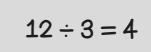


Sharing

12 shared into 3 equal groups

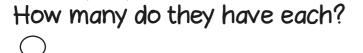


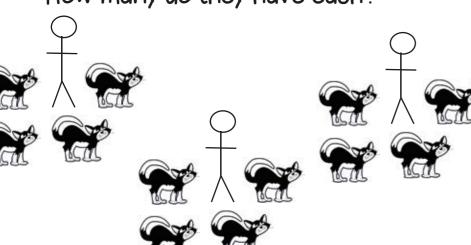
Grouping

How many groups of 3 are there in 12?

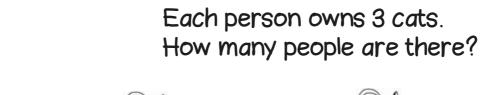
There are 12 cats.

Three people each have the same number of cats.

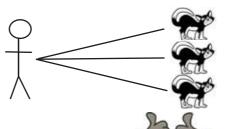


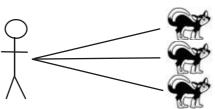


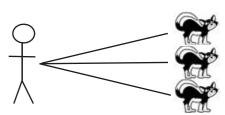
1 for you, 1 for you, 1 for you...



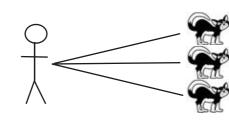
There are 12 cats.



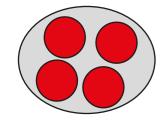


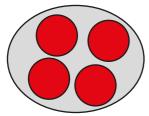


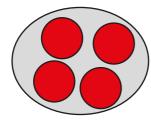
How shall I divide?



Grab a group of 3 grab a group of 3

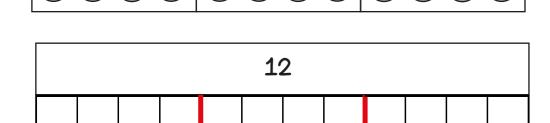


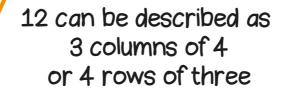


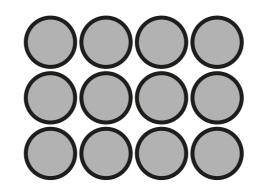


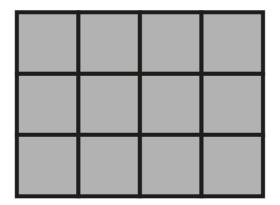
Bar model

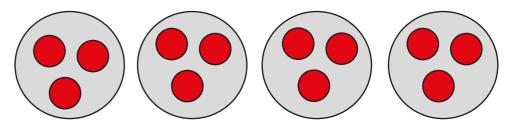


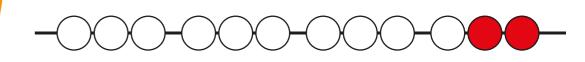


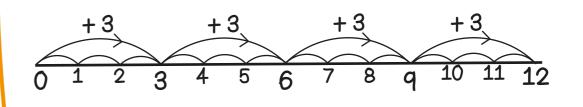




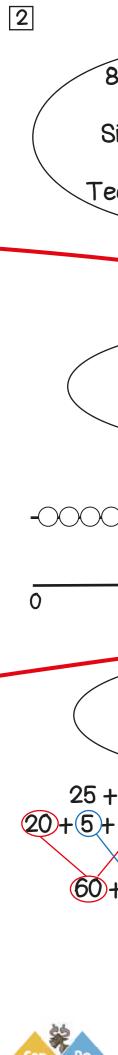












8 + 7, 9 + 9, 14 + 3

Number facts

Single digit numbers

Doubles

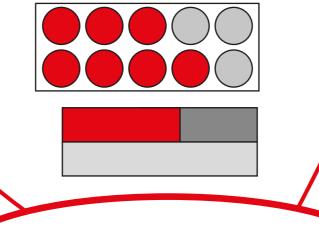
Teens and single digits

13 + 17
Use known facts
30 + 70

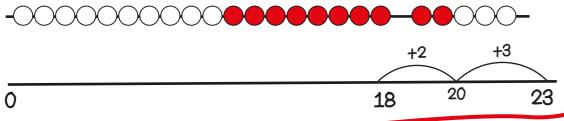
If I know 3 + 7 = 10
then I know
then I know
3 tens + 7 tens = 10 tens

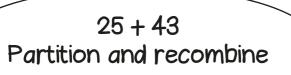
If I know 3 + 7 = 10
then I know
13 + 17 is 2 tens more

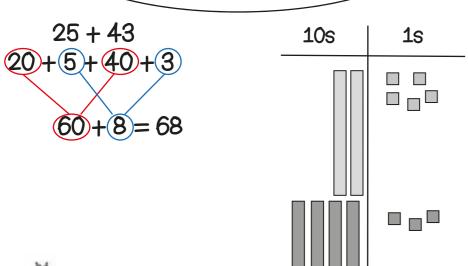
5 + 18 Greatest number first then bridge

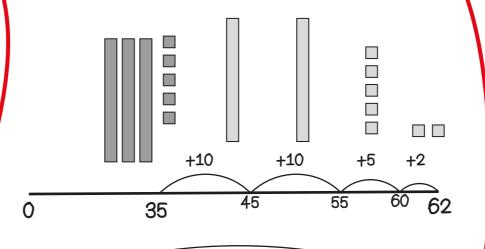


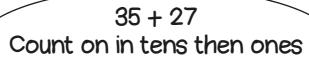




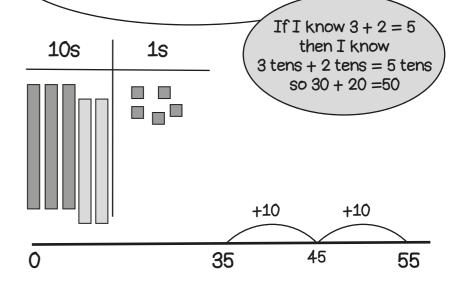


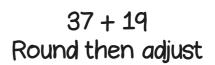


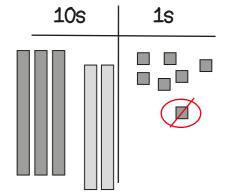




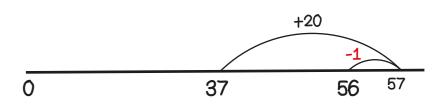
35 + 20 Add multiples of ten







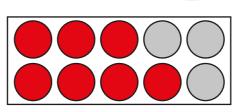
Add 20 then subtract 1



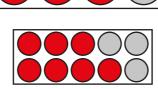


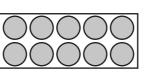
9-4, 13-5, 18-9 Number facts Single digit numbers Halves Teens and single digits I just knew it!

