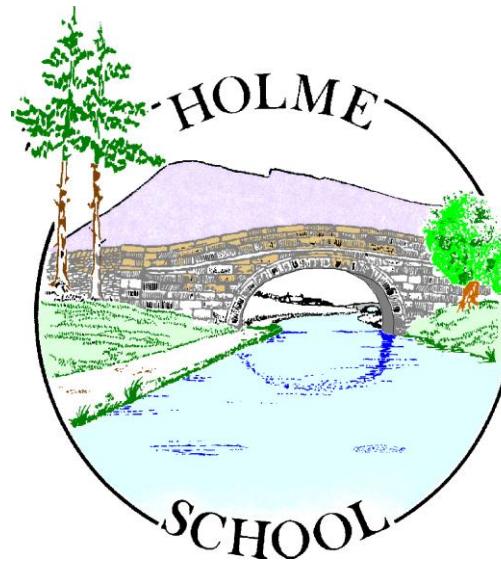


Holme Community School



Calculations Policy

Written by:	Mr I Holland (Deputy Headteacher)
First Published:	March 2021
This Review:	March 2021
Next Review Due:	March 2024

Aim of the policy:

- To ensure consistency and progression in our approach to calculation and enable a smooth transition between year groups and phases.
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations.
- To ensure that children can use these methods accurately with confidence and understanding.
- To ensure pupils understand important concepts and make connections within mathematics.
- To ensure pupils show high levels of fluency in performing written and mental calculations.
- To ensure that pupils are ready for the next stage of learning and have been given strong foundations in mental methods, the use of practical equipment, allowed to explore jottings in a range of forms and then to move onto more formal recording using a strong knowledge of place value, number lines labelled or blank, partitioning before eventually using compact written methods.
- To ensure that pupils are competent in fluency, reasoning and problem solving and can make informed and appropriate choices about the methods they wish to use (mental or written) to solve mathematical problems efficiently and effectively.

Responsibilities:

Teaching Assistants: To support class teachers by reinforcing these methods during group and intervention work.

Class Teachers: To ensure that teaching and learning follows these methods and the sequence of learning

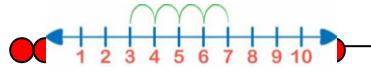
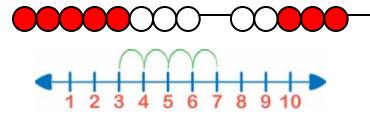
Subject Leader: To ensure that this policy is consistently applied and that teachers have the training and support to implement it effectively.

Senior Leadership Team: To ensure that monitoring of the policy takes places and that the subject leader has access to resources to ensure this policy is successful.

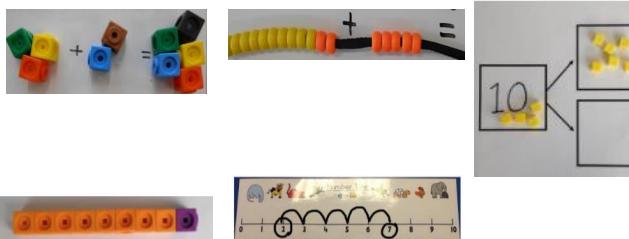
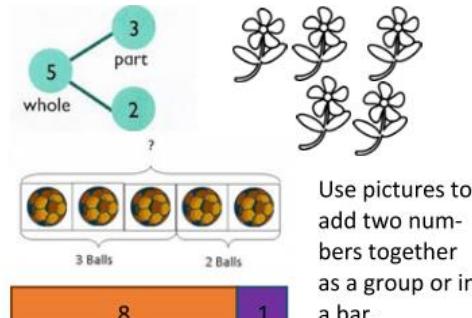
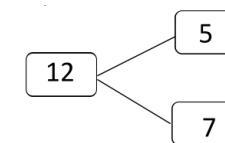
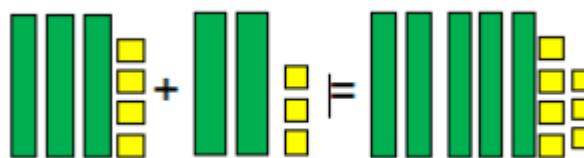
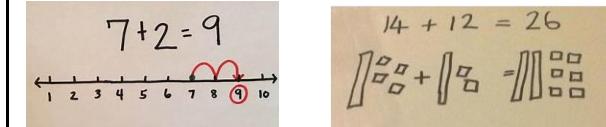
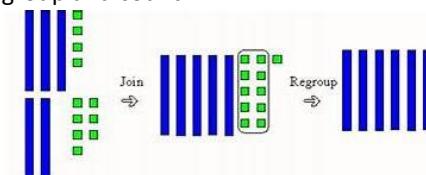
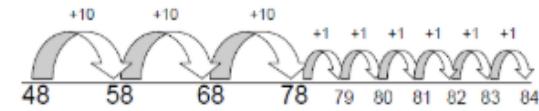
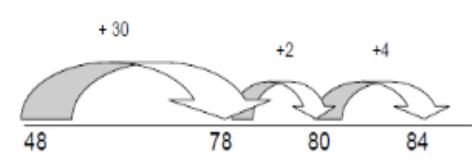
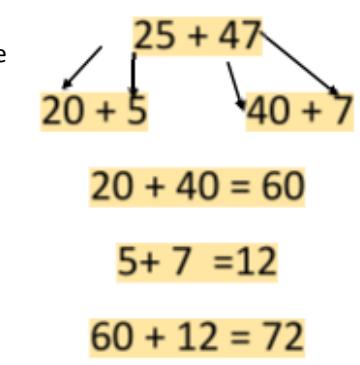
Governing Body: To monitor the implementation and impact of the policy.

