractive indices.

You can Calculate the Refractive Index using Snell's Law

When an incident ray travelling in air meets a boundary with another material, the angle of refraction of the ray, r, depends on the refractive index of the material and the angle of incidence, i.

You can **rearrange** Snell's Law to find an angle of refraction or incidence, e.g. $r = \sin^{-1}(\frac{\sin i}{n})$.

This page has a high refractive index - it's really slowed me down...

- 1) A wave hits a boundary between two media head on. Describe what happens to the wave.
- 2) A wave hits a boundary between two media at an angle. Describe what happens to the wave.
- 3) A light wave travelling in air hits a transparent material at an angle of 72° to the normal to the boundary. The angle of refraction is 39°. What is the refractive index of the material?
- 4) A light wave hits the surface of the water in a pond at 23° to the normal. The refractive index of the pond water is 1.3. What is the angle of refraction?

Atomic Structure

Atoms are Made Up of Three Types of Particle

- 1) According to the **nuclear model**, the atom is made up of electrons, protons and neutrons.
- 2) The nucleus is at the centre of the atom. It contains protons (which have a positive charge) and neutrons (which have no charge), giving the nucleus an overall positive charge. Protons and neutrons are both known as **nucleons**.
- 3) The nucleus is tiny but it makes up most of the mass of the atom. The rest of the atom is mostly empty space, containing only the negative electrons which orbit around the nucleus.

Atomic Structure can be Represented Using Nuclide Notation

- 1) The proton number (or atomic number), Z , is the number of protons in an atom.
- 2) The nucleon number (or mass number), A, is the total number of protons and neutrons.
- 3) An element can be described by its proton and nucleon numbers:

nucleon number $-AV$ element proton number symbol

For example, lithium has 4 neutrons and 3 protons, so its symbol is $\frac{7}{3}$ Li.

Isotopes are Different Forms of the Same Element

- 1) Isotopes are atoms with the same number of protons but a different number of neutrons.
- 2) This means they have the same proton number, but different nucleon numbers.
- 3) Many isotopes are unstable and give off radiation (see next page).

Radiocarbon dating - what physicists do on Valentine's Day...

- 1) How many protons and neutrons are there in each of the following nuclei? b) $^{239}_{94}Pu$ d) $^{60}_{27}Co$ e) $^{226}_{88}Ra$ a) $^{241}_{95}Am$ $C)$ ${}^{90}_{38}Sr$
- 2) What is an isotope of an element?

SECTION $6 - A$ **TOMS AND RADIOACTIVITY**

 $\frac{131}{531} \rightarrow \frac{131}{511} + \frac{9}{111}$ Proton and nucleon numbers don't change.

You beta learn this radiation stuff - I promise it's not alpha nothing...

- 1) What is an alpha particle made up of?
- 2) Describe what happens during the emission of beta and gamma radiation.
- 3) Complete the following decay equations by filling in any missing radiation symbols, proton numbers or nucleon numbers:

a) ${}^{242}_{94}Pu \rightarrow -U + {}^{4}_{2}o$ b) $-K \rightarrow {}^{40}_{20}Ca + {}^{0}_{-1}3$ c) ${}^{222}_{86}Rn \rightarrow {}^{218}_{84}Po + _$ d) ${}^{14}_{6}C \rightarrow -N + {}^{0}_{-1}3$

SECTION 6 - ATOMS AND RADIOACTIVITY

Planning an Experiment and Collecting Data

Scientists do Experiments to Answer Questions

You need to plan experiments carefully to make sure you get the best results possible:

- 1) Make a **prediction** or **hypothesis** a testable statement about what you think will happen.
- 2) Identify your variables (see below).
- 3) Think about any risks, and how you can minimise them.
- 4) Select the right **equipment** for the $job if you're measuring a time interval in minutes$ you might use a stopwatch, but if it's in milliseconds you may need to get a computer to measure the time for you, as your reaction time could interfere with your results.
- 5) Decide what **data** you need to collect and how you'll do it.
- 6) Write a clear, detailed **method** describing exactly what you're going to do.

You Need to Know What Your Variables Are

A variable is anything that has the **potential to change** in an experiment.

The **independent variable** is the thing you change in an experiment.