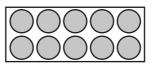
30 - 7 Use known facts 100 - 70



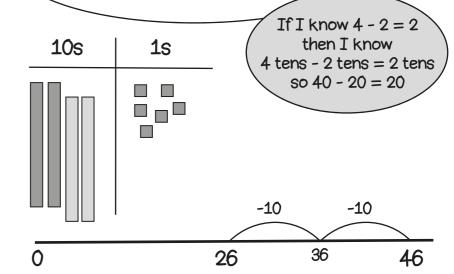
If I know 10 - 7 = 3then I know 30 - 7 is 2 tens and 3



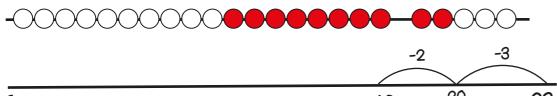




46 - 20 Count back: multiples of ten



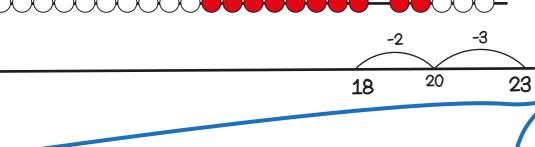
23 - 5Count back: bridge through a multiple of ten



-10

55

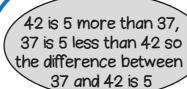
How shall I subtract?



55 - 24

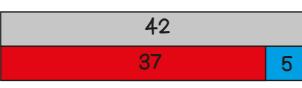
Count back in tens then ones

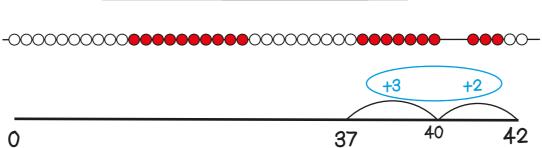
31



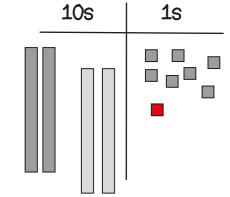
42 - 37

Find the difference between two numbers

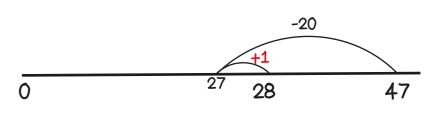




47 - 19 Round then adjust



Take away 20 then add 1

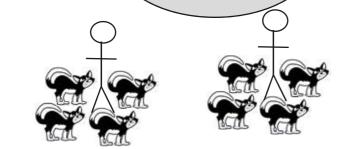




0

Equal groups

There are 3 groups with 4 cats in each group

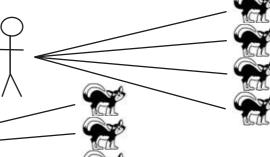


3 people each have 4 cats. How many cats are there in total?

Recall of 2x, 5x and 10x tables

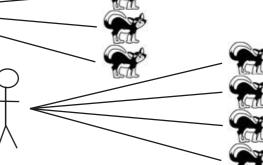
One to many correspondence

If each person has 4 cats, there are 4 times as many cats as people

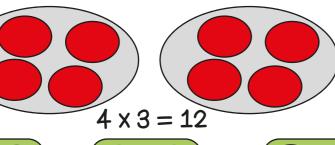


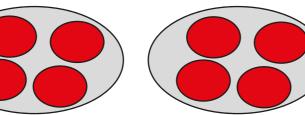






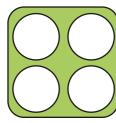
Four cats, multiplied by 3



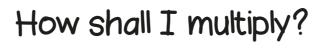


People	Cats
1	4
2	8
3	12
	(Car

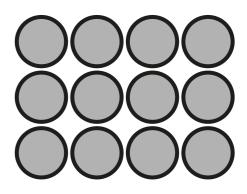








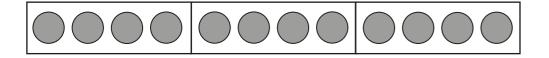




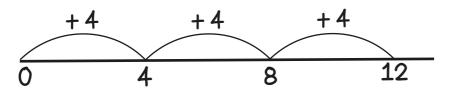
 $4 \times 3 = 12$ 

 $3 \times 4 = 4 \times 3$ 

#### Repeated addition



4	4	4



4 + 4 + 4 = 12

#### Count in ones

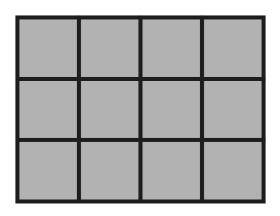
1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

Count in twos

2, 4, 6, 8, 10,12

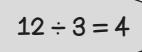
Use a known fact

If 2 x 3 is 6, then 4 x 3 is double 6.



Sharing

12 shared into 3 equal groups



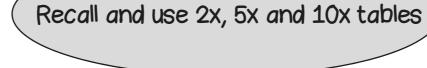
Grouping

How many groups of 3 are there in 12?

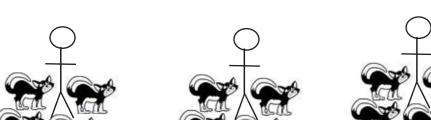
There are 12 cats.

Three people each have the same number of cats.

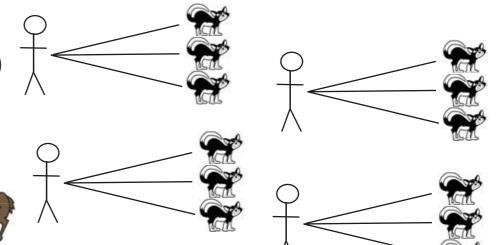
How many do they have each?



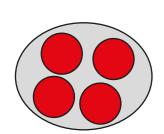
There are 12 cats. Each person owns 3 cats. How many people are there?

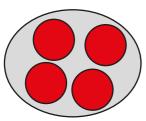


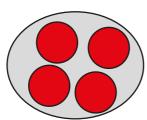
1 for you, 1 for you, 1 for you... Grab a group of 3, grab a group of 3...



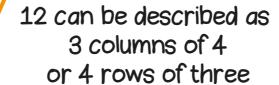
How shall I divide?

