

Sharing

12 shared into 3 equal groups

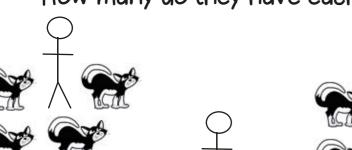
 $12 \div 3 = 4$

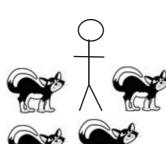
Grouping

How many groups of 3 are there in 12?

There are 12 cats.

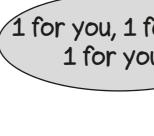
Three people each have the same number of cats. How many do they have each?

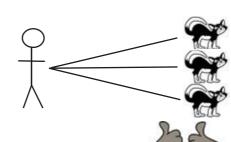


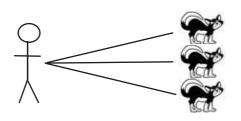


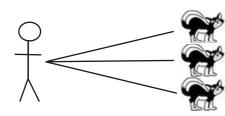
1 for you, 1 for you, 1 for you...

There are 12 cats. Each person owns 3 cats. How many people are there?

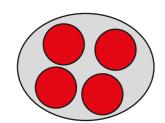


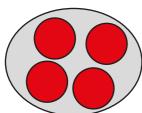


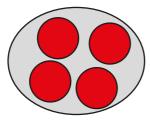




How shall I divide?







Bar model









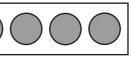


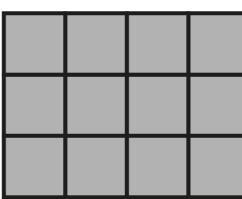
12

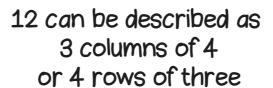


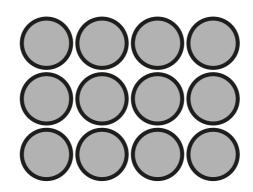


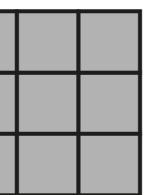




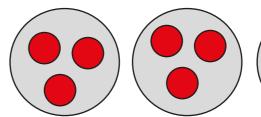


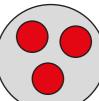


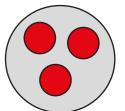


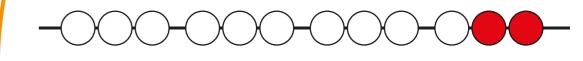


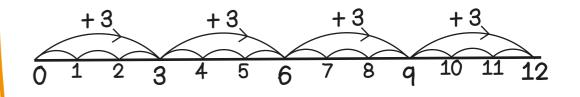
Grab a group of 3 grab a group of 3



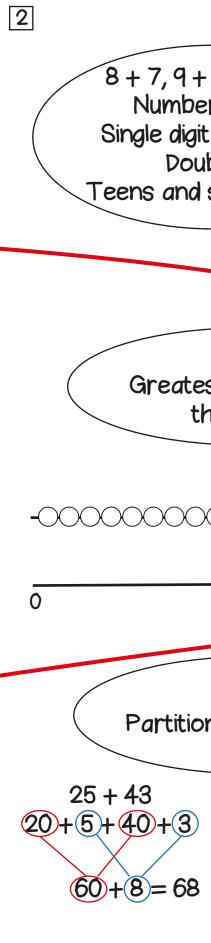












8 + 7, 9 + 9, 14 + 3

Number facts

Single digit numbers

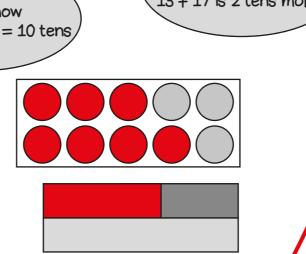
Doubles

Teens and single digits

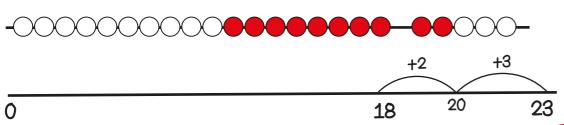
13 + 17
Use known facts
30 + 70

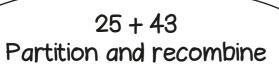
If I know 3 + 7 = 10
then I know
then I know
3 tens + 7 tens = 10 tens

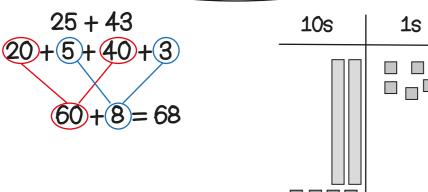
5 + 18 Greatest number first then bridge

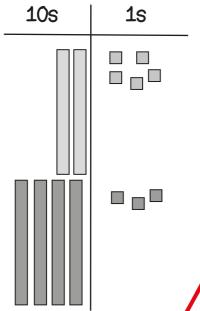


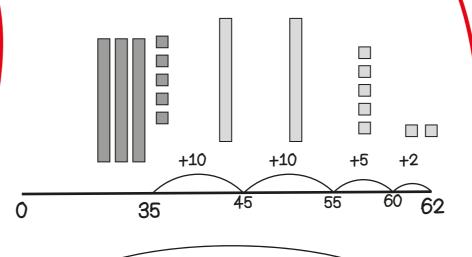
How shall I add?



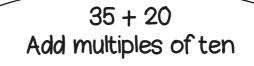


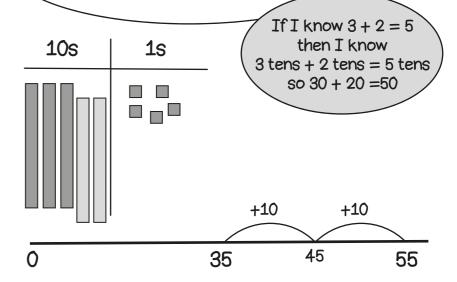


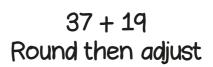


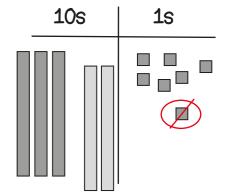


35 + 27 Count on in tens then ones

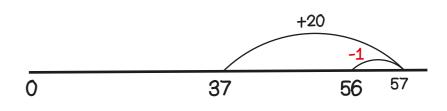








Add 20 then subtract 1



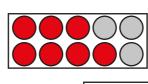


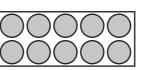


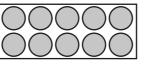
9 - 4, 13 - 5, 18 - 9 Number facts Single digit numbers Halves Teens and single digits I just knew it!