The dependent variable is the thing you measure in an experiment.

All the other variables must be kept the same to make it a fair test. These are control variables.

EXAMPLE: An experiment investigates how the height an object is dropped from affects the time it takes to fall. Identify the variables in this experiment.

The **independent variable** is the **height** you drop the object from $-$ it's what you change. The **dependent variable** is the **time** the object takes to $fall - it's what you measure.$ Everything else in the experiment should be **controlled**, so no other variables change. For example, the same object should be used throughout the experiment (so its size and mass don't change), the **conditions** in the room you do the experiment in should be constant, and you shouldn't change your measuring **equipment** halfway through.

Repeating an Experiment Lets You Calculate a Mean

Normally, you'll get a slightly different result every time you do an experiment, due to small random errors you can't control. E.g. - holding your head in a slightly different place each time you take a measurement from a ruler will cause random errors in the length you read off.

You can reduce the effect of these random errors on your results by repeating your experiment and taking an average, or mean, of your results.

To find the mean:

- 1) Add together the results of each repeat.
- 2) Divide this total by the number of repeats you did.

Independent variables – not keen on accepting help...

- 1) A scientist investigates how changing the potential difference across a circuit component affects the current through it. He measures the current three times at each potential difference.
	- a) Identify the independent and dependent variables in this investigation.
	- b) For a potential difference of 4 V, the scientist records currents of 0.13 A, 0.17 A and 0.12 A. Calculate the mean current through the component when the potential difference is 4 V.

 S ECTION 7 – Investigating and Interpreting

Conclusions and Uncertainty

Draw Conclusions that Your Results Support

You should draw a conclusion that explains what your data shows.

- 1) Your conclusion should be limited to what you've **actually done** and found out in your experiment. For example, if you've been investigating how the force applied to a spring affects how much it stretches, and have only used forces between 0 and 5 N, you can't claim to know what would happen if you used a force of 10 N, or if you used a different spring.
- 2) You also need to think about how much you can **believe** your conclusion, by evaluating the quality of your results (see below). If you can't trust your results, you can't form a **strong conclusion**.

You can Never Measure Anything Exactly

- 1) There will always be errors and uncertainties in your results caused by lots of different things, including human error (e.g. your reaction time). The more errors there are in your results, the lower the quality of your data. This will affect the strength of your **conclusion** (see above).
- 2) All measurements will have some uncertainty due to the equipment used. For example, if you measure a length with a ruler, you can only measure it to the nearest millimetre, as that's the smallest difference marked on the ruler's scale. If you measure a length with a ruler as 14 mm you can write this as 14 ± 0.5 mm to show that you could be up to half a millimetre out either way.
- 3) If you have a value without $a \pm sign$, the number of **significant figures** gives you an estimate of the **uncertainty**. For example, 72 ms⁻¹ has 2 significant figures, so without any other information you know this value must be 72 ± 0.5 ms⁻¹ — if the value was less than 71.5 ms⁻¹ it would have been rounded to 71 ms⁻¹, if it was greater than 72.5 ms^{-1} it would have been rounded to 73 ms^{-1} .

Think About How to Improve Your Experiment

You should always think about how your experiment could be improved:

- 1) Did the experiment actually test what it was supposed to? Could you make it more relevant to the question?
- 2) Was there anything you could have done to prevent some of the errors in your results?
- 3) Would different apparatus or a different method have given you better results?

In conclusion, I need a cup of tea...

- 1) A student records how long it takes for a car to stop when the brakes are fully applied. He uses a stopwatch, and gets a measurement of 7.628 ± 0.0005 seconds.
	- a) What is the smallest difference the stopwatch can measure?
	- b) The student says from his result he can accurately report the time taken for the car to stop to 4 significant figures. Is he correct? Explain your answer.

 $N.B. - All numerical answers here have been rounded to$ the same number of significant figures as the given data value with the least number of significant figures (see page 1).