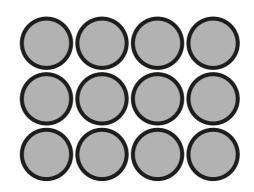


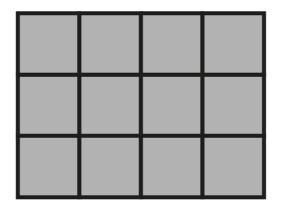




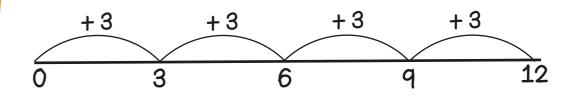
Bar model



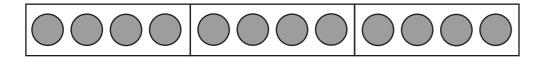








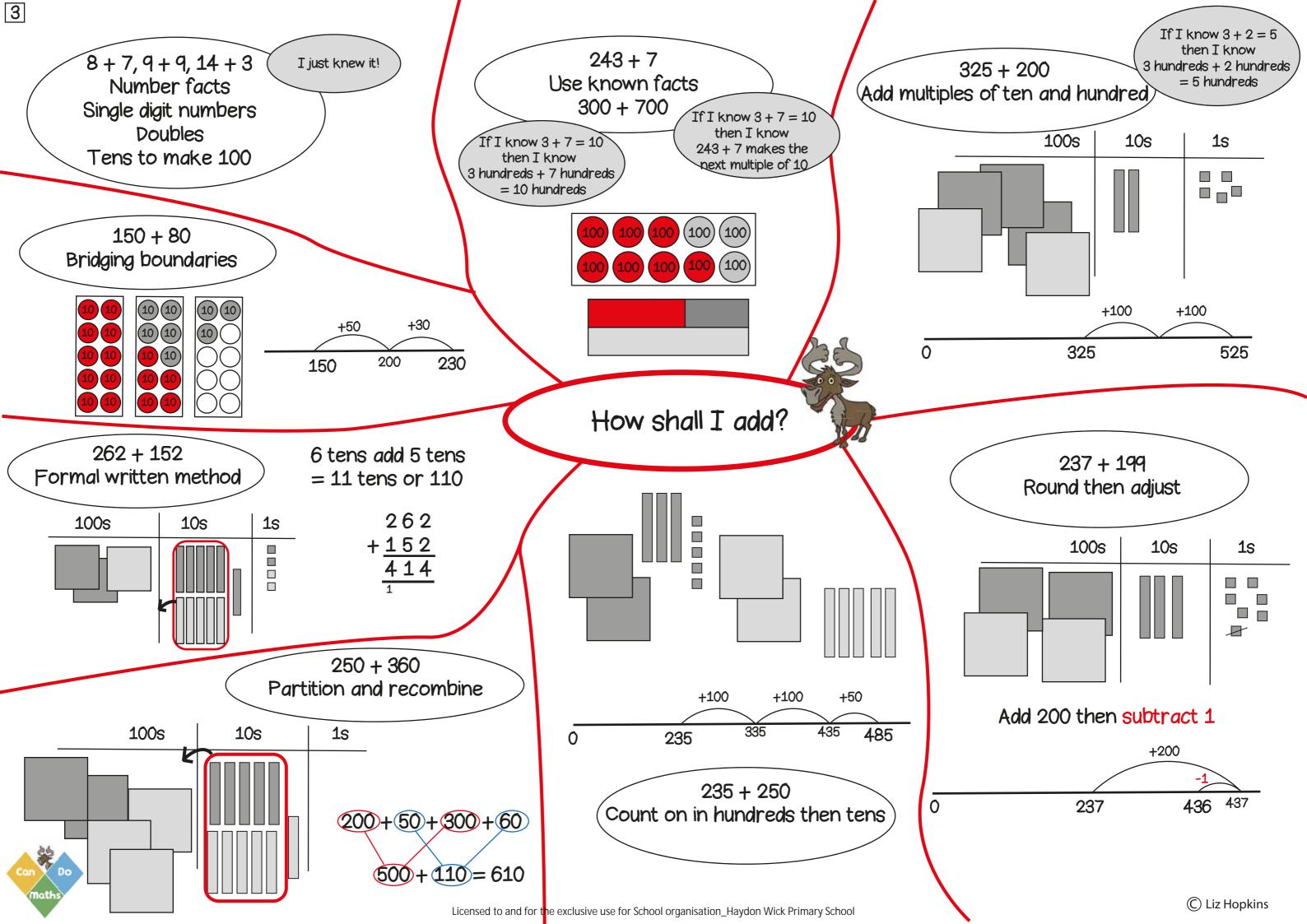
If I know  $3 \times 4 = 12$ then I know  $12 \div 3 = 4$ 



	12	
4	4	4

Link to fractions. One third of 12 is 4



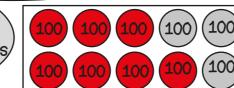




15 - 8, 18 - 5 Number facts Single digit numbers Teens and single digits I just knew it!

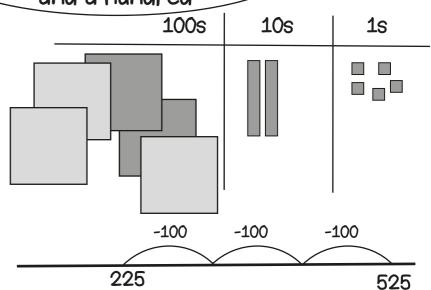
240 - 7 Use known facts 1000 - 700

If I know 10 - 7 = 3then I know 10 hundreds - 7 hundreds = 3 hundreds



If I know 10 - 7 = 3then I know any multiple of 10, take away 7 leaves 3 in the ones.

525 - 300 Take away multiples of ten and a hundred

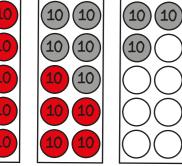


If I know 5 - 3 = 2then I know

5 hundreds - 3 hundreds

= 2 hundreds

by counting back in efficient steps 10 10 10 10 10 10

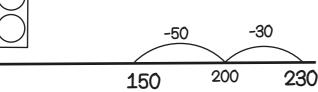


230 - 80

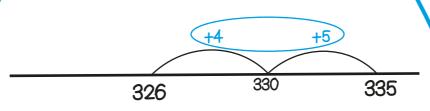
Bridging boundaries

230 - 30 - 50 = 150

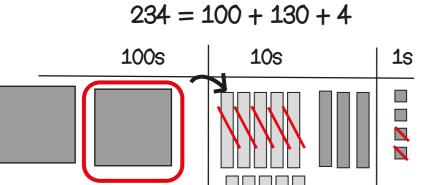
<sup>1</sup>2 <sup>1</sup>3 4



How shall I subtract?



-<u>152</u> 182

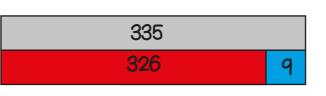


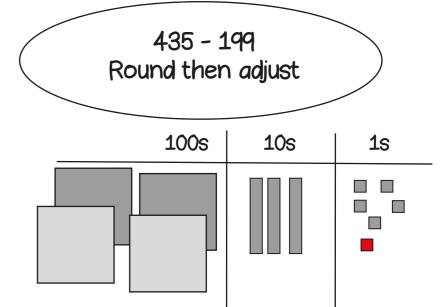
234 - 152

Formal written method

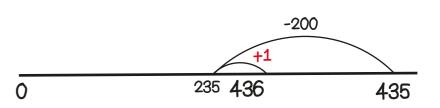
335 - 326 Find the difference between two numbers

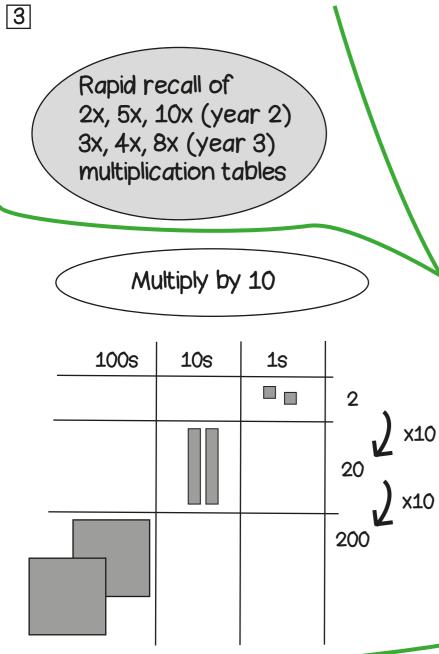
> 335 is 9 more than 326 326 is 9 less than 335 so the difference between them is 9