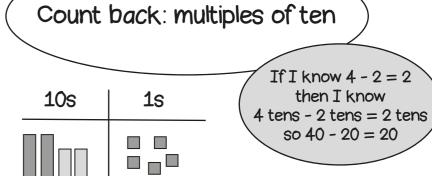
30 - 7 Use known facts 100 - 70

If I know 10 - 7 = 3then I know 30 - 7 is 2 tens and 3

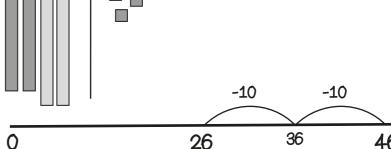




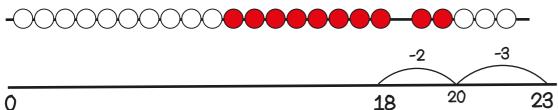


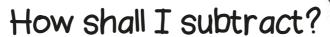


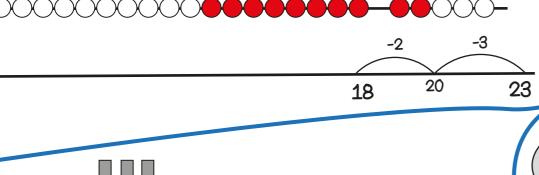
46 - 20



23 - 5Count back: bridge through a multiple of ten







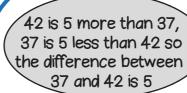
-10

55

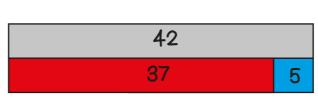
55 - 24

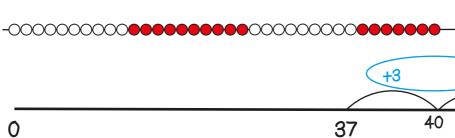
Count back in tens then ones

31

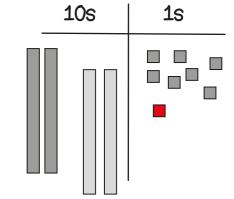


42 - 37 Find the difference between two numbers

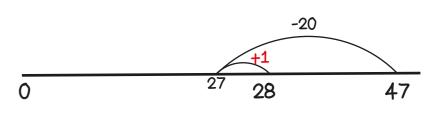




47 - 19 Round then adjust



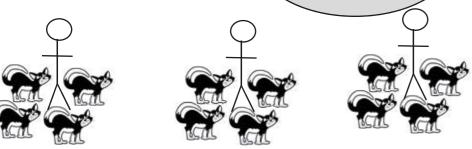
Take away 20 then add 1





Equal groups

There are 3 groups with 4 cats in each group

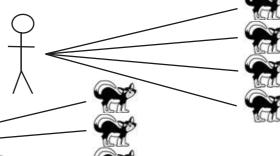


3 people each have 4 cats. How many cats are there in total?

Recall of 2x, 5x and 10x tables

One to many correspondence

If each person has 4 cats, there are 4 times as many cats as people

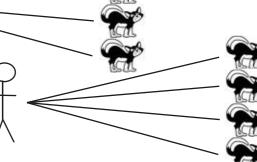




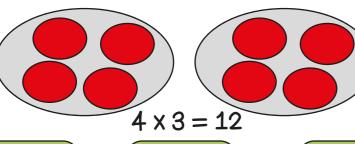


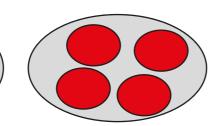




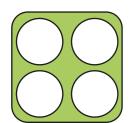


Four cats, multiplied by 3





People Cats 3



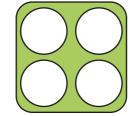




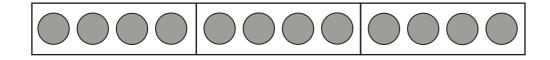
How shall I multiply?











4	4	4
+4	+4	+ 4
0	4 8	12

4 + 4 + 4 = 12

Count in ones

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

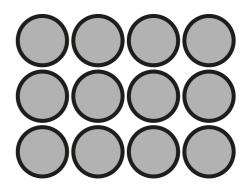
Count in twos

2, 4, 6, 8, 10,12

Use a known fact

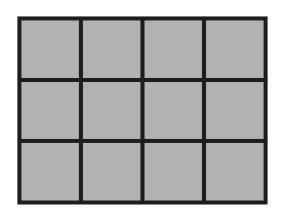
If 2 x 3 is 6, then 4 x 3 is double 6.





 $4 \times 3 = 12$

 $3 \times 4 = 4 \times 3$



Sharing

12 shared into 3 equal groups

 $12 \div 3 = 4$

Recall and use 2x, 5x and 10x tables

How shall I divide?

Grouping

How many groups of 3 are there in 12?

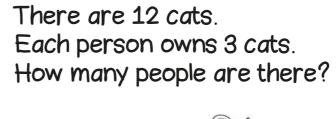
There are 12 cats.

Three people each have the same number of cats.

How many do they have each?

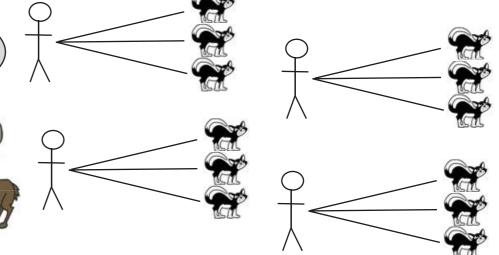


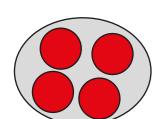
Grab a group of 3 grab a group of 3.

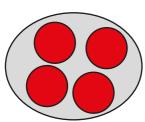


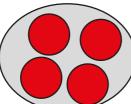


1 for you, 1 for you, 1 for you...

