



Rayner Stephens
HIGH SCHOOL

Curriculum

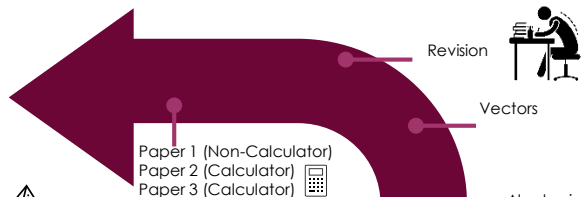
Intent

for

Maths

At Rayner Stephens High School, we believe that everyone can do maths. The intent of the mathematics curriculum is to provide students with a high-quality and ambitious curriculum which will allow all students to achieve their mathematical potential and prepare them well for everyday life and future employment. Through mathematics lessons, we promote mathematical thinking which will encourage students to develop conceptual understanding, to establish links between the different disciplines within maths and to provide the opportunity to apply this understanding to solve increasingly complex problems. In KS3, students are introduced to topics in mathematics using a concrete, pictorial, abstract approach to allow students to develop their fluency, reasoning and problem-solving skills. Topics are interleaved to allow students to improve their previous learning and allow them to develop application and skill links between the different areas of mathematics. In KS3, students are exploring topics in order to create the building blocks to prepare them for their GCSE studies in Years 10 and 11. Covering the disciplines of number, algebra, geometry, ratio, proportion, data handling and probability, students are given the opportunity to retrieve, affirm and extend their understanding as they progress on their mathematics journey through KS3 and KS4. Students will be encouraged to become fluent in the fundamentals, to be able to reason mathematically, by problem solving and be able to develop an argument or justification using mathematical language.

Mathematics Learning Journey Higher Tier

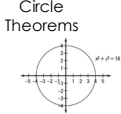


Vectors

Algebraic Proof

Transformation of Graphs

Functions



Paper 1 (Non-Calculator)
Paper 2 (Calculator)
Paper 3 (Calculator)

$a^2 + b^2 = c^2$
Pythagoras' Theorem
Surface Area
Coordinate Geometry
Probability
Angles
Arcs and Sectors
Averages
Similar Shapes in 2D and 3D
Quadratics
Data Handling and Histograms

YEAR 11

Simultaneous Equations
Probability
Frequency Diagrams
Data Handling
Volume
Circles
 $A = \pi r^2$

Bearings
Arcs and Sectors
Trigonometry
Volume
Compound Measures
Proportion
Simultaneous Equations
Iteration
Velocity Time Graphs
Circle Geometry

Surface Area
Graphs
Volume
Circles
Compound Measures

Forming and Solving
Expanding Brackets
Fractions
Product of Primes
Error Intervals
Two-way Tables
Angles Parallel Lines
Changing the Subject
Inequalities
Percentages
Forming and Solving Equations

YEAR 10

Coordinate Geometry
Standard Index Form
Solving Equations

Bearings
Factorising
Sequences
Ratio
Estimation
Frequency Trees
Constructions

Standard Index form
Indices
Fractions and Percentages

Measuring Angles
Angles in Polygons
Measurement
Scale
Trigonometry
Forming and Solving Equations

Indices
Sequences
Tables and Probability
Working in the Cartesian Plane
Multiplicative change
Addition and Subtraction of Fractions
Solving problems with Multiplication and Division

Angle Rules
Proportional Reasoning
Area
Pythagoras' Theorem

YEAR 8

Prime Numbers and Proof

Brackets, Equations and Inequalities

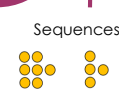
Representing data
Multiplying and dividing fractions
Ratio and Scale
Operations and Equations with Directed Number

Sets and Probability

YEAR 7

Sequences
Equality and Equivalence

Understand and Use Algebraic Notation
Place Value and Ordering Integers and Decimals
Solving Problems with Addition and Subtraction
Fraction and Percentage of Amounts
Addition and Subtraction of Fractions
Developing Geometric Reasoning



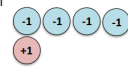
Equality and Equivalence

Fraction, Decimal and Percentage Equivalence

Solve Problems with Multiplication and Division

Operations and Equations with Directed Number

Measuring and Using Geometric Notation



welcome



Mathematics Learning Journey Foundation Tier



Revision

Paper 1 (Non-Calculator)
Paper 2 (Calculator)
Paper 3 (Calculator)