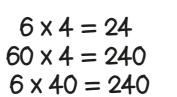
Take away 200 then add 1





6 x 4 Use known facts and place value

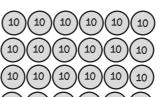
40 is ten times greater than 4





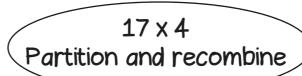


 $=24 \times 10$ 

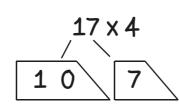


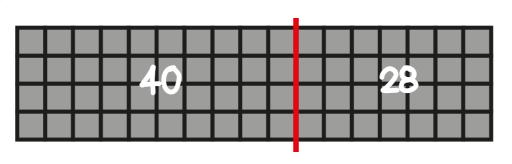
10 10

#### How shall I multiply?



$$10 \times 4 + 7 \times 4$$
  
 $40 + 28 = 68$ 







-0000000-000000-000000-

0000

0000

8

+8

Arrays



8+8+8=

(3+3+3+3+3+3+3+3

0000

8

If I know 3 x 8

then I know 8 x 3

	10	7
4	40	28

17

8 x 3

Repeated addition

0000

0000

8

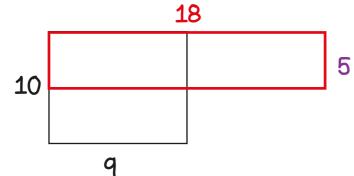
+8

16

5 x 18 10 x 9

 $= 5 \times 2 \times 18 \div 2$ 

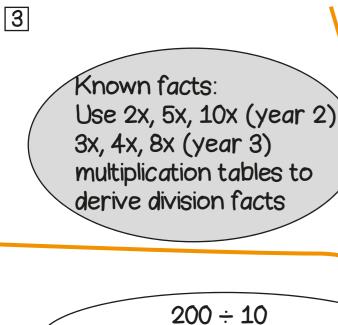
90

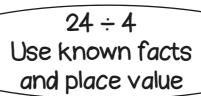


5 x 18

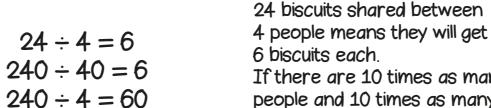
Double and halve







240 is ten times greater than 24



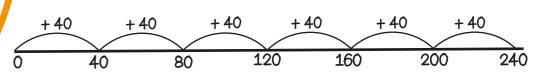
If there are 10 times as many people and 10 times as many biscuits, how many biscuits each now?

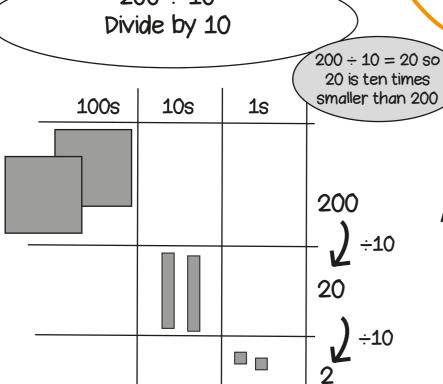
52 ÷ 4

Partition and recombine



 $240 \div 40 = 6$ How many steps of 40 make 240?



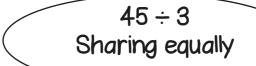


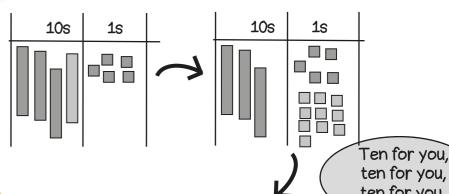
#### How shall I divide?

A tenth of is

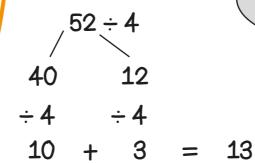
A tenth of 1 is 1 tenth  $1 \cdot 10 = 1$ 

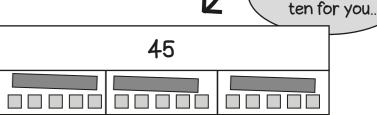
so  $1 \div 10 = \frac{1}{10}$ 





ten lots and the rest





Link to fractions

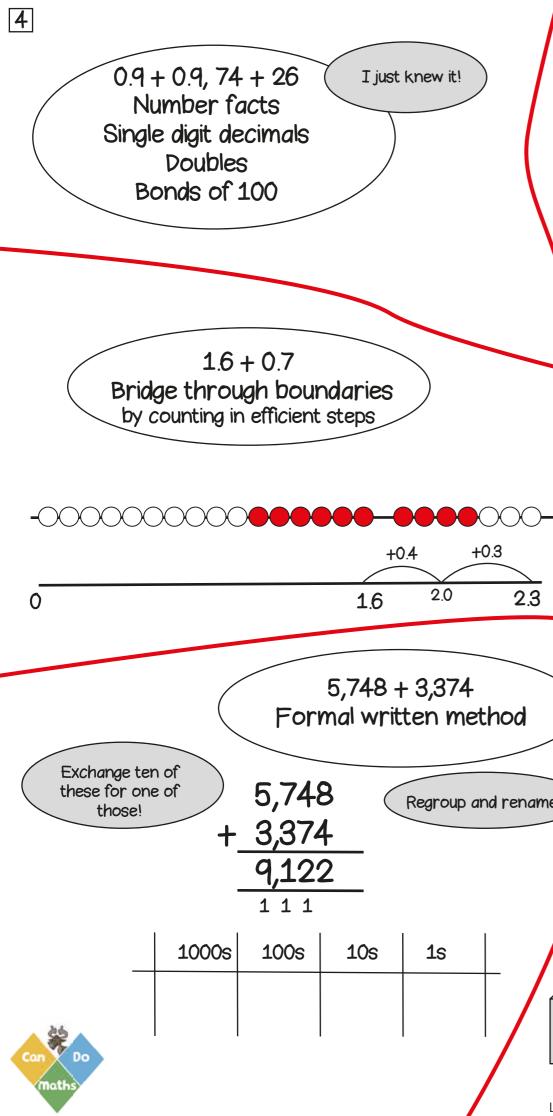
#### 42 ÷ 6 Double and halve

If there are half as many biscuits and half as many people...

$$42 \div 6 = 21 \div 3$$

			42		
7	7	7	7	7	7
	21				
7	7	7			





0.9 + 0.9, 74 + 26Number facts Single digit decimals Doubles Bonds of 100

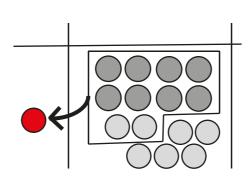
1.6 + 0.7

I just knew it!