Section 1 - Forces and Motion

Page 2 - Speed, Displacement and Velocity

- $speed = distance + time = 1500 + 210 = 7.142...$ \mathbf{r} $= 7.1$ ms⁻¹ (to 2 s.f.) distance = speed \times time = $(3.0 \times 10^8) \times (8.3 \times 60)$ \overline{z} $= 1.494 \times 10^{11}$
	- $= 1.5 \times 10^{11}$ m (to 2 s.f.)
- $\overline{\mathbf{3}}$ $time = distance \div speed$. 1.5 m = 150 cm, so time = $150 \div 0.24 = 625 = 620$ seconds (to 2 s.f.)
- \overline{A} $t = s + v = (1 \times 1000) + 50 = 20$ s
- $\overline{5}$ $s = v \times t = 7.50 \times 15.0 = 112.5$
	- $= 113$ m south (to 3 s.f.)

Page 3 - Drawing Displacements and **Velocities**

Page 4 - Combining Displacements and **Velocities**

Page 5 - Resolving Vectors

- Horizontal component = $v = v \cos \theta = 12 \times \cos 68$ $=$ 4.495... = 4.5 ms⁻¹ (to 2 s.f.) Vertical component = $v_y = v \sin \theta = 12 \times \sin 68$ $= 11.128... = 11 \text{ ms}^{-1}$ (to 2 s.f.)
- $\cos \theta = \frac{V_x}{V}$. Rearranging for θ gives: $\overline{2}$ $\theta = \cos^{-t}(\frac{V_x}{V}) = \cos^{-t} \frac{67}{98} = 46.868...$ $= 47^{\circ}$ (to 2 s.f.)
- Vertical velocity = $v = v \sin \theta = 5.9 \times \sin 23$ $\overline{3}$ $= 2.305... \ ms^{-1}$ Time taken to descend 150 m = $\frac{s}{v_0} = \frac{150}{2.305}$ $= 65.067...$ $= 65$ s (to 2 s.f.)

Page $6 -$ Acceleration

 $u = 12.8$ ms⁻¹ to the left = -12.8 ms⁻¹ $v = 18.3$ ms⁻¹ to the right = +18.3 ms⁻¹ $a = \frac{v - u}{t} = \frac{18.3 - (-12.8)}{22.0} = 1.4136...$ $= 1.41$ ms⁻² to the right (to 2 s.f.) $x - y - u = 4.5 - 1.5 = 16.66 = 17.5$ (to 2 s f)

$$
u = \sqrt{a} = \frac{0.18}{0.18} = 10.00... = 17
$$
 s (to 2 s.1.)

$$
u = v - (a \times t) = 0 - (-0.41 \times 3.7) = 1.517
$$

 $= 1.5$ ms⁻¹ (to 2 s.f.)

Page $7 -$ Acceleration Due To Gravity $t = \frac{V-U}{a} = \frac{-4.9-0}{-9.81} = 0.4994... = 0.50$ s (to 2 s.f.)

 \mathcal{I} $\overline{2}$ $u = v - (a \times t) = -26.5 - (-9.81 \times 2.15) = -5.4085$ $= 5.41 \text{ ms}^{-1}$ downwards (to 3 s.f.) $\overline{3}$ $v = u + (a \times t) = 0 + (-9.81 \times 10.0) = -98.1$ $= 98.1$ ms⁻¹ down $t = \frac{V - U}{a} = \frac{-24.5 - 0}{-9.81} = 2.4974... = 2.50$ s (to 3 s.f.) $\overline{4}$ \mathbf{r} $u = v - (a \times t) = -10.7 - (-9.81 \times 1.90) = 7.939$ $= 7.94 \text{ ms}^{-1}$ up (to 3 s.f.)

Page 9 - Displacement-Time Graphs

- 1 a) It is accelerating (towards the start line).
- b) Between 3 and 4 seconds it is moving towards the start line and decelerating until it is stationary. It travels 20 metres in this time. Between 4 and 6 seconds it remains stationary zero metres from the start line. 1100 $401 - 130$ 1.6 and 1.6 and 1.6

$$
= 120 \div 2 = 60 \text{ ms}^{-1}
$$

= 120 \div 2 = 60 \text{ ms}^{-1}

- d) Average velocity = $(180 80) \div 14 = 100 \div 14$ $= 7.1428... = 7$ ms⁻¹ (to 1 s.f.)
- e) Average speed = $(80 + 180) \div 14 = 260 \div 14$ $= 18.571... = 20$ ms⁻¹ (to 1 s.f.)