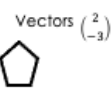
Simultaneous Equations

Venn Diagrams

Probability Trees



Probability



Vectors $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$

YEAR 10



Constructions

Further Probability

Equations in context

YEAR 11

$$a^2 + b^2 = c^2$$

Pythagoras' Theorem



Averages

Scatter Diagrams

Coordinate Geometry

Compound Measures

Transformations



Angles

Circles

Surface Area

Averages

Coordinate Geometry

Compound Measures

Transformations



Averages

Data Handling

Volume



Circles

$$A = \pi r^2$$

Compound Measures

Frequency Diagrams

Bearings

Trigonometry

Arcs and Sectors

Volume

Frequency Diagrams

Pie Charts

Graphs

Congruence and Similar Shapes

Vectors $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$



Surface Area

Angles Parallel Lines

Changing the Subject

Forming and Solving

Inequalities

Expanding Brackets

Percentages

Fractions

Product of Primes

Error Intervals

Two-way Tables



Graphs

Angles Parallel Lines

Changing the Subject

Forming and Solving

Inequalities

Expanding Brackets

Percentages

Fractions

Product of Primes

Error Intervals

Two-way Tables

Compound Measures

Bearings

Factorising

Sequences

Ratio

Estimation

Frequency Trees

Constructions

Further Probability

Coordinate Geometry

Standard Index Form

Solving Equations

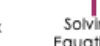
Index Laws

HCF and LCM

Frequency Trees

Constructions

Further Probability



Measuring Angles

Angles in Polygons

Measurement

Scale

Trigonometry

Forming and Solving Equations

Further Probability

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Fractions and Percentages

Sequences

Tables and Probability

Working in the Cartesian Plane

Multiplicative change

Addition and Subtraction of Fractions

Solving problems with Multiplication and Division

Equations in context



Fractions and Percentages

Angle Rules

Proportional Reasoning

Area

Pythagoras' Theorem

Prime Numbers and Proof



Indices

Sequences

Tables and Probability

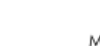
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Prime Numbers and Proof



Brackets, Equations and Inequalities

Representing data

Multiplying and dividing fractions

Ratio and Scale

Operations and Equations with Directed Number

Sets and Probability

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Place Value and Ordering Integers and Decimals

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Fraction and Percentage of Amounts

Addition and Subtraction of Fractions

Developing Geometric Reasoning

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Developing Geometric Reasoning

Understand and Use Algebraic Notation

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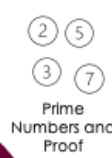
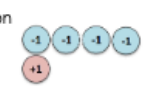
Solve Problems with Multiplication and Division