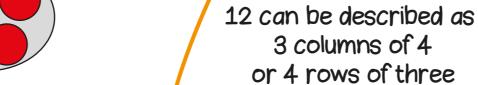


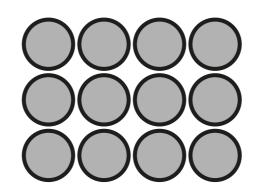


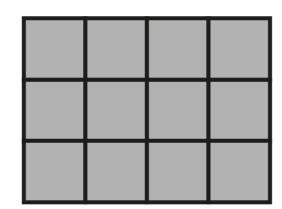


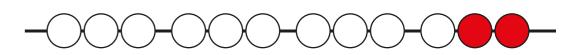


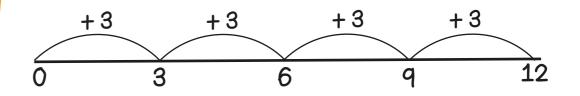
Bar model











If I know $3 \times 4 = 12$ then I know $12 \div 3 = 4$











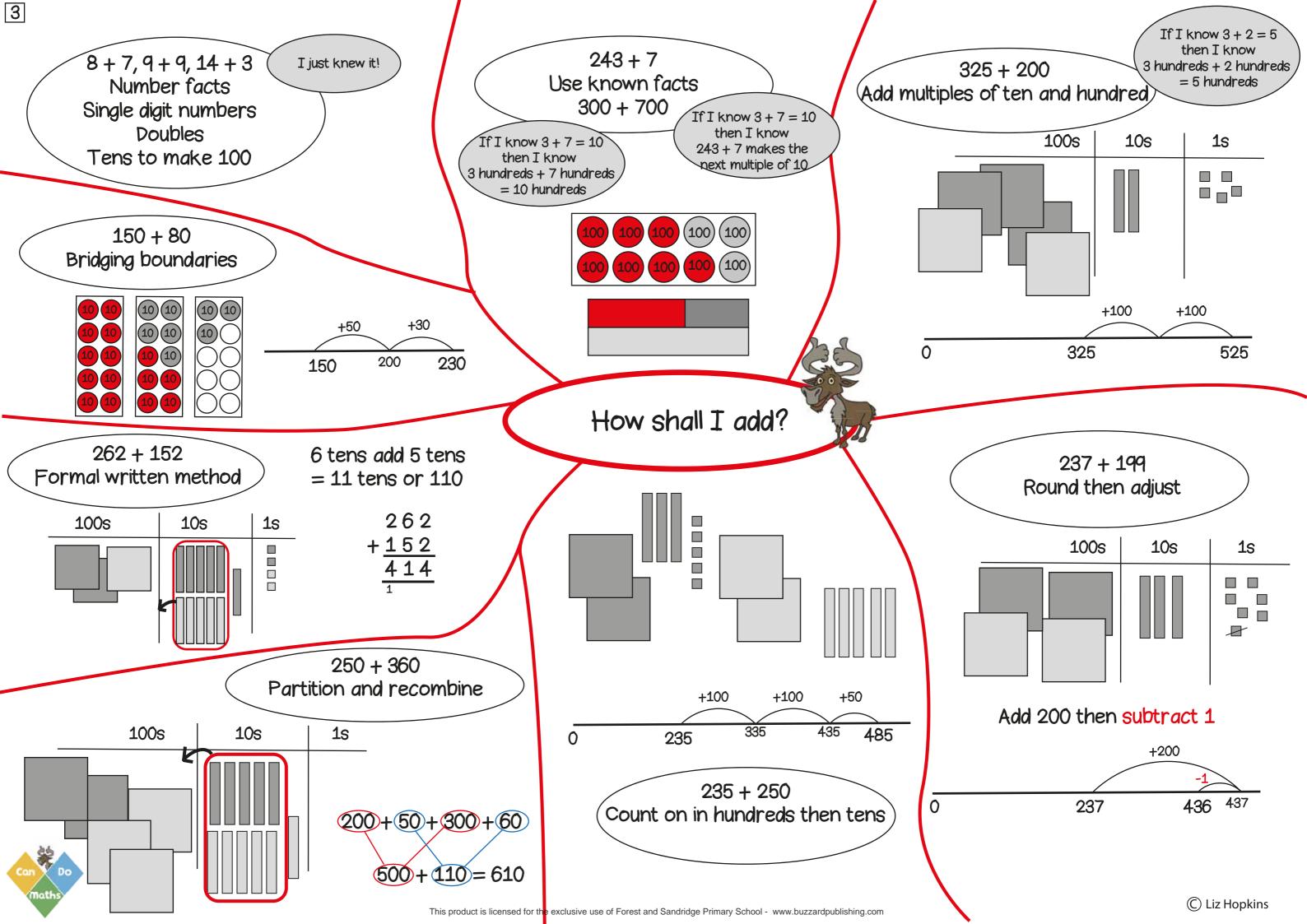




12 4 4

> Link to fractions. One third of 12 is 4







15 - 8, 18 - 5 Number facts Single digit numbers Teens and single digits

230 - 80

Bridging boundaries

by counting back in efficient steps

10 10

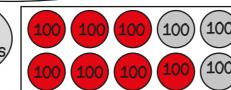
10 10

10 10

I just knew it!

240 - 7 Use known facts 1000 - 700

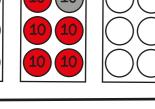
If I know 10 - 7 = 3then I know 10 hundreds - 7 hundreds = 3 hundreds

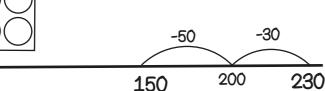


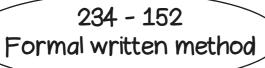
If I know 10 - 7 = 3then I know 3 in the ones.

any multiple of 10, take away 7 leaves

How shall I subtract?

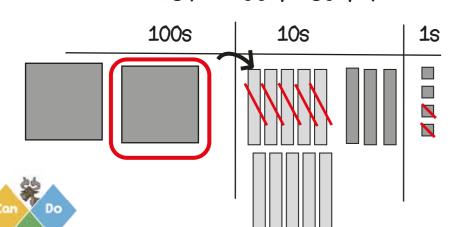


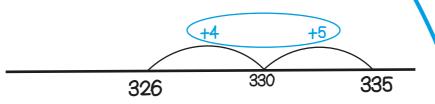




¹2 ¹3 4 -<u>152</u> 182

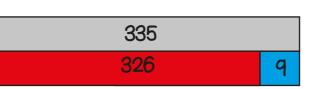
230 - 30 - 50 = 150

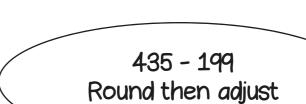




335 - 326 Find the difference between two numbers

> 335 is 9 more than 326 326 is 9 less than 335 so the difference between them is 9





525 - 300

Take away multiples of ten

and a hundred

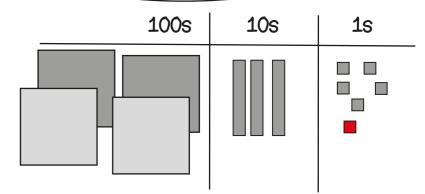
100s

-100

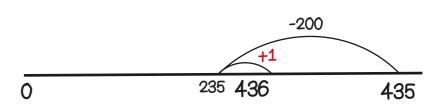
225

10s

-100



Take away 200 then add 1



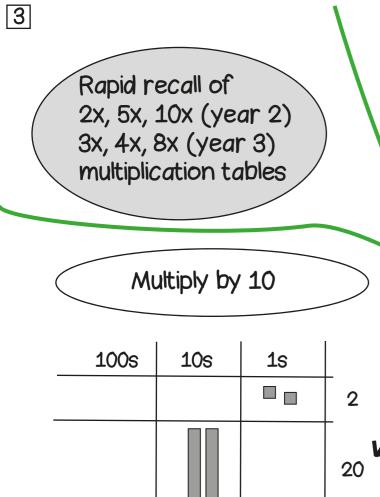
If I know 5 - 3 = 2then I know

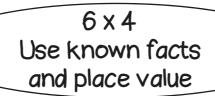
5 hundreds - 3 hundreds

= 2 hundreds

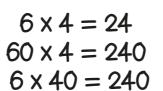
1s

-100

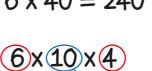




40 is ten times greater than 4

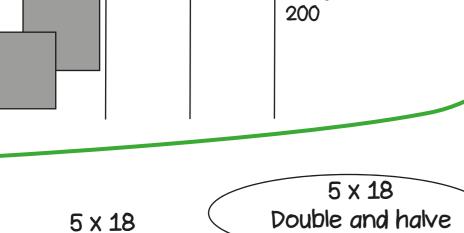




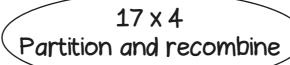


$$=24 \times 10$$

How shall I multiply?