7 + 8Use known facts

> If I know 7 + 8 = 15then I know 0.7 + 0.8 = 1.5

$$70 + 80 = 150$$
  
 $700 + 800 = 1,500$ 



2,403 + 3,020Use place value to add

If I know 2+3=5then I know 2000 + 3000 = 5000

I have noticed, one number has no hundreds or ones, the other has no tens

1000s	100s	10s	1s	
			00	-

#### How shall I add?

5,250 + 2,360Partition and recombine

#### 3,356 + 1,998 Round then adjust

1000s	100s	10s	<b>1</b> s

Regroup and rename

+0.3

2.3

2.0

1.6

5,748 + 3,374

Formal written method

.000s	100s	10s	1s	

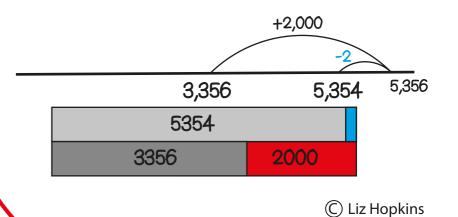
5,748

9,122

1 1 1

+ 3,374

1000s 100s 10s **1**s Add 2,000 then take away 2



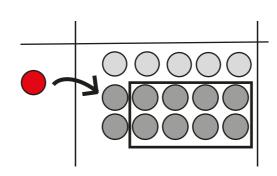
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13 - 5, 1.8 - 0.8 Number facts Single digit numbers Halves Wholes and tenths

15 - 8 = 7Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

$$150 - 80 = 70$$
  
 $1500 - 800 = 700$ 



6,342 - 3,020 Use place value to subtract

1000s

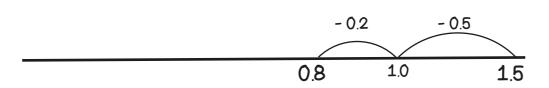
By using place value counters it is easy to

see how to take away

1s

**10s** 

1.5 - 0.7Bridge through boundaries by counting in efficient steps



How shall I subtract?

5,352 - 2,136 Formal written method

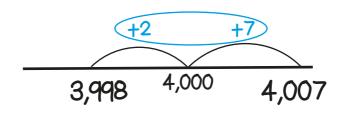
Regroup and rename

I just knew it!

Exchange ten of 5,352 these for one of those! 2,436 2,916

1000s	100s	10s	<b>1</b> s	

4007-3998 Find the difference between two numbers



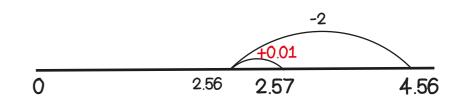
4,007	
3,998	9

4.56 - 1.99 Round then adjust

100s

<b>1</b> s	$\frac{1}{10}$ S	100 s

Take away 2 then add one hundredth







Known facts: Rapid recall of all multiplication tables up to 12 x 12

## 6 x 4

Use known facts and place value

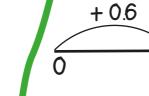
greater than 4

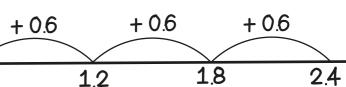
40 is ten times







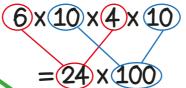




6 x 4

Use known facts

and place value



x10

x10

x100

2.34

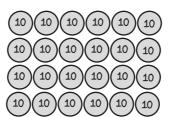
23.4

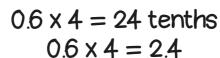
234

 $6 \times 4 = 24$ 

 $60 \times 4 = 240$ 

 $60 \times 40 = 2400$ 





 $0.6 \times 4 = 2.4$ 

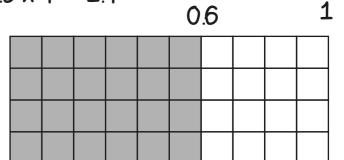
4 jumps of 0.6



0.6 is ten times

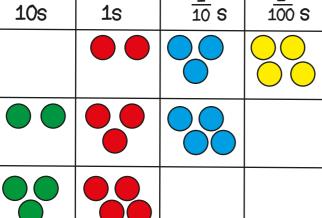
smaller than 6

0.6

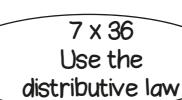


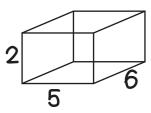
2.34 x 100 Multiply by 10, 100

10 s	100 s	
		_

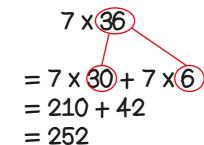


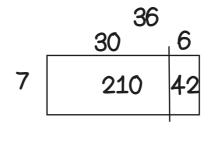
How shall I multiply?





45 x 6 Use factors and commutativity



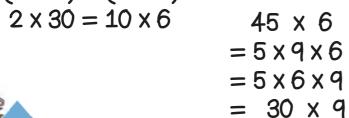


100s

 $\bigcirc\bigcirc$ 

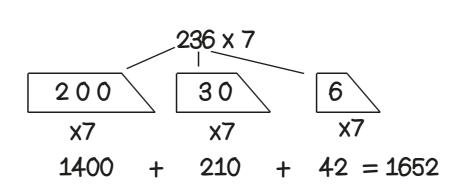
1000s

 $2 \times (5 \times 6) = (2 \times 5) \times 6$ 



= 270

Write as factors then re-order



36 x 7 Formal written method

	30	6	36
7	210	42	X 7 252

1



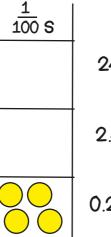
100s

**10**s

Known facts:
Use recall of all
multiplication tables
up to 12 x 12 to
derive division facts

 $24 \div 100$  Divide by 10, 100

1s



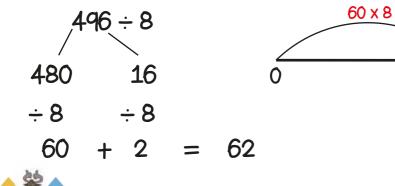
24 2.4 2.4 2.4 2.10 2.4 2.100

2 x 8

496

480

 $\frac{1}{10}$  s



#### 24 ÷ 4 Use known facts and place value

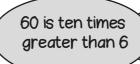
 $24 \div 4 = 6$   $240 \div 40 = 6$  $2400 \div 400 = 6$ 

$$2400 \div 400 = \frac{24 \times 100}{4 \times 100}$$
$$\frac{24}{4} = 6$$

### 240 is ten times greater than 24

24 biscuits shared between 4 people means they will get 6 biscuits each.

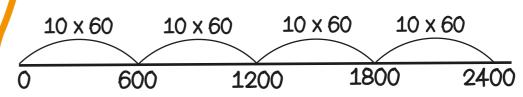
If there are 100 times as many people and 100 times as many biscuits, how many biscuits each now?



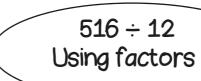
2400 ÷ 60 Use known facts and place value

$$2400 \div 60 = 40$$

How many steps of 60 make 2400?