Operations and Equations with Directed Number

Measuring and Using Geometric Notation

Developing Geometric Reasoning

welcome



Year 7 - Mathematics

Curriculum intent	<p>Through mathematics lessons we promote mathematical thinking to allow all students to achieve their mathematical potential and engage in the study of mathematics. Using a mastery style approach to mathematics allows all students to develop their fluency, reasoning and problem solving using the concrete, pictorial, abstract (CPA) approach. As students progress through their learning topics from previous learning will be interleaved into future learning so students develop application and skill links between different areas of mathematics.</p> <p>In year 7, students start their journey with algebraic thinking, students will further develop pattern spotting, and develop a deep understanding of the basic algebraic forms and fundamentals. Much of this work will be developed using physical manipulatives and further their numerical reasoning. Students will then explore further the concepts of equivalence and equality in both algebraic and numerical form, this will link to real life concepts and explore associated topics to apply these skills.</p> <p>As year 7 continues students will explore new areas of mathematics linked to the four operations and fractions allowing students to develop and apply these central concepts to different areas of mathematics, including frequency diagrams, averages and area. Students will develop their application of calculations using formal methods, please refer to our calculation policy for more details.</p> <p>In Term 3 students will build on their KS2 skills in early work in probability and number proof, developing their ability to justify and reason deductively in both number and algebra.</p>					
Term	Autumn 1	Autumn 2	Spring 1	Spring 2	Summer 1	Summer 2
Knowledge	<ul style="list-style-type: none"> • Sequences • Understand and use algebraic notation 	<ul style="list-style-type: none"> • Equality and Equivalence • Place value and ordering integers and decimals 	<ul style="list-style-type: none"> • Fraction, decimal and percentage equivalence • Solve problems with addition and subtraction 	<ul style="list-style-type: none"> • Solve problems with multiplication and division • Fraction and percentage of amounts • Operations and equations with directed number 	<ul style="list-style-type: none"> • Operations and equations with directed number • Addition and subtraction of fractions 	<ul style="list-style-type: none"> • Sets and probability • Prime numbers and proof
Term	Autumn 1	Autumn 2	Spring 1	Spring 2	Summer 1	Summer 2
Skills	<ul style="list-style-type: none"> • Moving between different numerical, graphical and diagrammatic representations 	<ul style="list-style-type: none"> • Simplify & manipulate algebraic expressions to maintain equivalence 	<ul style="list-style-type: none"> • Represent decimals and fractions on a number line • Compare quantities using fractions, 	<ul style="list-style-type: none"> • Use the properties of multiplication and division, including the commutative 	<ul style="list-style-type: none"> • Understand and use multiple representations of directed numbers 	<ul style="list-style-type: none"> • Identify sets and create and represent them on Venn diagrams

	<ul style="list-style-type: none"> • Make and test conjunctures about patterns • Recognise & generate terms. • Use a calculator to check accuracy • Use algebra to generalise the structure of arithmetic • Formulate mathematical relationships • Recognise and use relationships between operations, including inverse operations • Use and interpret formal algebraic notation • Substitute into expressions • Generate terms of a sequence • Produce graphs of linear functions of one variable 	<ul style="list-style-type: none"> • Use approximation through rounding to estimate answers • Use algebraic methods to solve linear equations with one variable. • Use place value for decimals • Understand and use place value for decimals, measures & integers of any size • Use mathematical symbols for equality and inequality • Compare and order any number up to one billion • Describe, interpret and compare the median & range • Use powers of ten in calculations • Write numbers in standard form 	<p>decimals and percentages</p> <ul style="list-style-type: none"> • Express one quantity as a fraction of another • Use and interpret simple pie charts • Using diagrams to represent any fraction as a diagram, on a number line • Identify and use equivalent fractions • Understanding fractions as division • Convert fluently between simple fractions, decimals and percentages • Understanding fractions greater than a whole • Use the properties of addition and subtraction, including the associative law of arithmetic • Develop mental strategies for addition and subtraction • Use formal written methods for addition and subtraction, applied to positive integers and decimals • Recognise and use the most appropriate method: mental strategies, formal written or calculator 	<p>associative laws of arithmetic</p> <ul style="list-style-type: none"> • Understand and use factors and multiples • Multiply and divide integers and decimals by powers of 10 • Convert between different metric units • Use formal written methods for multiplication and division, applied to positive integers and decimals • Understand and use order of operations • Find fraction and percentage of amounts using mental methods and a calculator • Solve fraction and percentage problems • Understand and use multiple representations of directed numbers 	<ul style="list-style-type: none"> • Perform calculations that cross zero • Complete calculations using all four operators involving direct numbers • Use of a calculator with directed numbers • Evaluate algebraic expressions involving directed numbers • Understand and use two step equations • Explore powers and roots. • Understand representations of fractions • Understand and use equivalent fractions • Convert between mixed numbers and fractions • Add and subtract proper fractions in any form • Add and subtract improper fractions and mixed numbers • Use fractions in algebraic contexts • Use equivalence to add and subtract decimals, percentages and fractions • Add and subtract simple algebraic fractions. 	<ul style="list-style-type: none"> • Understand and use intersection and the union of sets • Know and use the vocabulary of probability • Generate sample spaces for an event • Know the sum of probabilities of all outcomes is 1 • Calculate the probability of single events • Understand and use the probability scale. • Identify and use factors and multiples • Find common factors and multiples including HCF & LCM • Write a number as a product of its prime factors • Make and test conjectures, using counter examples to disprove a conjecture
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			<ul style="list-style-type: none"> • Solve problems involving perimeter, financial maths, timetables, frequency diagrams • 			
Assessments	<ul style="list-style-type: none"> • 2unit assessments 	<ul style="list-style-type: none"> • 2 unit assessments • Term Assessment 	<ul style="list-style-type: none"> • 2 unit assessments 	<ul style="list-style-type: none"> • 3 unit assessments 	<ul style="list-style-type: none"> • 2 unit assessments • Term Assessment 	<ul style="list-style-type: none"> • 2 unit assessments
Curiosity	<ul style="list-style-type: none"> • Work on your IQ and test your pattern spotting skills https://www.intelligentest.com/questions/pattern-recognition/index.html • Enter the National Cipher Challenge (Oct-Jan) https://www.cipherchallenge.org/ • Research the famous Fibonacci sequence. Can you summarise your research in a poster or factsheet? • Try following sequences to solve the game about (app also available) http://gameaboutsquares.com/ 	<ul style="list-style-type: none"> • Try out some of the UKMT Junior Challenge questions – some students get the chance to enter in Feb! https://www.interactive-maths.com/ukmt-random-question-generator.html • Investigate palindromes – here's a short article to get you started https://nrich.maths.org/2574 • Equivalence pairs – can you get to cards face down Level 5? https://nrich.maths.org/1249 	<ul style="list-style-type: none"> • If you've been selected for the UKMT Junior Challenge questions – get some extra practice in! https://www.interactive-maths.com/ukmt-random-question-generator.html • You're throwing a birthday party for your friend. What will you do and how much will it cost? • In newspapers and magazines find fractions decimals or percentages in them and convert all the values you find. 	<ul style="list-style-type: none"> • Make a how to use your calculator guide! It will come in helpful for future learning • You're planning an epic journey, use Google Earth to figure out where you will travel, and how far in total you will travel. Can you give distances in cm, m and km? 	<ul style="list-style-type: none"> • Can you investigate average temperatures across the work, can you find very cold cities/places and compare them to very warm cities/places, Work out the differences • Try to keep practising your negative number skills! https://www.cimt.org.uk/projects/mepres/book7/bk7i15/bk7_15i1.htm & https://www.cimt.org.uk/projects/mepres/book7/bk7i15/bk7_15i2.htm • Can you design a board game which tests your fraction arithmetic? 	<ul style="list-style-type: none"> • Can you sort shapes based on their properties into a Venn diagram? https://mathsframe.co.uk/en/resources/resource/83/sort-shapes-venn • Can you test the hypotheses? https://nrich.maths.org/6033 • Can you explain why every year must contain at least one Friday the thirteenth? What is the greatest number of Friday the thirteenth that can fall in one year?