Calculation Policy

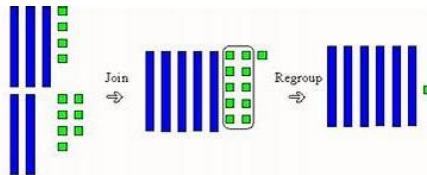
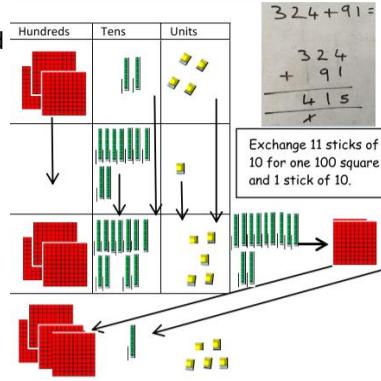
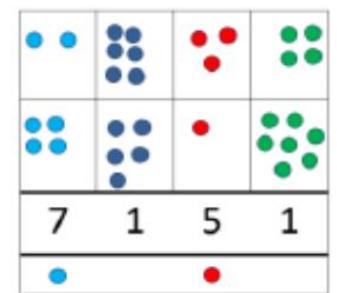
EYFS (Nursery & Reception)

Addition	Subtraction	Multiplication	Division
<p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects.</p>  <p>They combine objects in practical ways and count all.</p>  <p>They understand addition as counting on and will count on in ones and twos using objects, cubes, bead string and number line.</p>  <p>They use concrete and pictorial representation to record their calculations.</p> <p>They begin to use + and =</p>  <p>They are encouraged to develop a mental picture of the number system in their heads to use for calculations.</p>  <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>	<p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects.</p>  <p>They understand subtraction as counting out.</p>  <p>They begin to count back in ones and twos using objects, cubes, bead string and number line.</p>  <p>They use concrete and pictorial representation to record their calculations.</p> <p>They begin to use - and =</p> <p>They are encouraged to develop a mental picture of the number system in their heads to use for calculations.</p> <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>	<p>Children use concrete objects to make and count equal groups of objects.</p> <p>They will count on in twos using a bead string and number line.</p> <p>They understand doubling as repeated addition.</p> $2 + 2 = 4$ <p>They use concrete and pictorial representation to record their calculations.</p> <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>	<p>Children use concrete objects to count and share equally into 2 groups.</p> <p>6 cakes shared between 2 people each person gets 3 cakes. $6 \div 2 = 3$</p>  <p>They count a set of objects and halve them by making two equal groups.</p> <p>They understand sharing and halving as dividing by 2.</p> <p>They will begin to use objects to make groups of 2 from a given amount.</p> <p>They use concrete and pictorial representation to record their calculations.</p>  <p>Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p>

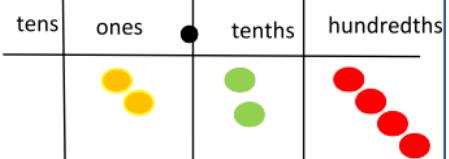
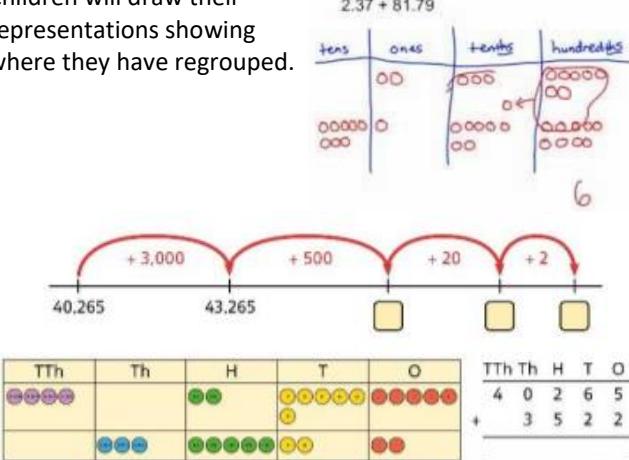
ADDITION - KS1 (Years 1&2)

Concrete			
Pictorial			
Abstract			
Stage 1	<p>Use part part whole model, cubes and bead strings to add two numbers together as a group or in a bar.</p> 	<p>Use jottings to represent numbers.</p>  <p>Use pictures to add two numbers together as a group or in a bar.</p>	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p>  <p>$11 + 4 = 15$</p> <p>They may use their fingers to support their mental methods</p>  <p>$5 + 2 = 7$</p>
Stage 2	<p>Grouping objects to add Children will use dienes cubes to add larger numbers where regrouping is not required.</p> <p>They will also use a bead string to add larger numbers by counting in tens and ones</p> 	<p>Number line Start at the larger number on the number line and count on in ones or in one jump to find the answer. Children will show their representations from the concrete method using pictures.</p>  <p>Numbers will get progressively larger throughout the keystage. Children will be able to add tens and ones using an empty number line.</p>	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p>$27 + 10 = 37$</p> <p>$27 + 20 = 47$</p> <p>Children will begin to add multiples of tens.</p> <p>$27 + \square = 57$</p>
Stage 3	<p>Partitioning Children will add larger numbers where they will need to join, regroup and count.</p> 	<p>Number line Use an empty number line to count in tens and then ones.</p>  <p>When confident:</p> 	<p>Partitioning Children will begin to use the partitioning method. Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total.</p> 