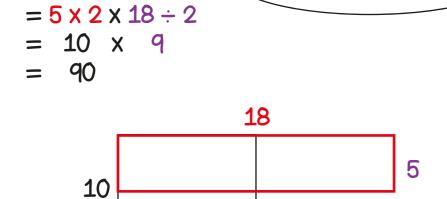


x10

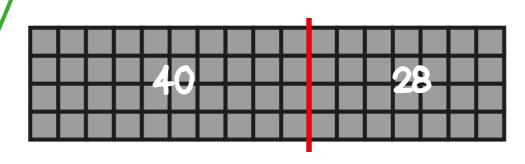


 $10 \times 4 + 7 \times 4$ 40 + 28 = 68





9

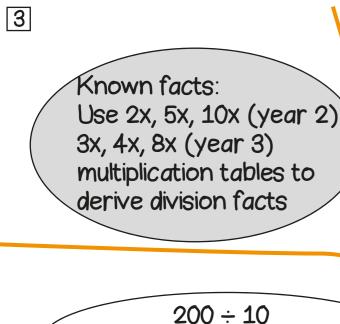


8 x 3 Repeated addition 8+8+8= (3+3+3+3+3+3+3+3 -0000000-000000-000000-0000 0000 0000 0000 0000 8 8 8 +8 +8 16 Arrays If I know 3 x 8 then I know 8 x 3 Scaling The red tower is 3 times taller 24cm than the grey tower 8cm

17 x 4 Formal written method

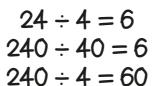
	10	7
4	40	28





24 ÷ 4 Use known facts and place value

240 is ten times greater than 24

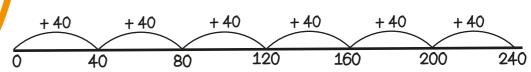


24 biscuits shared between 4 people means they will get 6 biscuits each.

If there are 10 times as many people and 10 times as many biscuits, how many biscuits each now?

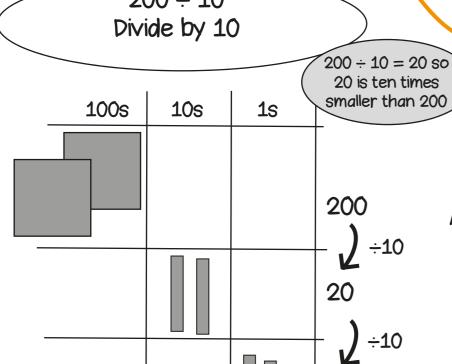


 $240 \div 40 = 6$ How many steps of 40 make 240?



45 ÷ 3

Sharing equally

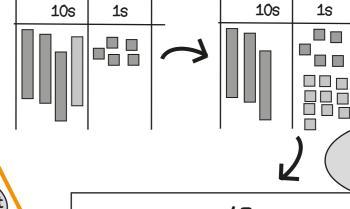


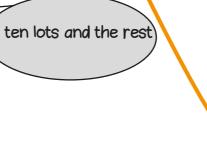
How shall I divide?

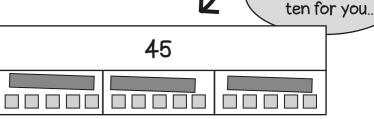
A tenth of ☐ is ☐

A tenth of 1 is 1 tenth so $1 \div 10 = \frac{1}{10}$

52 ÷ 4 Partition and recombine





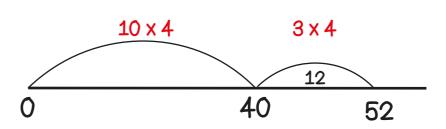


42 ÷ 6 Double and halve If there are half as many biscuits and half as many people...

$$42 \div 6 = 21 \div 3$$

			42		
7	7	7	7	7	7
	21				
7	7	7			

13



Ten for you,

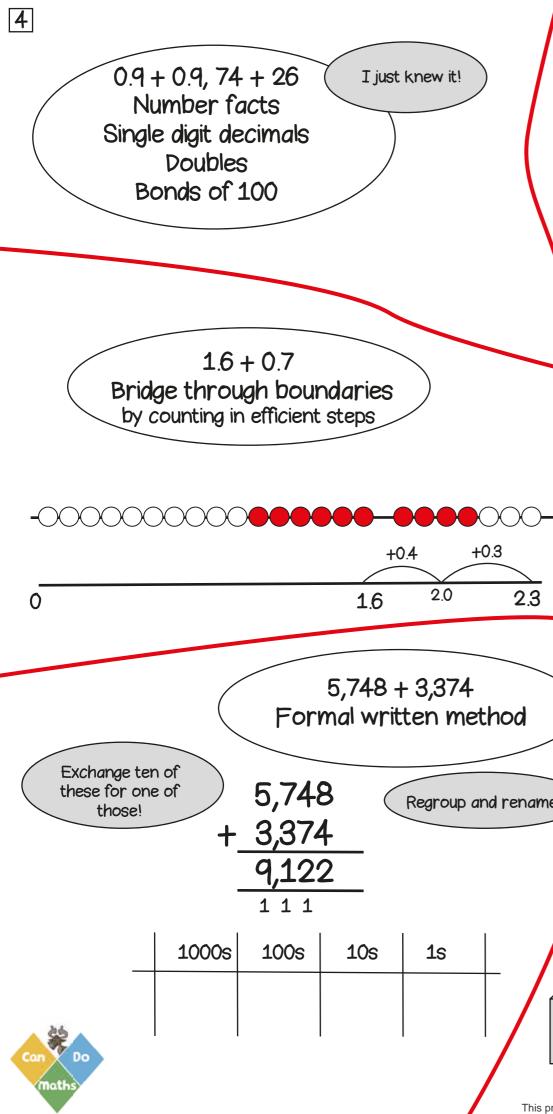
ten for you,

Link to fractions

52 ÷ 4

40

÷4



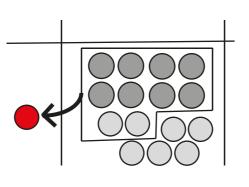
I just knew it!