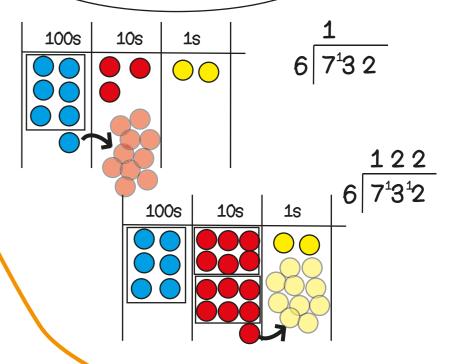


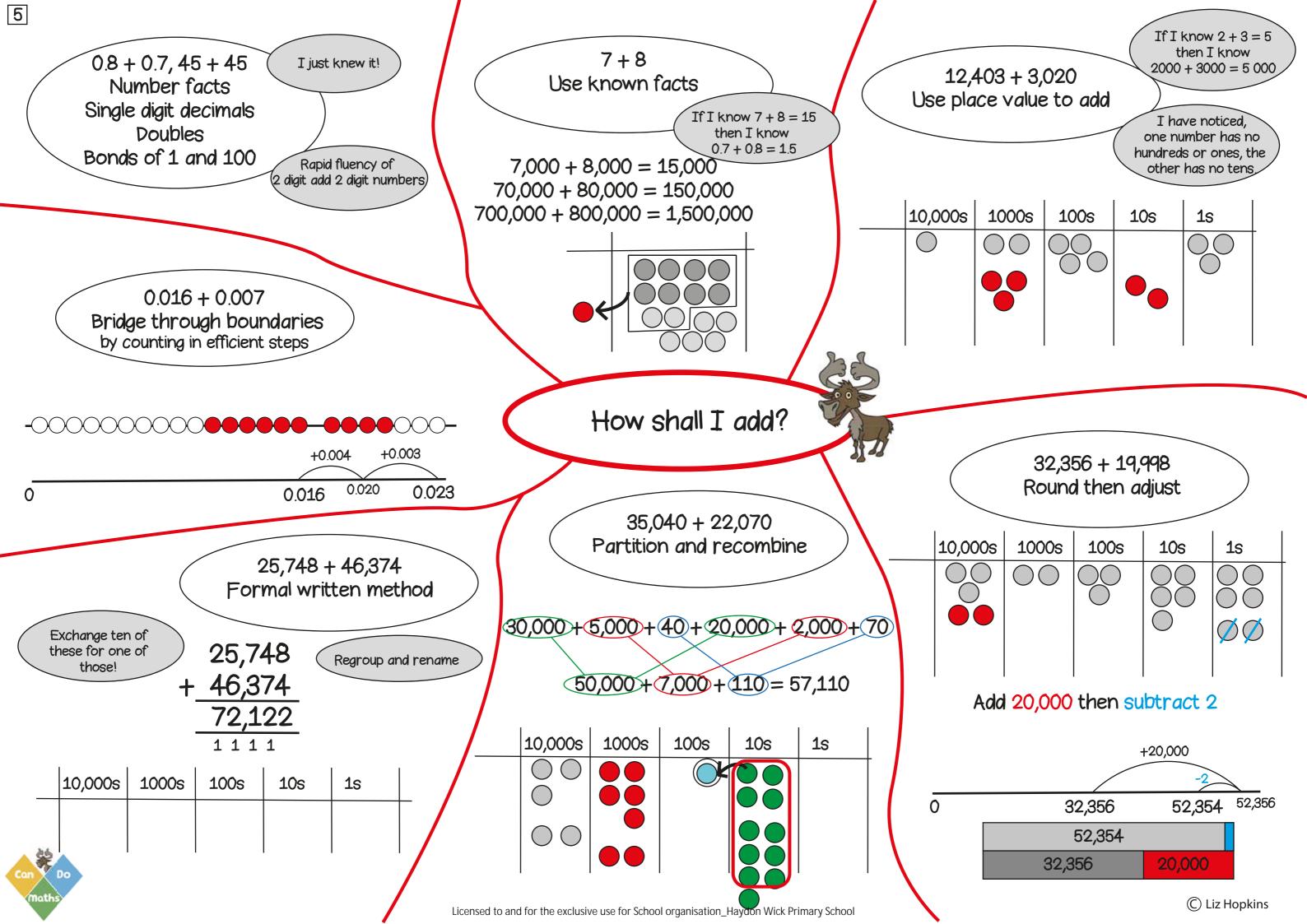
#### How shall I divide?



516												
	17	72			17	'2						
43	43	43	43									

#### 732 ÷ 6 Formal written method





9 - 4, 13 - 5, 18 - 9

Number facts

Single digit decimals

Halves

Subtract from 1 and 100

I just knew it!

Rapid fluency of

2 digit subtract

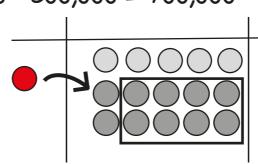
2 digit numbers

15 - 8 = 7 Use known facts

> If I know 15 - 8 = 7 then I know 1.5 - 0.8 = 0.7

15,000 - 8,000 = 7,000

150,000 - 80,000 = 70,000 1,500,000 - 800,000 = 700,000



40,012 - 3,005 Use place value to subtract

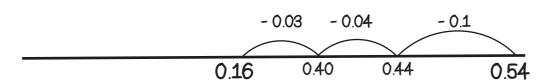
5 less than 12 is 7 Now it is easy to take away 3000

If I know 40 - 3 = 37 then I know that 40 thousand take away 3 thousand is 37 thousand

40,000 = 4 tens of thousands or 40 thousands 12 = 1 ten and 2 ones or 12 ones

40,012 = 40 thousands and 12 ones take away 3 thousands and 5 ones equals 37 thousands and 7 ones.

0.54 - 0.17
Bridge through boundaries
by counting in efficient steps



How shall I subtract?

45,748 - 26,374 Formal written method

Exchange ten of these for one of those!

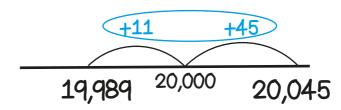
345,748 26,374

Regroup and rename

- <u>26,374</u> <u>19,374</u>

10,000s	1000s	100s	10s	<b>1</b> s	

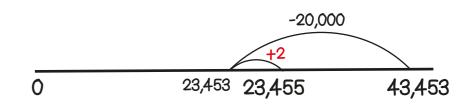
20,045 - 19,989 Find the difference between two numbers

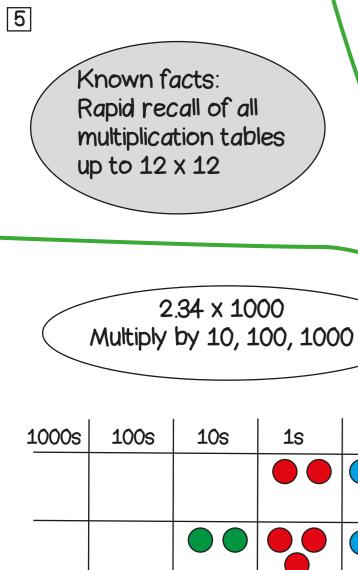


20,045 19,989 56 43,453 - 19,998 Round then *adjust* 

10,000s	1000s	100s	<b>10</b> s	1s	

Take away 20,000 then add 2





6 x 4 Use known facts and place value

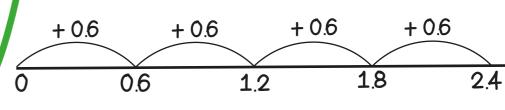
x100

$$6 \times 4 = 24$$
  
 $60 \times 4 = 240$   
 $60 \times 40 = 2400$ 

40 is ten times

greater than 4





 $0.6 \times 4 = 2.4$ 

4 jumps of 0.6

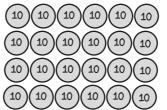
6 x 4

Use known facts

and place value

0.6

1



 $0.6 \times 0.4 = 24$  hundredths  $0.6 \times 0.4 = 0.24$ 

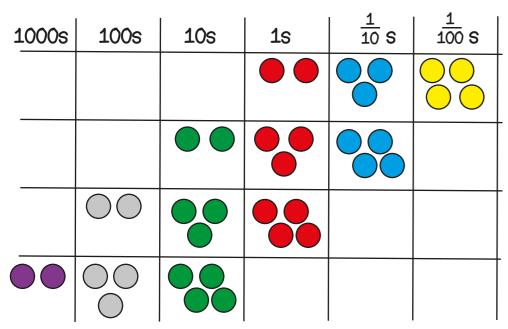
0.6 is ten times

smaller than 6





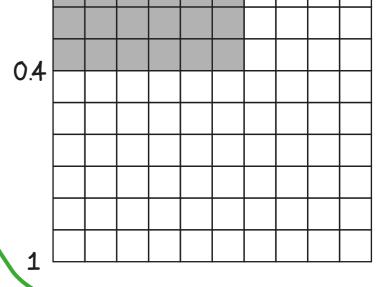
How shall I multiply?