Page 11 - Velocity-Time Graphs

1 a)
$$
A (0 s \cdot 10 s)
$$
, acceleration = $\frac{10-6}{10-0} = \mathbf{0.4 \, \text{m s}^2}$,
\n $B (10 s \cdot 20 s)$, acceleration = $\frac{10-10}{20-10} = \mathbf{0 \, \text{m s}^2}$,
\n $C (20 s \cdot 30 s)$, acceleration = $\frac{2-10}{30-20} = -0.8 \, \text{m s}^{-2}$
\nb) $A (0 s \cdot 10 s)$, area = $16(6 + 10) \times 10 = 80 \, \text{m}$
\n $B (10 s \cdot 20 s)$, area = $10 \times 10 = 100 \, \text{m}$
\n $C (20 s \cdot 30 s)$, area = $10 \times 10 = 100 \, \text{m}$
\nTotal distance traveled = $80 + 100 + 60 = 240 \, \text{m}$

- 2 a) A (0 s-3 s), acceleration = $\frac{15-0}{3-0}$ = 5 ms⁻² B (3 s-4 s), acceleration = $\frac{10-15}{4-2}$ = -5 ms⁻² C (4 s-6 s), acceleration = $\frac{20-10}{6-4}$ = 5 ms⁻²
	- b) A (0 s-3 s), area = $\frac{1}{2} \times 15 \times 3 = 22.5$ m $B(3 s-4 s)$, area = $\frac{1}{2}(15 + 10) \times 1 = 12.5$ m C (4 s-6 s), area = $\frac{1}{2}$ (10 + 20) × 2 = 30 m Total distance travelled = $22.5 + 12.5 + 30 = 65$ m

Page 12 - Adding and Resolving Forces

1 a) $8-5=3$ N to the right, forces are unbalanced. b) $700 - 200 = 500$ N to the left, forces are unbalanced. $c)$ 2 – 2 = 0 N, forces are balanced.

Page 14 - Forces and Acceleration

- $\mathbf{1}$ $F = m \times a = 840 \times 0.50 = 420 N$
- $\overline{\mathbf{z}}$ $F = m \times a = 0.120 \times 9.81 = 1.1772$
- $= 1.18 N$ (to 3 s.f.)
- $\overline{3}$ $a = F + m = 250 + 0.5 = 500$ ms⁻²
- \overline{A} $m = F + a = 55000 + 0.275 = 200000 \text{ kg}$
- $a = F + m = 8600 + 15000 = 0.573...$ ms⁻²
 $a = \frac{V U}{t}$, so $v = u + (a \times t) = 0 + (0.573... \times 25)$ $\overline{5}$ $= 14.333... = 14 \text{ ms}^{-1}$ (to 2 s.f.)

 $\overline{\mathbf{3}}$

$= 141$ \bar{I} (to 3 s.f.) c) Work done = increase in E_i + increase in E_i so: $E_k = W - E_p = 312.5 - 141.01... = 171.48...$ $= 171 \int (to 3 s.f.)$ d) $v = \sqrt{\frac{2 \times E_k}{m}} = \sqrt{\frac{2 \times 171.48...}{5.75}} = 7.7230...$ $= 7.72$ ms⁻¹ (to 3 s.f.)

Page 18 - Work

Page $19 - Work$

 $W = F \times s = 25 \times 44 = 1100 J$

 $=$ 35 \int (to 2 s.f.)

Page $20 - Power$

$$
I \qquad P = \frac{W}{t} = \frac{250}{4.0} = 62.5 = 63 \ W \ (to 2 \text{ s.f.})
$$

- $t = \frac{W}{P} = \frac{91 \times 1000}{14 \times 1000} = \frac{91000}{14000} = 6.5$ s $\overline{\mathcal{L}}$
- $W = F \times s = 276 \times (1.25 \times 1000) = 3450001$ 3 $P = \frac{W}{t} = \frac{345000}{2.5 \times 60} = 2300 \text{ W}$

Page 21 - Power

$$
P = F \times v = 1.80 \times 10^5 \times 40.0
$$

= **7.20 × 10⁶ W** (or 7.20 MW)

The skydiver's weight is equal to the force, F, exerted by $\overline{2}$ gravity on her mass, so:

$$
F = \frac{P}{V} = \frac{31500}{45} =
$$
 700 N

$$
v = \frac{P}{F} = \frac{5.20 \times 10^4}{1650} = 31.515... = 31.5 \text{ ms}^{-1}
$$
 (to 3 s.f.)