7 + 8Use known facts

> If I know 7 + 8 = 15then I know 0.7 + 0.8 = 1.5

$$70 + 80 = 150$$

 $700 + 800 = 1,500$



2,403 + 3,020Use place value to add

If I know 2+3=5then I know 2000 + 3000 = 5000

I have noticed, one number has no hundreds or ones, the other has no tens

1000s	100s	10s	1s	
				-

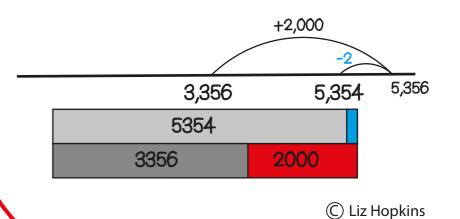
How shall I add?

5,250 + 2,360Partition and recombine

3,356 + 1,998 Round then adjust

1000s	100s	10s	1 s

Add 2,000 then take away 2



5,748 + 3,374 Formal written method

1.6

2.0

+0.3

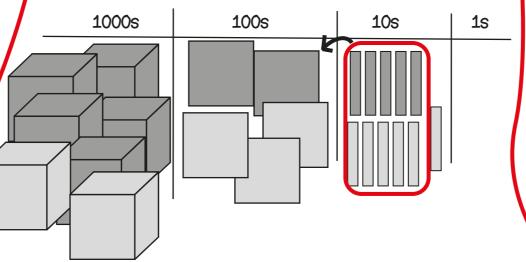
Regroup and rename

2.3

5,748 + 3,374 9,122 1 1 1

1.6 + 0.7

1000s	100s	10s	1 s



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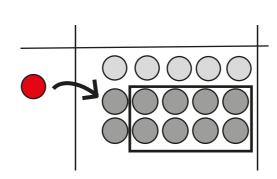
13 - 5, 1.8 - 0.8 Number facts Single digit numbers Halves Wholes and tenths

15 - 8 = 7Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

$$150 - 80 = 70$$

 $1500 - 800 = 700$

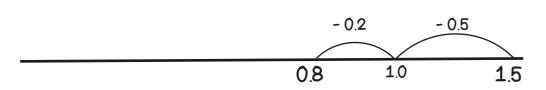


6,342 - 3,020 Use place value to subtract

By using place value counters it is easy to see how to take away

100s 1s 1000s **10s**

1.5 - 0.7Bridge through boundaries by counting in efficient steps



How shall I subtract?

5,352 - 2,136 Formal written method

I just knew it!

Exchange ten of these for one of those!

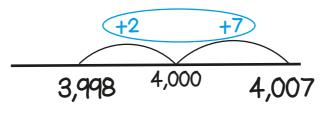
5,352 2,436

Regroup and rename

2,916

1000s	100s	10s	1 s	

4007-3998 Find the difference between two numbers

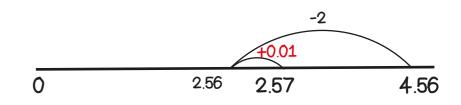


4,007	
3,998	9

4.56 - 1.99 Round then adjust

1 s	$\frac{1}{10}$ S	100 s

Take away 2 then add one hundredth







Known facts: Rapid recall of all multiplication tables up to 12 x 12

6 x 4 Use known facts and place value

 $6 \times 4 = 24$ $60 \times 4 = 240$

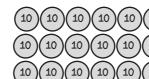
 $60 \times 40 = 2400$



40 is ten times

greater than 4

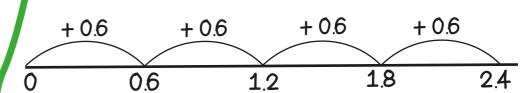
10 10 10 10 10



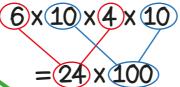
0.6 is ten times smaller than 6

6 x 4 Use known facts and place value

 $0.6 \times 4 = 2.4$ 4 jumps of 0.6



2.34 x 100 Multiply by 10, 100



x10

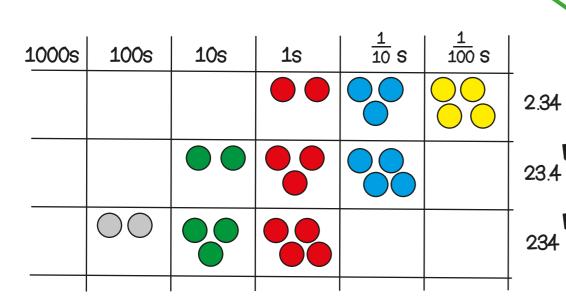
x10

10 10 10 10 10 10 10 10 10 10 10 10 10 10 10

$0.6 \times 4 = 24 \text{ tent}$:hs
$0.6 \times 4 = 2.4$	

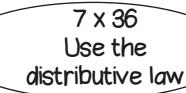
4

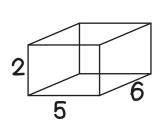
0.6



x100

How shall I multiply?



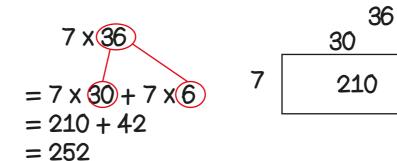


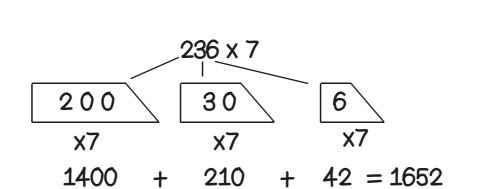
 $2 \times (5 \times 6) = (2 \times 5) \times 6$ $2 \times 30 = 10 \times 6$

45 x 6 $=5\times9\times6$ $=5\times6\times9$ $= 30 \times 9$ = 270

45 x 6 Use factors and commutativity

> Write as factors then re-order





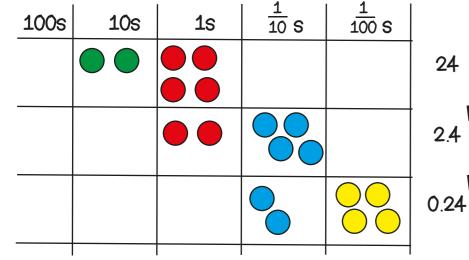
36 x 7 Formal written method

	30	6	36
7	210	42	X 7 252



Known facts:
Use recall of all
multiplication tables
up to 12 x 12 to
derive division facts

 $24 \div 100$ Divide by 10, 100



24 2+10

24 ÷ 4 Use known facts and place value

$$24 \div 4 = 6$$

 $240 \div 40 = 6$
 $2400 \div 400 = 6$

$$2400 \div 400 = \frac{24 \times 100}{4 \times 100}$$
$$\frac{24}{4} = 6$$

÷100

240 is ten times greater than 24

24 biscuits shared between 4 people means they will get 6 biscuits each.

If there are 100 times as many people and 100 times as many biscuits, how many biscuits each now?

60 is ten times greater than 6 2400 ÷ 60 Use known facts and place value

 $2400 \div 60 = 40$ How many steps of 60 make 2400?