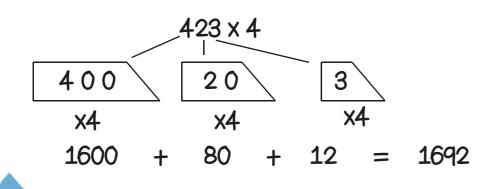
2.34 **x10** 23.4 x10 234 / x10 2340

15 x 42 Using factors and distributive law

15 x 48  $= 15 \times 6 \times 8$  $= 90 \times 8$ = 720



423 x 4 Partition and recombine



15 x 14)  $= 15 \times 6 + 15 \times 8$ = 90 + 120

= 210

427 x 38 Formal written method

		400	20	7
	30	12,000	600	210
,	8	3,200	160	56

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Known facts:

Use recall of all

up to 12 x 12 to

multiplication tables

derive division facts

Include calcuations where remainders occur

24 ÷ 4 Use known facts

and place value

24,000 is a thousand times greater than 24

0.6 is ten times smaller than 6

0.6

1000s 100s

 $2.4 \div 0.6$ Use known facts and place value

How many steps of 0.6 make 2.4?

$$2.4 \div 0.6 = 4$$
w many steps of 0.6 i

+ 0.6+ 0.6 + 0.6 + 0.6

1.2

5724 ÷ 4

Formal written method

$$24 \div 4 = 6$$
  
 $240 \div 40 = 6$   
 $2400 \div 400 = 6$   
 $24,000 \div 4000 = 6$ 

If there are 1000 times as many people and 1000 times as many biscuits, how many biscuits ach now?

4 people means they will get

6 biscuits each.

$$24,000 \div 400 = \underbrace{24 \times 1000}_{4 \times 100}$$

	ea
24,000 ÷ 400 =	24 x 1000
	4 x 100

$$\frac{240}{4} = 60$$

÷10

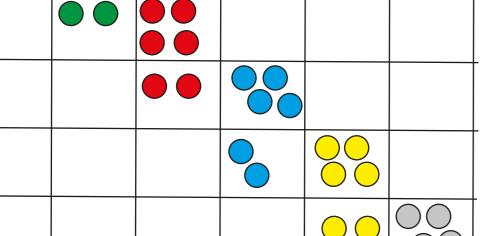
÷10

÷1000

# 100s

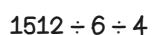
24 ÷ 1000

Divide by 10, 100, 1000

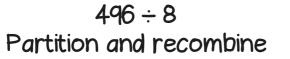


## How shall I divide?

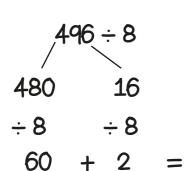
1512 ÷ 24 Using factors

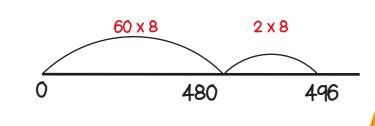


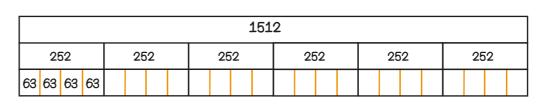
		_5 -		-000	
					24
					2.4
					0.24
			00	00	0.024

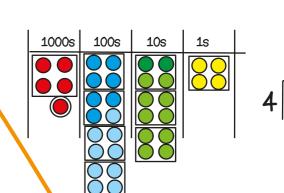


62













44 + 56, 27 + 27 Number facts Single digit decimals Doubles Bonds of 1 and 100

I just knew it!

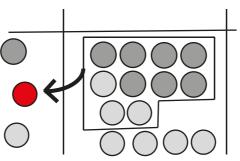
Rapid fluency of 2 digit add 2 digit numbers 17 + 17 Use known facts

> If I know 17 + 17 = 34 then I know 1.7 + 1.7 = 3.4

17,000 + 17,000 = 34,000

170,000 + 170,000 = 340,000

1,700,000 + 1,700,000 = 3,400,000



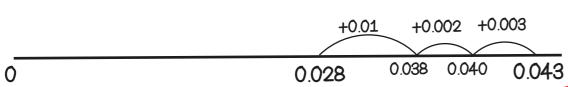
1,102,403 + 50,020 Use place value to add

I have noticed, one number has no hundreds or ones, the other has no tens

1,000,000s	100,000s	10,000s	1000s	100s	10s	<b>1</b> s
				00		

## 0.028 + 0.015 Bridge through boundaries by counting in efficient steps





325,748 + 246,374 Formal written method

Regroup and rename

Exchange ten of these for one of those!

325,748 + 246,374 572,122

100,000s	10,000s	1000s	100s	10s	<b>1</b> s	

#### How shall I add?

307,040 + 206,070 Partition and recombine

300,000 + 7,000 + 40 + 200,000 + 6,000 + 70

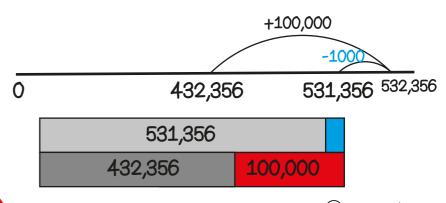
500,000 + 13,000 + 110 = 513,110

100,000s	10,000s	1000s	100s	10s	1s
00					
00					

432,356 + 99,000 Round then *adjust* 

100,000s	10,000s	1000s	100s	10s	<b>1</b> s
	00	<b>Ø</b>		000	000

Add 100,000 then take away 1,000



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0.9 - 0.4, 100 - 65 Number facts Single digit decimals Halves

Bonds of 1 and 100

Rapid fluency of 2 digit subtract 2 digit numbers

I just knew it!

0.054 - 0.017

Bridge through boundaries by counting in efficient steps

0.037 0.040 0.044 0.054

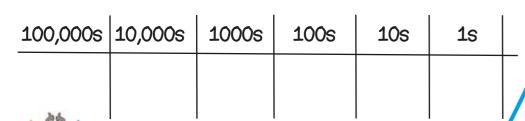
445,748 - 126,374 Formal written method

Regroup and rename

Exchange ten of these for one of those!