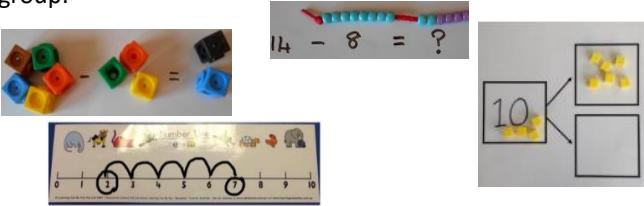
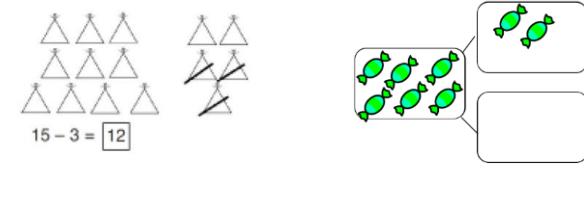
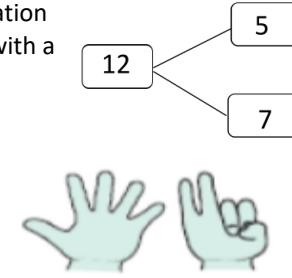
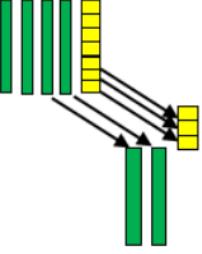
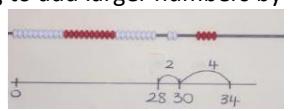
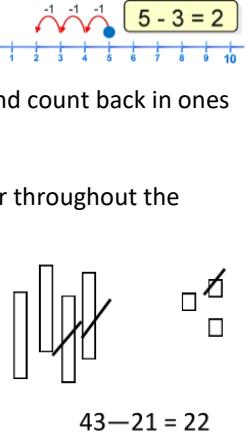
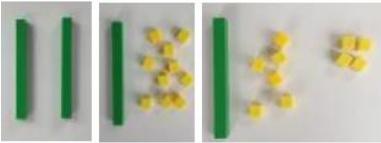
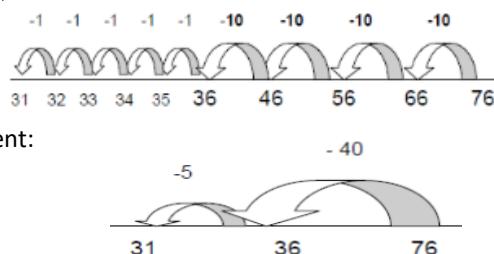
ADDITION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
Stage 1	<p>Use dienes cubes to consolidate learning from KS1. Ensure children are confident at using these to join, regroup and count. This will support them moving onto the next stage of column addition.</p> 	<p>Number line Consolidate their learning from KS1 by using an empty number line to count larger numbers.</p> 	<p>Partitioning Children will consolidate using the partitioning method. The layout will begin to form a written method to support further progress onto the column method. Hundreds, Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total.</p> $ \begin{array}{r} 200 + 60 + 3 \\ + 100 + 10 + 9 \\ \hline 300 + 70 + 12 \\ \hline 300 + 80 + 2 \end{array} $
Stage 2	<p>Introduce children to place value counters and dienes cubes. Use the column method layout to support their learning onto the abstract method.</p> 	<p>Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line.</p> 	<p>Expanded column method - Formal method Children to use the Expanded Column Method. Start by partitioning the numbers before the formal column to show the exchange. Once confident, they can move onto the column method in stage 3.</p> $ \begin{array}{r} 176 \\ + 147 \\ + 13 \\ + 110 \\ \hline 200 \\ \hline 323 \end{array} \quad \begin{array}{r} (7+6) \\ (70+40) \\ (100+100) \\ \hline 147 \end{array} \quad \begin{array}{r} 147 \\ + 176 \\ \hline 323 \end{array} $
Stage 3	<p>Children will add larger numbers where they will need to exchange place value counters or dienes cubes.</p> 	<p>Bar Model Bar model can be introduced using a two-bar model</p> $ \begin{array}{c} 3 + 4 = ? \\ \hline \begin{array}{ c c } \hline 3 & 4 \\ \hline \end{array} \\ \hline \begin{array}{ c } \hline ? \\ \hline \end{array} \\ \hline 3 + 4 = 7 \end{array} $	<p>Column method - Formal method Column Method for addition to be used. The exchanged value should be crossed out when used.</p> $ \begin{array}{r} 4478 \\ + 3762 \\ \hline 8240 \end{array} $

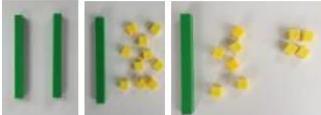
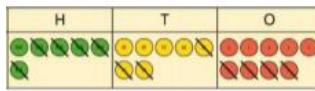
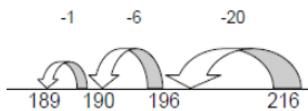
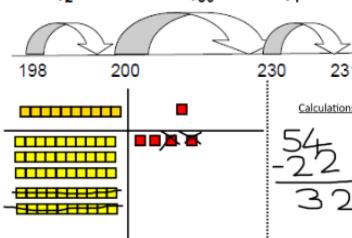
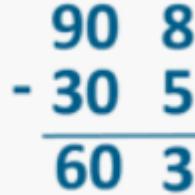
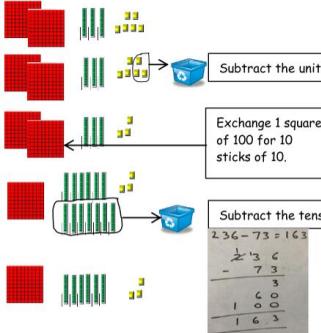
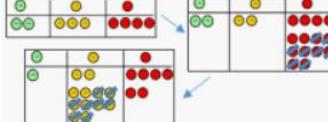
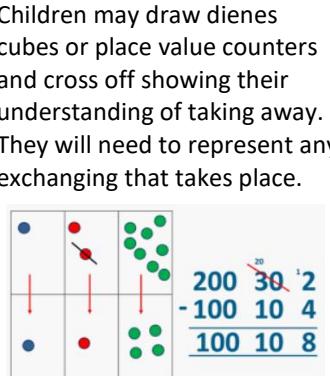
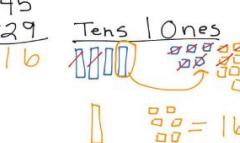
ADDITION - Upper KS2 (Years 5 & 6)

	Concrete	Pictorial	Abstract					
Stage 1	<p>Introduce decimal place value counters and model regrouping for addition.</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">tens</td> <td style="text-align: center;">ones</td> <td style="text-align: center;">.</td> <td style="text-align: center;">tenths</td> <td style="text-align: center;">hundredths</td> </tr> </table> 	tens	ones	.	tenths	hundredths	<p>Children will draw their representations showing where they have regrouped.</p> <p>$2.37 + 81.79$</p> 	<p>Column method</p> <p>Children will continue to develop their understanding of column method addition. Calculations will become larger and include decimal places.</p> <p>$\begin{array}{r} 379.173 \\ + 203.116 \\ \hline 582.289 \end{array}$</p>
tens	ones	.	tenths	hundredths				
Stage 2	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for those children struggling to grasp a concept and those with SEND.</p>	<p>Children will begin to use the bar model when problem solving. Jottings and calculations should be recorded to show their processes.</p> <p>$18 - 3 = ?$</p> <p>$\begin{array}{c} 18 \\ + 35 \\ \hline 53 \end{array} \quad \begin{array}{r} 77 \\ - 53 \\ \hline 24 \end{array}$</p>	<p>Column method</p> <p>Children to further develop their confidence using the column method. Larger numbers, decimal places and inserting zero for place holders when decimals are different.</p> <p>$\begin{array}{r} 447813 \\ + 376245 \\ \hline 824058 \end{array}$</p> <p>Numbers with 3 decimal place</p> <p>$\begin{array}{r} 379.173 \\ + 203.116 \\ \hline 582.289 \end{array}$</p> <p>Numbers with a different number of decimal places</p> <p>Insert zeros for place holders.</p> <p>$\begin{array}{r} 23.361 \\ 9.080 \\ + 59.770 \\ \hline 93.511 \end{array}$</p> <p>$45.25 + 8.5 + 3.247$</p> <p>$\begin{array}{r} 45.250 \\ + 8.500 \\ + 3.247 \\ \hline 56.997 \end{array}$</p>					