1 Useful energy out =
$$
E_2 = m \times g \times h
$$

\n $Efficiency = \frac{useful energy \times h}{total energy} = \frac{1}{2} \times 9.81 \times 2.50 = 316.3725 \text{ J}$
\n $Efficiency = \frac{useful energy \times 100\%}{total energy \times 100\%} = 84.366 = 84.4\%$
\n2 a) $E_k = \frac{1}{2} \times m \times v^2 = \frac{1}{2} \times 560 \times 25^2 = 1.75 \times 10^5$
\n= 1.8 x 10² J (or 180 k) (to 2 s.f.)
\nb) $Efficiency = \frac{useful energy \times 100 \times 25}{total energy \times 100\%} = \frac{1.75 \times 10^5}{2} \times 100\% = 12.5$

$$
= 13\% (to 2 s.f.)
$$

Section 3 - Materials

Page 24 - Forces and Springs

 $F = k \times \Delta l = 64.1 \times 0.245 = 15.7045$ $\mathbf{1}$ $= 15.7 N$ (to 3 s.f.)

$$
2 \qquad \Delta l = \frac{F}{L} = \frac{378}{84.0} = 4.50 \, \text{m}
$$

- 3 a) $F = m \times g = 7.4 \times 9.81 = 72.594 N$ $k = \frac{F}{\Delta l} = \frac{72.594}{0.084} = 864.214... = 860$ Nm⁻¹ (to 2 s.f.)
	- b) $F = k \times \Delta l = 864.214... \times 0.095 = 82.100...$ N $m = \frac{F}{g} = \frac{82.100...}{9.81} = 8.369... = 8.4$ kg (to 2 s.f.) Yes, the bag can be taken on the flight.
- 4 a) The maximum force at which an object's extension is still proportional to the force applied to it.
	- b) It could have been stretched bevond its elastic limit.

 \mathbf{I}

 $\overline{2}$

 $\sqrt{3}$

 \mathbf{I}

 $\overline{2}$

 $\overline{3}$

1

 $\overline{2}$

 $\overline{\mathbf{3}}$

 \mathbf{I}

 $\overline{2}$

Section 2 – Energy

Page $15 -$ Kinetic Energy

 $E_v = \frac{1}{2} \times m \times v^2 = \frac{1}{2} \times 0.125 \times 72.0^2 = 324 J$

 $E_k = \frac{1}{2} \times m \times v^2$ so $m = \frac{2 \times E_k}{v^2} = \frac{2 \times 5.4 \times 10^7}{15^2}$

 $v = \sqrt{\frac{2 \times E_k}{m}} = \sqrt{\frac{2 \times 1.0 \times 10^{-6}}{0.057}} = 5.9234... \times 10^{-3}$

 $= 2.6 \times 10^6$ I (to 2 s.f.)

 $m = \frac{E_p}{g \times h} = \frac{1715}{9.81 \times 7.00} = 24.974... =$ **25.0 kg (to 3 s.f.)**

 $h = \frac{E_p}{m \times g} = \frac{24700}{65.0 \times 9.81} = 38.735... = 38.7 \text{ m (to 3 s.f.)}$

 $m = \frac{E_p}{g \times h} = \frac{2850}{9.81 \times 5.10} = 56.964... =$ 57.0 kg (to 3 s.f.) E_n lost = $m \times g \times h$ = 0.475 \times 9.81 \times 0.920 = 4.28697 J

 $= 4.25$ ms⁻¹ (to 3 s.f.)