10 :	x 60 1	.0 x 60	LO x 60	10 x 60
0	600	1200	1800	2400

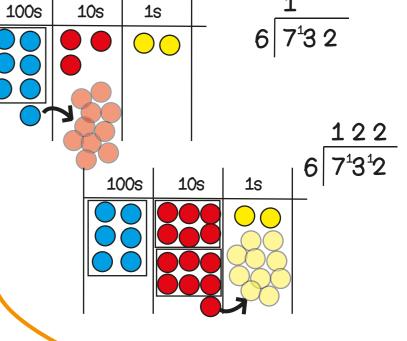
732 ÷ 6

Formal written method

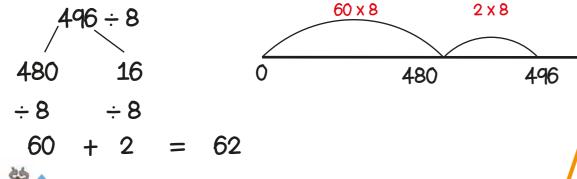
How shall I divide?

516 ÷ 12 Using factors

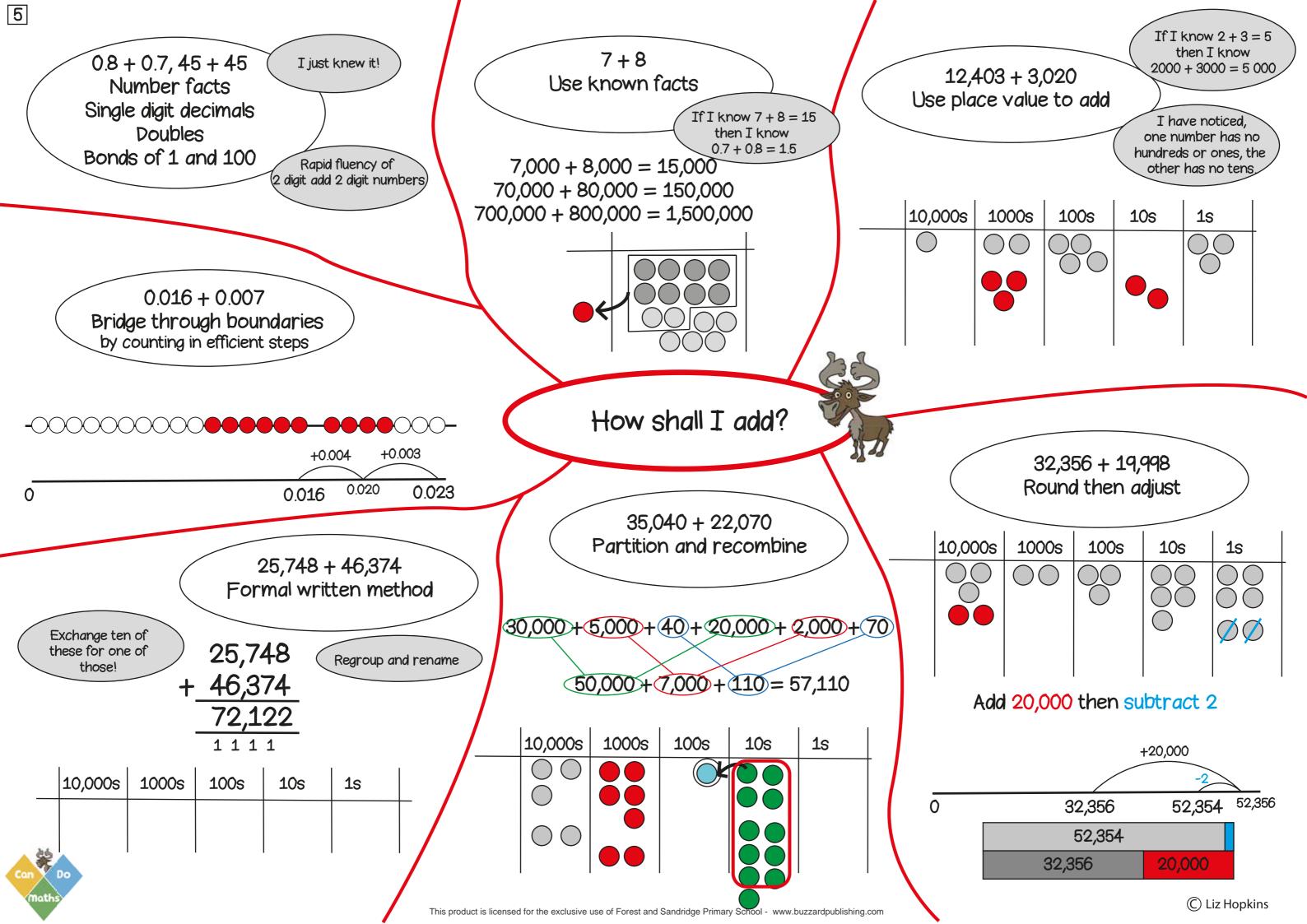
516											
	17	72			17	2		172			
43	43 43 43 43										



496 ÷ 8 Partition and recombine







9-4, 13-5, 18-9 Number facts Single digit decimals Halves

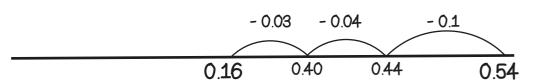
I just knew it!

Subtract from 1 and 100

2 digit numbers

Rapid fluency of 2 digit subtract

0.54 - 0.17Bridge through boundaries by counting in efficient steps



45,748 - 26,374 Formal written method

Exchange ten of these for one of those!

45,748

Regroup and rename

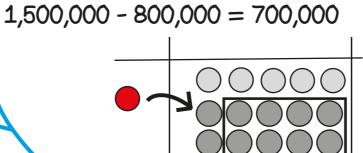
26,374 19,374

 2,000s	1000s	100s	10 s	1s	

15 - 8 = 7Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

15,000 - 8,000 = 7,000 150,000 - 80,000 = 70,000



Use place value to subtract If I know 40 - 3 = 37then I know that 40 thousand take away 3 thousand is 37 thousand

5 less than 12 is 7 Now it is easy to

take away 3000

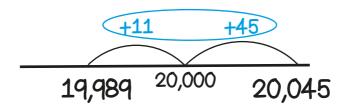
40,000 = 4 tens of thousands or 40 thousands 12 = 1 ten and 2 ones or 12 ones

40,012 = 40 thousands and 12 ones take away 3 thousands and 5 ones equals 37 thousands and 7 ones.

40,012 - 3,005

How shall I subtract?