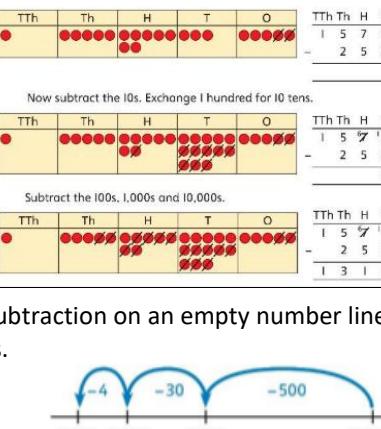
SUBTRACTION - KS1 (Years 1&2)

	Concrete	Pictorial	Abstract
Stage 1	<p>Taking objects away Use part whole model, cubes and bead strings to subtract two numbers together by moving objects away from the group.</p> 	<p>Use jottings to represent numbers. Children will learn to cross out drawn objects to show what has been taken away.</p> 	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p>$11 - 4 = 7$</p> <p>They may use their fingers to support their mental methods</p> 
Stage 2	<p>Children will use dienes cubes to subtract larger numbers where exchanging is not required. Children will lay out the first number using the dienes cubes and then move the second number away to show the subtraction.</p>  <p>They will also use a bead string to add larger numbers by counting in tens and ones.</p> 	<p>Number line Children will begin to draw their own number lines. Start at the larger number on the number line and count back in ones or in one jump to find the answer.</p> <p>Numbers will get progressively larger throughout the keystage. Children will be able to subtract tens and ones using an empty number line.</p> <p>Children will show their representations from the concrete method using pictures.</p> 	<p>Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.</p> <p>$25 - 12 = 13$</p> <p>Children will begin to subtract multiples of tens.</p> <p>$25 - 10$</p> <p>$25 - 10 = 15$</p>
Stage 3	<p>Children will begin to use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones.</p> 	<p>Empty number line - Use an empty number line to count back in tens and then ones.</p> <p>When confident:</p> 	

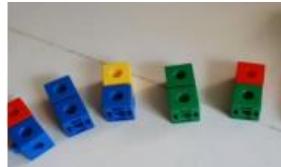
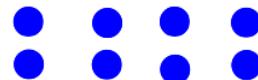
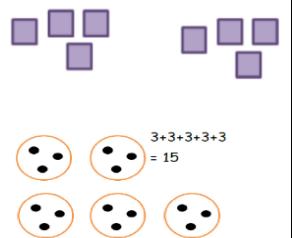
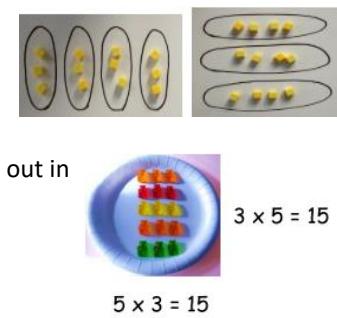
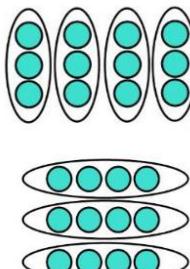
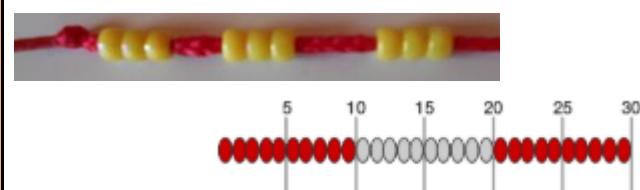
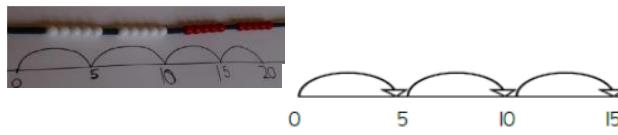
SUBTRACTION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
Stage 1	<p>Children consolidate and use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones.</p> <p>They will be able to begin to lay this out like the column method and removing counters or cubes away to represent taking away.</p>  <p> </p>	<p>Consolidate their learning from KS1 by using an empty number line to calculate larger numbers.</p> <p>Children will also be able to draw representations of dienes cubes and place value counters by crossing out the number being taken away.</p>	<p>Develop the use of empty number line with calculations that bridge 100:</p>  <p>Count on to find small differences:</p>  <p></p> <p>$\begin{array}{r} 47 - 24 = 23 \\ - 30 \quad 5 \\ \hline 60 \quad 3 \end{array}$</p> <p>$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$</p>
Stage 2	<p>Children begin to set out HTU - HTU using dienes cubes and place value counters (that cross the tens boundary) in columns and record as column subtraction with decomposition. Teach children how to exchange units of numbers.</p>  <p></p>	<p>Children may draw dienes cubes or place value counters and cross off showing their understanding of taking away. They will need to represent any exchanging that takes place.</p> 	<p>Partitioning method - with exchanging</p> <p>Children will use the partitioning method to show exchanging.</p> <p>$\begin{array}{r} 45 \\ - 29 \\ \hline 16 \end{array}$ </p> <p>$\begin{array}{r} 50 \\ - 100 \\ \hline 100 \end{array}$ $\begin{array}{r} 13 \\ + 9 \\ \hline 22 \end{array}$</p> <p>Once confident, children can start to use the column method.</p> <p>$\begin{array}{r} 5 \quad 1 \\ - 2 \quad 6 \quad 3 \\ \hline 1 \quad 4 \quad 4 \end{array}$</p>
Stage 3	<p>Children continue to develop their confidence in using dienes cubes and place value counters to show decomposition using the column method.</p> 	<p>Bar Model</p> <p>Introduce as a two-bar model:</p> <p>$\begin{array}{r} 18 - 3 = ? \\ 18 \\ ? \quad 3 \\ 18 - 3 = 15 \end{array}$</p>	<p>Column Method</p> <p>Children continue to use column method to subtract larger numbers.</p> <p>$\begin{array}{r} 5 \quad 13 \quad 1 \\ - 2 \quad 6 \quad 8 \quad 4 \\ \hline 3 \quad 7 \quad 8 \quad 3 \end{array}$</p>