445,748 126,374

+ <u>126,374</u> 319,374



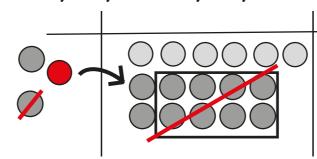
36 - 18 = 18Use known facts

> If I know 36 - 18 = 18 then I know 3.6 - 1.8 = 1.8

36,000 - 18,000 = 18,000

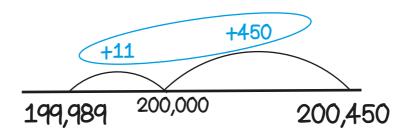
360,000 - 180,000 = 180,000

3,600,000 - 1,800,000 = 1,800,000



How shall I subtract?

200,450 - 199,989 Find the difference between two numbers



200,450 199,989 461 400,032 - 30,005 (Use place value to subtract

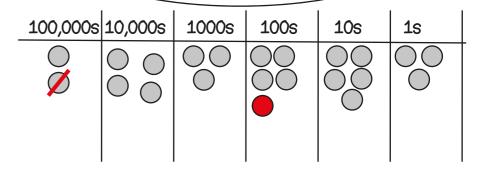
5 less than 32 is 27

400,000 = 4 hundreds of thousands or 400 thousands

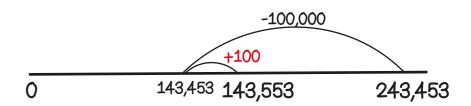
400 - 30 = 370 so 400,000 - 3,000 = 370,000

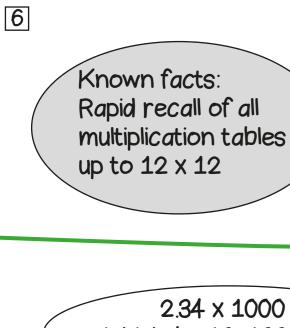
400,032 = 400 thousands and 32 ones take away 30 thousands and 5 ones = 370,027

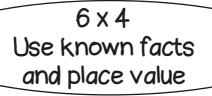
> 243,453 - 99,900 Round then *adjust*



Take away 100,000 then add 100





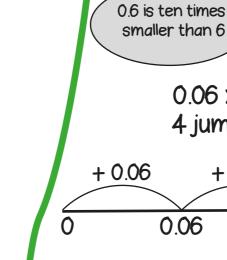


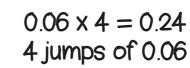
40 is ten times greater than 4

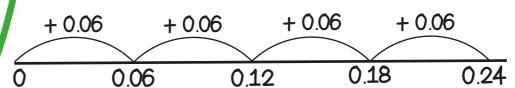
$$60 \times 40 = 2400$$
  
 $600 \times 400 = 240,000$ 

6000 x 4000 = 24,000,000

6x10x4x10





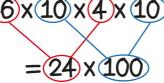


6 x 4

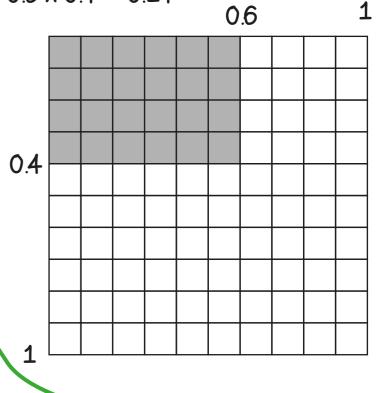
Use known facts

and place value

2.34 x 1000 Multiply by 10, 100, 1000



 $0.6 \times 0.4 = 24$  hundredths  $0.6 \times 0.4 = 0.24$ 



100 S 1 10 S 100s 1000s **10s** 1s 2.34 23.4  $\bigcirc\bigcirc$ 234 2340

#### How shall I multiply?

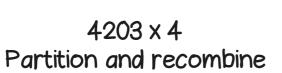
15 x 42 Using factors and distributive law

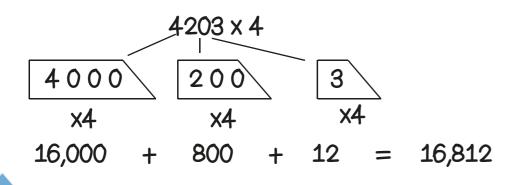
15 x 48  $= 15 \times 6 \times 8$  $= 90 \times 8$ = 720

x100

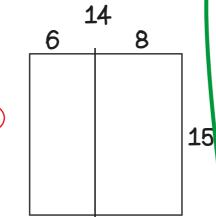
**x10** 

x10





15 x 14)  $= 15 \times 6 + 15 \times 8$ = 90 + 120= 210



2427 x 38 Formal written method

Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

6

Include calcuations where remainders occur

#### 24 ÷ 4

Use known facts and place value

240 is ten times greater than 24

24 biscuits shared between

4 people means they will get

If there are 10 times as many

people and 10 times as many

biscuits, how many biscuits

6 biscuits each.

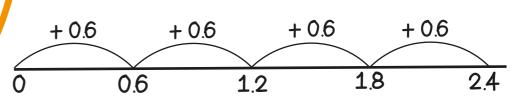
each now?

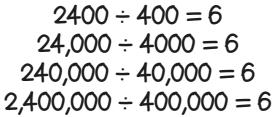
0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?





÷10

 $240 \div 40 = 6$ 

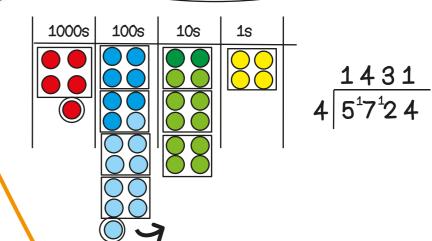
 $240,000 \div 400 = 24 \times 10,000$ 4 x 100

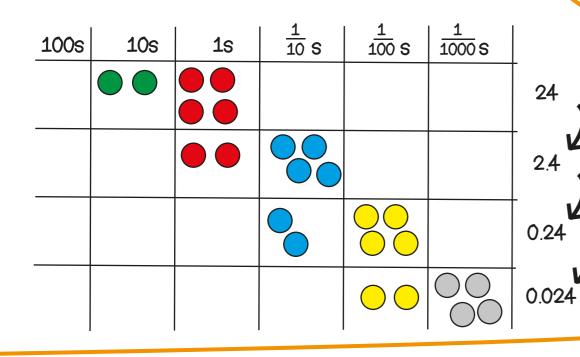
$$\frac{2400}{4} = 600$$

÷1000

#### How shall I divide?

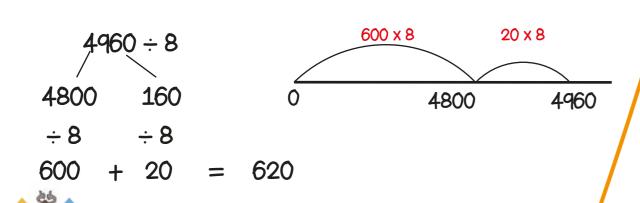
7182 ÷ 21 Formal written method





1512 ÷ 24 Using factors

#### 4960 ÷ 8 Partition and recombine



#### $1512 \div 6 \div 4$

										:	151	2										
		25	52	252				252			252			252			252					
4	63 63 63 63																					

	342	
21	7182 63	
!	63	
	88	
	<u>84</u>	
	42	
	<u>42</u>	
	0	