20,045 - 19,989 Find the difference between two numbers

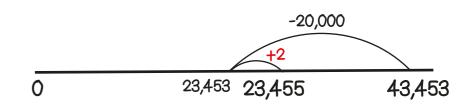


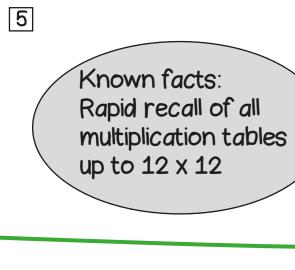
20,045 19,989 56

43,453 - 19,998 Round then adjust

10,000s	1000s	100s	10s	1 s	

Take away 20,000 then add 2



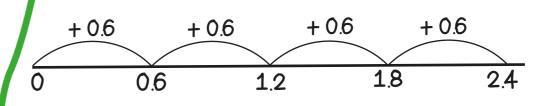


6 x 4 Use known facts and place value

40 is ten times greater than 4





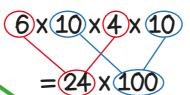


6 x 4

Use known facts

and place value

2.34 x 1000 Multiply by 10, 100, 1000



x10

x10

/ x10

x100

 $6 \times 4 = 24$

 $60 \times 4 = 240$

 $60 \times 40 = 2400$

10 10

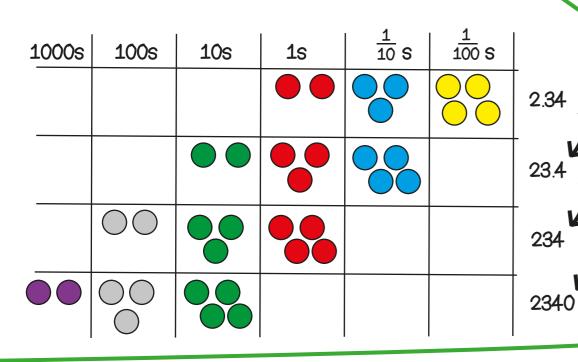
 $0.6 \times 0.4 = 24$ hundredths $0.6 \times 0.4 = 0.24$

 $0.6 \times 4 = 2.4$

4 jumps of 0.6

0.6 is ten times

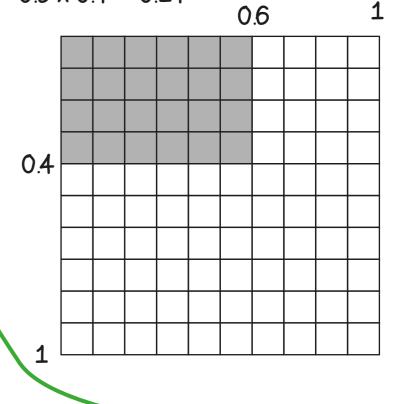
smaller than 6



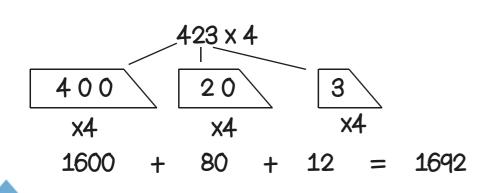
How shall I multiply?

15 x 42 Using factors and distributive law

15 x 48 = 15 x 6 x 8 6 = 90 x 8 = 720



423 x 4 Partition and recombine



15 x 14 = 15 x 6 + 15 x 8 = 90 + 120 = 210

427 x 38 Formal written method

_		400	20	7
3	30	12,000	600	210
-	В	3,200	160	56

427

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Include calcuations where remainders occur

24 ÷ 4 Use known facts

and place value

÷1000

24,000 is a thousand times greater than 24

0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$24 \div 4 = 6$$
 24 biscuits shared between 4 people means they will get

$$240 \div 40 = 6$$
 6 biscuits each.

If there are 1000 times as many people and 1000 times as many biscuits, how many biscuits each now?

+ 0.6+ 0.6 + 0.6 + 0.60.6 1.2

 $2.4 \div 0.6 = 4$

How many steps of 0.6 make 2.4?

24 ÷ 1000 Divide by 10, 100, 1000

Known facts:

Use recall of all

up to 12 x 12 to

multiplication tables

derive division facts

	ea
24,000 ÷ 400 =	= 24 x 1000
	4 × 100
240 =	60

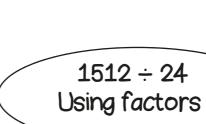
 $2400 \div 400 = 6$

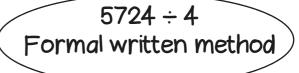
 $24,000 \div 4000 = 6$

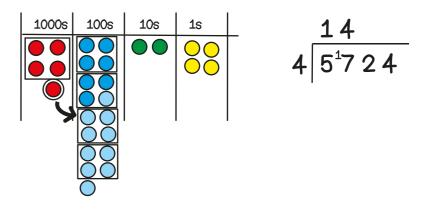
÷10

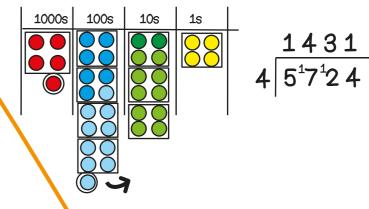
100s	10s	1s	$\frac{1}{10}$ s	100 s	1000s	
						24
						2.4
						0.24
				00	00	0.024

How shall I divide?

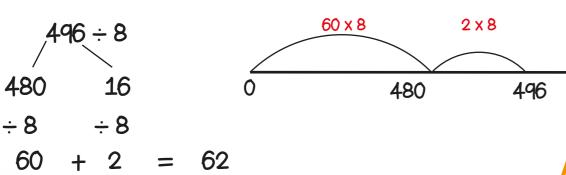


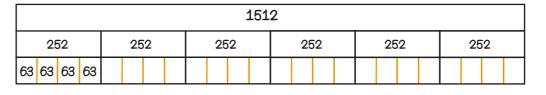






496 ÷ 8 Partition and recombine







44 + 56, 27 + 27Number facts Single digit decimals Doubles Bonds of 1 and 100

I just knew it!

17 + 17Use known facts

1,102,403 + 50,020 Use place value to add

100,000s | 10,000s |

00

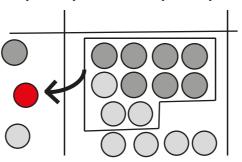
I have noticed. one number has no hundreds or ones, the other has no tens

Rapid fluency of (2 digit add 2 digit numbers)

1.7 + 1.7 = 3.417,000 + 17,000 = 34,000

170,000 + 170,000 = 340,000

1,700,000 + 1,700,000 = 3,400,000



1,000,000s 100,000s 10,000s 1000s 100s 10s 1s $\bigcirc\bigcirc$ 00

0.028 + 0.015Bridge through boundaries by counting in efficient steps

How shall I add?