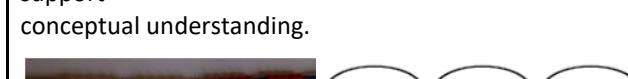
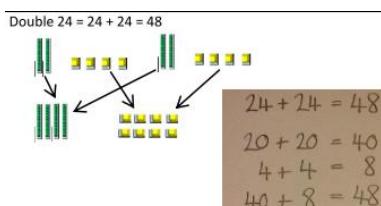
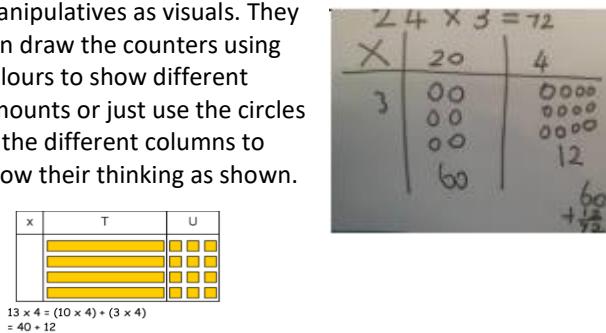
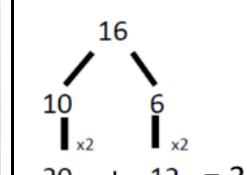
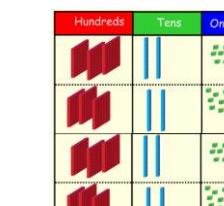
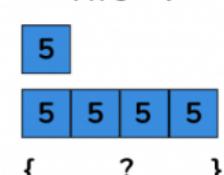
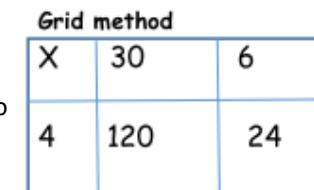
SUBTRACTION - Upper KS2 (Years 5 & 6)

Concrete		Pictorial	Abstract			
Stage 1	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for those children struggling to grasp a concept and those with SEND.</p>	<p>Children can draw using place value counters showing how exchanging takes place between the units of numbers.</p> <p>$15,735 - 2,582 = 13,153$</p> <p>Now subtract the 10s. Exchange 1 hundred for 10 tens.</p> <p>Subtract the 100s, 1,000s and 10,000s.</p> <p>Children also show subtraction on an empty number line using larger numbers.</p> 	<p>Column Method</p> <p>Children will continue to develop their understanding of column method subtraction. Calculations will become larger.</p> <p>5 digit - 5 digit</p> $ \begin{array}{r} 5 \ 1 \ 3 \ 1 \\ - 2 \ 6 \ 8 \ 5 \ 4 \\ \hline 3 \ 7 \ 8 \ 4 \ 3 \end{array} $			
Stage 2	<p>Introduce decimal place value counters and model exchange for subtracting between units of numbers.</p> <p>$5.74 - 2.25 = ?$</p> <p>Exchange 1 tenth for 10 hundredths.</p> <p>Now subtract the 5 hundredths.</p> <p>Now subtract the 2 tenths, then the 2 ones.</p>	<p>Children will draw their representations showing where they have exchanged.</p> <p>Bar Model</p> <p>Continue to use and focus on use as a tool for problem solving</p> <p>$18 - 3 = ?$</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">18</td> <td style="text-align: center;">?</td> <td style="text-align: center;">3</td> </tr> </table> <p>$18 - 3 = 15$</p>	18	?	3	<p>Children will continue to develop their understanding of column method subtraction. Calculations will become larger, include decimal places and require 0 to be added as a placeholder.</p> <p>6 digit - 6 digit</p> $ \begin{array}{r} 5 \ 1 \ 3 \ 1 \\ - 2 \ 6 \ 8 \ 5 \ 1 \ 4 \\ \hline 3 \ 7 \ 8 \ 4 \ 2 \ 3 \end{array} $ <p>Numbers with 3 decimal place</p> $ \begin{array}{r} 3 \ 1 \\ - 2 \ 1 \ 6 \ 2 \ 7 \ 3 \\ \hline 5 \ 2 \ 7 \ 5 \ 2 \ 5 \end{array} $ <p>Numbers with a different number of decimal places</p> $ \begin{array}{r} 6 \ 9 \ 2 - 2 \ 7 \ 5 \ 4 \\ \hline 4 \ 1 \ 6 \ 6 \end{array} $ <p>8 1 1</p> $ \begin{array}{r} 6 \ 9 \ 8 \ 0 \\ - 2 \ 7 \ 5 \ 4 \\ \hline 4 \ 1 \ 6 \ 6 \end{array} $
18	?	3				

MULTIPLICATION - KS1 (Years 1&2)