 E_n lost = E_k gained, so $E_k = \frac{1}{2} \times m \times v^2 = 4.28697$ J $v = \sqrt{\frac{2 \times E_k}{m}} = \sqrt{\frac{2 \times 4.28697}{0.475}} = 4.2485...$

 E_k lost = 1/2 × m × v^2 = 1/2 × 0.015 × 420² = 1323 J \mathcal{E}_p gained = \mathcal{E}_k lost, so $\mathcal{E}_p = m \times g \times h = 1323$ J $h = \frac{E_p}{m \times g} = \frac{1323}{0.015 \times 9.81} = 8990.8...$ $= 9000$ m (to 2 s.f.)

 $W = F \cos \theta \times s = 17 \times \cos 35 \times 2.5 = 34.81...$

1 a) $W = F \times s = 125 \times 2.50 = 312.5 = 313$ **J** (to 3 s.f.)

b) $E_p = m \times g \times h = 5.75 \times 9.81 \times 2.50 = 141.01...$

 $= 5.9 \times 10^{-3}$ ms⁻¹ (or 0.59 cms⁻¹) (to 2 s.f.)

Page 16 - Gravitational Potential Energy $E_n = m \times g \times h = 750 \times 9.81 \times 350 = 2575125$

Page 17 - Conservation of Energy E_k lost = E_p gained = 2850 J

So $E_p = m \times g \times h = 2850 J$

 $= 4.8 \times 10^{5} kg$

ANSWERS

Section 4 - Electricity

Page 25 - Current and Potential Difference

- $I = \frac{Q}{t}$, so $t = \frac{Q}{I} = \frac{12}{20} = 4.0$ s \mathbf{I}
- $V = \frac{W}{Q}$, so $W = V \times Q = 1.5 \times 9.2 = 13.8 V$ $\overline{2}$
- $I = \frac{Q}{t}$, so $Q = I \times t = 3.80 \times 275 = 1045$ C $\overline{\mathbf{3}}$ $V = \frac{W}{Q} = \frac{9540}{1045} = 9.129... = 9.13$ V (to 3 s.f.)

Page 26 - Current in Electric Circuits

 $\overline{1}$ $0.5 = I_1 + 0.2 + 0.05$ $0.5 = I₁ + 0.25$ $I_1 = 0.5 - 0.25$ $I_1 = 0.25 A$ $0.4 + 0.3 + I_2 = 1.3$
 $0.7 + I_2 = 1.3$ $\overline{2}$ $I_2 = 1.\overline{3} - 0.7$ $\hat{I}_{2} = 0.6 A$

Page 27 - Potential Difference in Electric **Circuits**

 $\begin{array}{cc} I & a) & I2 = V_M + 3 \\ & V_M = 12 - 3 \end{array}$ $= 9V$ b) $12 = 6 + 2 + V_5$ $V_s = 12 - 6 - 2$ $=4V$ $12V$ $\overline{2}$

Page 28 - Resistance

 \mathbf{I} $V = I \times R$, so $V = 2.5 \times 15 = 37.5 = 38$ V (to 2 s.f.) $I = \frac{V}{R} = \frac{6.0}{2500} =$ **0.0024 A** (or 2.4 mA) $\overline{2}$ $R = \frac{V}{I} = \frac{1.5}{0.024} = 62.5 = 63 \Omega$ (to 2 s.f.) $\overline{\mathbf{3}}$

Page 29 - I-V Graphs

Provided the temperature is constant, the current though an ohmic component is directly proportional to the potential difference across it $(V = IR)$.

Page 30 - Power in Circuits

- $P = V \times I = 6.5 \times 0.12 = 0.78 W$ \mathcal{I}
- 2 a) $I = \frac{P}{V} = \frac{45}{14} = 3.214... = 3.2$ A (to 2 s.f.) b) $W = P \times t = 45 \times 12 = 540$ I

Page 31 - Power in Circuits

- $P = I^2 R = 1.2^2 \times 2400 = 3456 = 3500$ W (to 2 s.f.) \mathbf{r}
- $P = \frac{V^2}{R} = \frac{6^2}{100} = \frac{36}{100} = 0.36 W$ $\overline{2}$ $W = P \times t = 0.36 \times 60 = 21.6 = 20$ I (to 1 s.f.)
- $R = \frac{P}{I^2} = \frac{6.0}{0.50^2} = 24 \Omega$ 3