If I know 17 + 17 = 34

then I know

+0.002 +0.003 0.038 0.040 0.043 0.028

307,040 + 206,070 Partition and recombine

325,748 + 246,374 Formal written method

Regroup and rename

1s

300,000 + 7,000 + 40 + 200,000 + 6,000 + 70

500,000 + 13,000 + 110 = 513,110

these for one of those!	325,748
	246,374
	572 122

1000s

Exchange ten of

100,000s 10,000s

1 1 1 1

100s

10s

Ŀ	100,000s	10,000s	1000s	100s	10s	1 s	
	\bigcirc						
	\bigcirc						
•		l					I

Add 100,000 then take away 1,000

432,356 + 99,000

Round then adjust

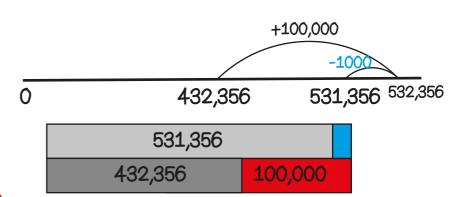
1000s

 $\bigcirc \emptyset$

100s

10s

1s



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0

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0.9 - 0.4, 100 - 65 (Number facts Single digit decimals Halves

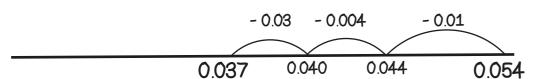
Bonds of 1 and 100

Rapid fluency of 2 digit subtract 2 digit numbers

I just knew it!

0.054 - 0.017

Bridge through boundaries by counting in efficient steps



445,748 - 126,374 Formal written method

Regroup and rename

Exchange ten of these for one of those!

445,748 126,374

+ <u>126,374</u> 319,374

100,000s 10,000s 1000s 100s 10s 1s

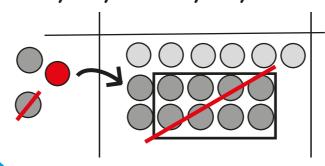
36 - 18 = 18Use known facts

> If I know 36 - 18 = 18 then I know 3.6 - 1.8 = 1.8

36,000 - 18,000 = 18,000

360,000 - 180,000 = 180,000

3,600,000 - 1,800,000 = 1,800,000



400,032 - 30,005 (Use place value to subtract

5 less than 32 is 27

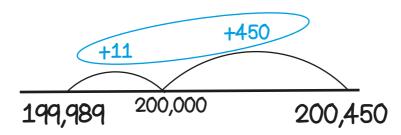
400,000 = 4 hundreds of thousands or 400 thousands

400 - 30 = 370 so 400,000 - 3,000 = 370,000

400,032 = 400 thousands and 32 ones take away 30 thousands and 5 ones = 370,027

How shall I subtract?

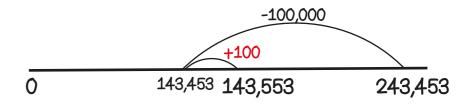
200,450 - 199,989 Find the difference between two numbers



200,450 199,989 461 243,453 - 99,900 Round then adjust

100,000s	10,000s	1000s	100s	10s	1 s	
	00				00	-

Take away 100,000 then add 100





up to 12 x 12

6 x 4 Use known facts and place value

x10

x10

40 is ten times greater than 4

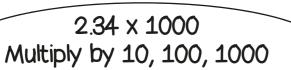
$$60 \times 40 = 2400$$

 $600 \times 400 = 240,000$

6000 x 4000 = 24,000,000

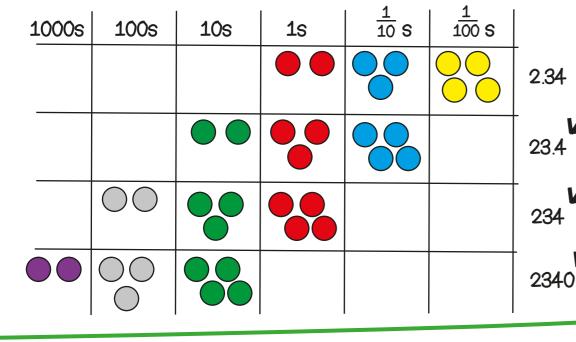
6x10x4x10

x100





How shall I multiply?



4203 x 4

Partition and recombine

4203 x 4

200

x4

12

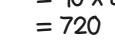
+

16,812

800

15 x 42 Using factors and distributive law

15 x 48 $= 15 \times 6 \times 8$ $= 90 \times 8$





0.6 is ten times

smaller than 6

0.06

0.4

+0.06

 $0.06 \times 4 = 0.24$

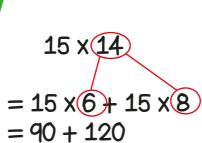
4 jumps of 0.06

0.12

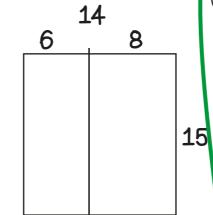
+0.06

 $0.6 \times 0.4 = 24$ hundredths

 $0.6 \times 0.4 = 0.24$



= 210



2427 x 38 Formal written method



6 x 4

Use known facts

and place value

0.18

0.6

+0.06

0.24

1

+ 0.06



4000

x4

16,000

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Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

6

100s

10s

Include calcuations where remainders occur

 $24 \div 4$

Use known facts and place value

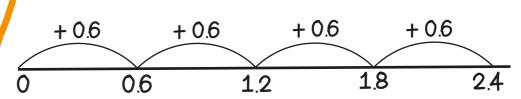
240 is ten times greater than 24

0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?

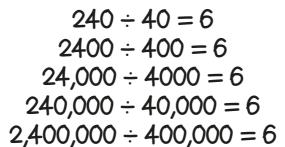


7182 ÷ 21

Formal written method

24 ÷ 1000 Divide by 10, 100, 1000

1s



4 people means they will get 6 biscuits each. If there are 10 times as many people and 10 times as many biscuits, how many biscuits

24 biscuits shared between

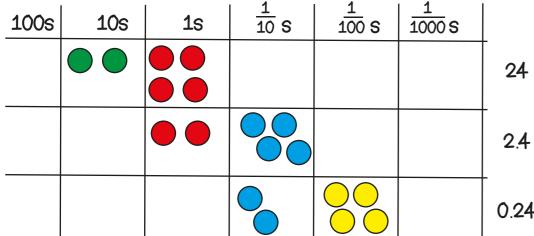
each now?

$$240,000 \div 400 = 24 \times 10,000$$

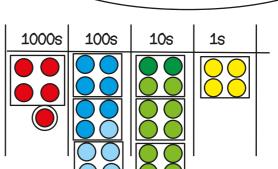
$$4 \times 100$$

$$2400 = 600$$

÷1000



How shall I divide?



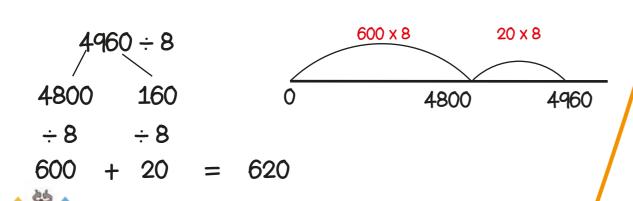
0.24 0.024

÷10

24

1512 ÷ 24 Using factors

4960 ÷ 8 Partition and recombine



 $1512 \div 6 \div 4$

	1512																						
	252 252					25	52			252			252				252						
63	63	63	63																				