	Concrete	Pictorial	Abstract
Stage 1	<p>Repeated addition - Groups of multiple objects Children will count groups of the same number of objects and add them together. The children learn about grouping in practical contexts and through pictorial representations.</p> 	<p>Children draw representations to show counting in multiples and groups.</p>  <p>Double 4 is 8</p> 	<p>Children show multiplication as repeated addition. Children may provide pictorial representations to support.</p> 3×9 $3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 27$
Stage 2	<p>Arrays Children will be able to represent a multiplication calculation using an array and write the multiplication symbol within a number sentence. Children will also understand that multiplication can be carried out in any order (commutative).</p> 	<p>Children draw representations to show arrays.</p> 	<p>Children use arrays to show how to solve multiplication calculations. Children are able to show that multiplication can be done in any order (commutative).</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p> <p>$3 \times 5 = 15$</p> <p>$5 \times 3 = 15$</p> <p>Introduce \times sign and record as number sentence</p> <p>$7 \times 10 = 70$</p> <p>$4 \times 5 = 20$</p> <p>$5 + 5 + 5 = 15$</p> <p>$3 + 3 + 3 + 3 + 3 = 15$</p> <p>$5 \times 3 = 15$</p> <p>$3 \times 5 = 15$</p>
Stage 3	<p>Number line Children will understand the operation of multiplication as repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadstring concrete resources may be used to support conceptual understanding.</p> 	<p>Children show multiplication as repeated addition.</p> <p>$5 + 5 + 5 = 15$</p> <p>Introduce \times sign and record as number sentence</p> <p>$7 \times 10 = 70$</p> <p>$4 \times 5 = 20$</p>

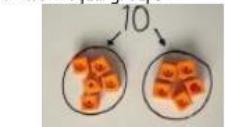
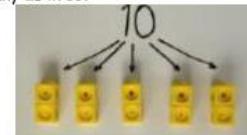
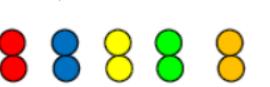
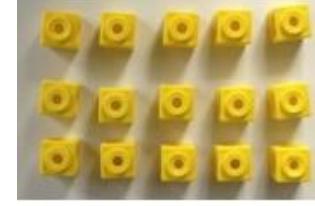
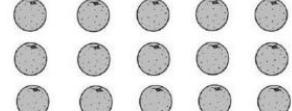
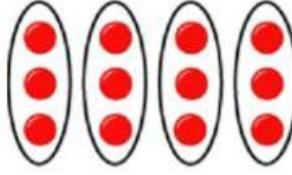
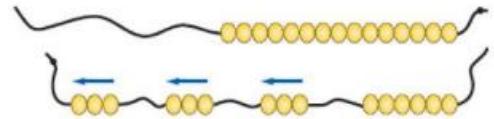
MULTIPLICATION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
Stage 1	<p>Number line - Consolidation Children will understand the operation of multiplication as repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	<p>Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadstring concrete resources may be used to support conceptual understanding.</p> 	<p>Children show multiplication as repeated addition. $5 + 5 + 5 = 15$</p> <p>Introduce \times sign and record as number sentence $7 \times 10 = 70$ $4 \times 5 = 20$</p>
Stage 2	<p>Partitioning Children will learn to multiply ones and tens separately before recombining the numbers back together. They can use Dienes cube of place value counters to achieve this.</p> <p>Double 24 = $24 + 24 = 48$</p>  <p> $24 + 24 = 48$ $20 + 20 = 40$ $4 + 4 = 8$ $40 + 8 = 48$ </p>	<p>Pictorial representations can be made using their concrete manipulatives as visuals. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown.</p>  <p> $13 \times 4 = (10 \times 4) + (3 \times 4)$ $= 40 + 12$ $= 52$ </p>	<p>Partition a number and then multiply each part before recombining it back together.</p>  <p> $27 \times 5 =$ $20 \times 5 = 100$ $7 \times 5 = 35$ $\underline{135}$ </p>
Stage 3	<p>Grid Method Show the links with arrays to first introduce the grid method.</p> <p>Move onto Dienes cubes to move towards a more compact method.</p> <p>Move on to place value counters to show how we are finding groups of a number. We are multiplying by 5 so we need 5 rows of that number.</p>  <p> $4 \times 5 = ?$ $4 \times 5 = 20$ </p>	<p>Bar Model Introduce as a model to show multiplication.</p> 	<p>Children should be able to draw the grid method for each multiplication. The grid method will be used to show how this relates to a formal written method.</p> <p>Grid method may then lead to the expanded method.</p>  <p> 36 $\times 4$ $\underline{24 \ (6 \times 4)}$ $\underline{120 \ (30 \times 4)}$ $\underline{144}$ </p>

MULTIPLICATION - Upper KS2 (Years 5 & 6)

	Concrete	Pictorial	Abstract		
Stage 1	<p>Concrete materials may be needed to support children's conceptual understanding. Dienes cubes and place value counters will support.</p> <p>When multiplying by 10,100,1000 initial concrete resources will be used to support understanding.</p> <p>Use place value equipment to multiply by 10, 100 and 1,000 by unitising.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 5px;"> $4 \times 1 = 4 \text{ ones} = 4$ $4 \times 10 = 4 \text{ tens} = 40$ $4 \times 100 = 4 \text{ hundreds} = 400$ </td> <td style="padding: 5px;"> </td> </tr> </table> <p>$4 \times 3 = 12$ $4 \times 300 = 1,200$</p> <p>$6 \times 4 = 24$ $6 \times 400 = 2,400$</p>	$4 \times 1 = 4 \text{ ones} = 4$ $4 \times 10 = 4 \text{ tens} = 40$ $4 \times 100 = 4 \text{ hundreds} = 400$		<p>Use place value equipment to compare methods.</p> <p>Method 1</p> <p>Method 2</p> <p>$4 \times 3,000 = 12,000$ $4 \times 200 = 800$ $4 \times 20 = 80$ $4 \times 5 = 20$ $12,000 + 800 + 80 + 20 = 12,900$</p>	<p>Long multiplication</p> <p>Children may wish to use 2 separate calculations to support their understanding. Reinforce language of place value when multiplying by multiples of 10. Extend to 3 or 4-digit numbers multiplied by a 2-digit number.</p> <p style="text-align: right;"> $\begin{array}{r} 23 \\ \times 13 \\ \hline 299 \end{array} \quad \begin{array}{r} 23 \\ + 69 \\ \hline 230 \end{array} \quad \begin{array}{r} 230 \\ \times 10 \\ \hline 230 \end{array} \quad \begin{array}{r} 23 \\ \times 23 \\ \hline 529 \end{array} \quad \begin{array}{r} 23 \\ \times 230 \\ \hline 5290 \end{array} \quad \begin{array}{r} 23 \\ \times 2300 \\ \hline 52900 \end{array}$ </p>
$4 \times 1 = 4 \text{ ones} = 4$ $4 \times 10 = 4 \text{ tens} = 40$ $4 \times 100 = 4 \text{ hundreds} = 400$					
Stage 2	<p>When multiplying decimals by 10,100,1000 initial concrete resources will be used to support understanding to show how exchanging can take place.</p> <p>$0.14 \times 10 = 1.4$</p>	<p>This pictorial grid method will support children's understanding of multiplying by 10, 100, 1000.</p> <p>$2.5 \times 10 = 25$ $2.5 \times 100 = 250$ $2.5 \times 1,000 = 2,500$</p>	<p>Use column multiplication, ensuring understanding of place value at each stage.</p> <p style="text-align: right;"> $\begin{array}{r} 1274 \\ \times 32 \\ \hline 2548 \\ 3822 \\ \hline 40768 \end{array} \quad 1274 \times 32 = 40,768 \end{math>$</p>		
Stage 3	<p>Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for those children struggling to grasp a concept and those with SEND.</p>	<p>Bar Model</p> <p>Develop use of bar model, focusing on its use as a problem-solving tool.</p> <p>$4 \times 5 = ?$</p> <p>$\{ \quad ? \quad \}$</p> <p>$4 \times 5 = 20$</p>	<p>Multiplication of Decimals</p> <p>Children should be taught to estimate an answer by rounding, carry out the calculation without the decimal, and then insert the decimals afterwards.</p>		