Section 5 - Waves

Page 33 - Frequency and the Wave Equation

$$
I = \frac{1}{f} = \frac{1}{6.25 \times 10^5} = 1.60 \times 10^{-6} \text{ s}
$$

\n
$$
2 \qquad f = \frac{1}{f} = \frac{1}{0.0012} = 833.33... = 830 \text{ Hz (to 2 s.f.)}
$$

\n
$$
3 \qquad v = f \times \lambda = 3.5 \times 1.4 = 4.9 \text{ ms}^{-1}
$$

\n
$$
4 \qquad a) \qquad f = \frac{1}{f} = \frac{1}{2.1} = 0.1408... = 0.14 \text{ Hz (to 2 s.f.)}
$$

\n
$$
b) \qquad v = f \times \lambda, \text{ so } \lambda = \frac{V}{f} = \frac{1800}{0.4008...} = 1278
$$

\n
$$
= 1300 \text{ m (to 2 s.f.)}
$$

Page 34 - Superposition of Waves

- 1 a) If two waves meet they will briefly combine and become one single wave, with a displacement equal to the displacement of each individual wave added together.
	- b) When the amplitude of the combined wave is larger than the amplitude of the individual waves.
	- c) When the amplitude of the combined wave is smaller than the amplitude of the individual waves.
- $\overline{2}$ Amplitude = $0.67 + 0.67 = 1.34$ mm
- $\overline{3}$ The waves will cancel each other out completely. so the amplitude will be $0 m$.
- \overline{A} Amplitude = $35 + 41 = 76$ cm

Page 35 - Reflection and Diffraction

Angle of incidence (i) = angle of reflection (r) $\overline{2}$

- $\overline{3}$ When the gap is about the same size as the wavelength, there will be a lot of diffraction. When the gap is made slightly larger, the amount of diffraction will decrease.
- Light diffracts as it passes through the slit and forms a $\overline{4}$ diffraction pattern of light and dark fringes.

Page 36 - Refraction

 $\overline{\mathcal{L}}$

- \mathbf{I} The wave slows down without changing direction.
	- The wave slows down and changes direction.

3
$$
n = \frac{\sin i}{\sin r} = \frac{\sin 72}{\sin 39} = 1.511... = 1.5
$$

 \overline{A} $n = \frac{\sin t}{\sin t}$ so sin $r = \frac{\sin t}{n} = \frac{\sin 2t}{1.3} = 0.3005...$ so $r = sin^{-1} 0.3005... = 17.49... = 17^{\circ}$ (to 2 s.f.)

Section 6 - Atoms and Radioactivity

Page 37 - Atomic Structure

- 1 a) 95 protons, 146 neutrons
	- b) 94 protons, 145 neutrons
	- c) 38 protons, 52 neutrons
	- d) 27 protons, 33 neutrons
	- e) 88 protons, 138 neutrons
- An isotope is a different form of the same $\overline{2}$ element. It has the same number of protons but a different number of neutrons.

Page 38 - Nuclear Radiation

- An alpha particle is made up of two protons and two neutrons.
- $\overline{2}$ In beta radiation a neutron in the nucleus turns into a proton and an electron. The electron is emitted from the nucleus. In gamma radiation high-energy electromagnetic radiation is emitted from the nucleus. There is no

change to the number of protons and neutrons.

- 3 a) $^{242}_{44}Pu \rightarrow ^{238}_{92}U + ^{4}_{20}$
	- b) $^{40}_{19}K \rightarrow ^{40}_{29}Ca + ^{0}_{-1}B$
	- c) ${}^{222}_{86}Rn \rightarrow {}^{218}_{84}Po + {}^{4}_{20}$
	- d) ${}^{14}C \rightarrow {}^{14}N + {}^{0}_{-1}B$

Section 7 - Investigating and Interpreting

Page 39 - Planning an **Experiment and Collecting Data**

- 1 a) Independent variable: potential difference across the component. Dependent variable: current through the component.
	- b) $(0.13 + 0.17 + 0.12) \div 3 = 0.14 A$

Page 40 - Analysing Your Data

Page 41 - Conclusions and Uncertainty

- 1 a) 0.001 s (or 1 ms)
	- b) No. There will be some human error in the result caused by the student's reaction time.