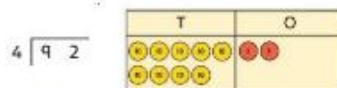
DIVISION - KS1 (Years 1&2)

	Concrete	Pictorial	Abstract
Stage 1	<p>Sharing and Grouping Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p> <p>Share 10 into 2 equal groups</p>  <p>How many 2s in 10?</p> 	<p>Use pictures to share objects. Use circles rather than dots to aid counting.</p> <p>Share 10 into 2 equal groups</p>  <p>How many 2s in 10?</p>  <p>Develop division as repeated subtraction on a number line.</p> <p>12 shared between 3 is 4</p>	<p>Children will be able to represent a division calculation using a pictorial method and write the division within a number sentence.</p> <p>$10 \div 2 = 5$</p> <p>Share 10 into 2 equal groups</p> 
Stage 2	<p>Arrays Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg:</p> $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	<p>Draw arrays to show how pictures are divided.</p>  	<p>Children will be able to represent a division calculation using an array and write the division within a number sentence</p> <p>$12 \div 3 = 4$</p> 
Stage 3	<p>Repeated addition and subtraction Children will understand the operation and repeated addition or subtraction using bead strings and number lines. This will support the pictorial element.</p> <p>$15 \div 3 = 5$</p> 		

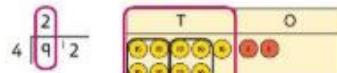
DIVISION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
Stage 1	<p>Division with no remainders through sharing. Use concrete materials to share into groups.</p> <p>$60 \div 3 = 20$ CONCRETE / PICTORIAL (Base 10 equipment) sharing</p> <p>$96 \div 3 = 32$</p> <p>$6 \text{ tens} \div 3 = 2 \text{ tens} = 20$</p>	<p>Consolidate learning from KS1 using diagrams of sharing and repeated subtraction and addition on a number line to make jumps</p> <p>Example without remainder: $40 \div 5$ Ask "How many 5s in 40?"</p> <p>Concrete methods could be represented pictorially within books to show understanding.</p>	<p>How many groups of 6 in 24?</p> <p>$24 \div 6 = 4$</p> <p>Abstract methods may be supported with pictorial methods within the children's books.</p>
Stage 2	<p>Division with remainder through sharing</p> <p>$14 \div 3 =$ Divide objects between groups and see how much is left over.</p> <p>Division no remainders - introduction to bus stop method</p> <p>Use place value equipment on a place value grid alongside short division. The model uses grouping.</p>	<p>Students can continue to use drawn diagrams with circles to help them divide numbers into equal groups. Remainders will be seen by not fitting into a whole group.</p> <p>Draw dots and group them to divide an amount and clearly show a remainder.</p> <p>Example without remainder: $40 \div 5$ Ask "How many 5s in 40?"</p> <p>Example with remainder: $38 \div 6$</p>	<p>Children will begin to move onto division with remainders. A number sentence will support any abstract written calculation by using pictorial method to support.</p> <p>$29 \div 8 = 3 \text{ REMAINDER } 5$</p> <p>↑ ↑ ↑ ↑ dividend divisor quotient remainder</p> <p>Short division Children will begin to use the formal written method of division without remainders. This will only come after a clear concept is understood using manipulatives.</p> <p>Dividing by 2,3,4, and 5</p>

Division with remainders - Bus stop



First, lay out the problem.

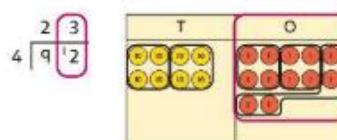
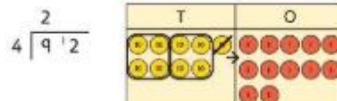


How many groups of 4 go into 9 tens?

2 groups of 4 tens with 1 ten left over.

Exchange the 1 ten left over for 10 ones.

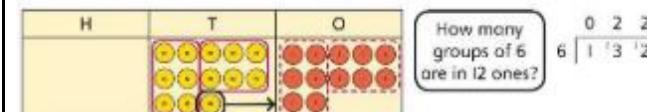
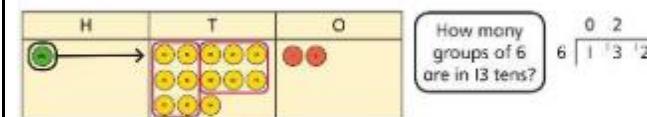
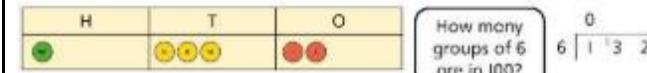
We now have 12 ones.



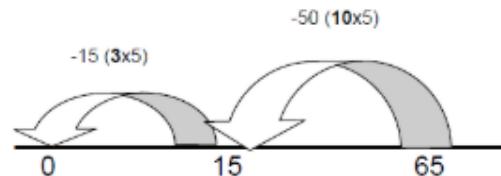
How many groups of 4 go into 12 ones?

3 groups of 4 ones.

Pictorial representations can be used to support any concrete manipulatives.



Continue to use blank number lines as appropriate, using multiples of the divisor.
 $65 \div 5 = 13$



Chunking

Chunking is repeated subtraction of the divisor and multiples of the divisor.

$$73 \div 5$$

$$\begin{array}{r}
 5 \overline{)73} \\
 -50 \\
 \hline
 23 \\
 -20 \\
 \hline
 3
 \end{array}$$

(10×5)
 (4×5)
 $10 + 4 = 14$

How many 5s have been subtracted?
14 sets of 5, with 3 left over.

Answer: $73 \div 5 = 14 \text{ r}3$

Bus Stop Method for division

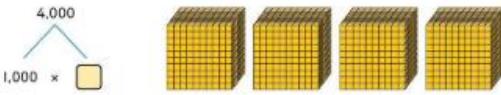
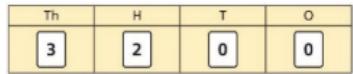
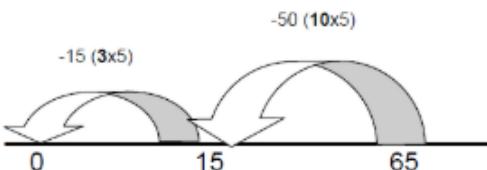
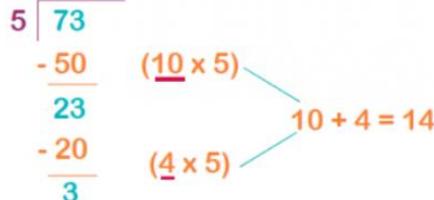
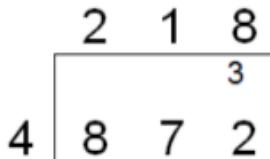
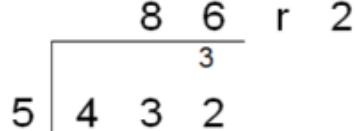
Begin with divisions that divide equally with no remainder.

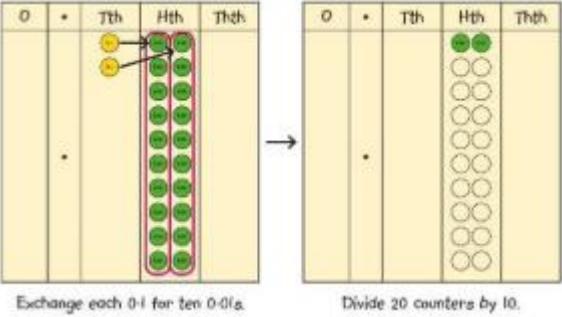
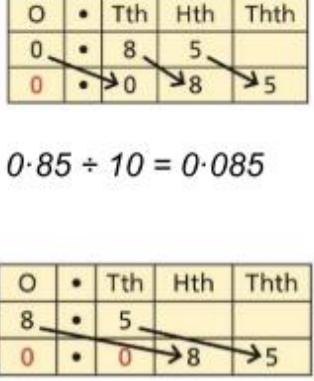
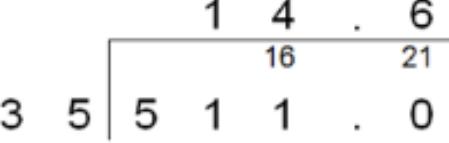
$$\begin{array}{r}
 2 \ 1 \ 8 \\
 \hline
 3 \\
 4 \overline{)8 \ 7 \ 2}
 \end{array}$$

Move onto divisions with a remainder.

$$\begin{array}{r}
 8 \ 6 \ r \ 2 \\
 \hline
 3 \\
 5 \overline{)4 \ 3 \ 2}
 \end{array}$$

DIVISION - Upper KS2 (Years 5 & 6)

	Concrete	Pictorial	Abstract
Stage 1	<p>Dividing whole numbers by 10, 100 and 1,000 Use place value equipment to support unitising for division. $4,000 \div 1,000$</p>  <p>4,000 is 4 thousands.</p> <p>$4 \times 1,000 = 4,000$</p> <p>So, $4,000 \div 1,000 = 4$</p> <p>Concrete and pictorial representations may still be required to support the formal method of division (Bus Stop) - Go back to LKS2 to consolidate learning.</p>	<p>Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.</p>  <p>$3,200 \div 100 = ?$</p> <p>3,200 is 3 thousands and 2 hundreds.</p> <p>$200 \div 100 = 2$</p> <p>$3,000 \div 100 = 30$</p> <p>$3,200 \div 100 = 32$</p> <p>So, the digits will move two places to the right.</p> <p>Continue to use blank number lines as appropriate, using multiples of the divisor. $65 \div 5 = 13$</p> 	<p>Chunking Chunking is repeated subtraction of the divisor and multiples of the divisor.</p> <p>$73 \div 5$</p>  <p>How many 5s have been subtracted? 14 sets of 5, with 3 left over.</p> <p>Answer: $73 \div 5 = 14 \text{ r}3$</p> <p>Bus Stop Method for division</p> <p>Begin with divisions that divide equally with no remainder.</p>  <p>Move onto divisions with a remainder.</p> 

<p>Dividing decimals by 10, 100 and 1,000 Use place value counters to represent dividing by 10, 100, 1000. Represent division using exchange on a place value grid.</p> <p>Stage 2</p> <p>0.2 is 2 tenths. 2 tenths is equivalent to 20 hundredths. 20 hundredths divided by 10 is 2 hundredths.</p>  <p>Exchange each 0.1 for ten 0.01s. Divide 20 counters by 10.</p>	<p>Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.</p> <p>Stage 3</p> <p>$0.85 \div 10 = 0.085$</p> <p>$8.5 \div 100 = 0.085$</p> 	<p>Finally move into decimal places to divide the total accurately using a formal method for division (Bus stop)</p> <p>Stage 3</p> 
<p>Long Division - Abstract Method A colour-coded system can be used to clarify the process to children as on the left.</p> <p>In addition to this the children should be taught an expanded variant of Bus Stop, with the additional use of skeleton tables for the divisor, eg:</p> <p>27 54 81 108 135 162</p>	<p>Stage 3</p> 