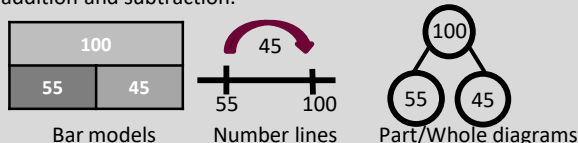
Year 7 Mathematics Knowledge Organiser – Solving Problems with Addition and Subtraction

Key Vocabulary:

1	Addition	To find the total of two or more numbers. Other words to describe addition include: 'add', 'plus', 'sum'.
2	Subtraction	To find the difference between two numbers. To find out how many are left when some are taken away.
3	Commutative	Changing the order of the operations does not change the result. This applies to addition and multiplication.
4	Integer	A whole number that can be positive, negative or zero.
5	Decimal	A number with a decimal point in it. Can be positive or negative.
6	Associative	When you add or multiply you can do so regardless of how the numbers are grouped.
7	Inverse	To perform the opposite operation. For example, the inverse of addition is subtraction.
8	Balance	The amount of money in an account.
9	Credit	Money that goes into an account.
10	Debit	Money that leaves an account.
11	Standard Form	A way to write very big numbers or very small numbers with one number before the decimal point, multiplied by a power of 10. It allows saying and calculating with very big numbers or very small numbers to be easier to handle.

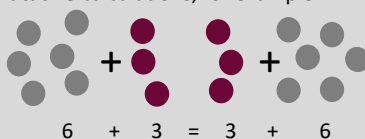
12 Addition and Subtraction

We can use different modelling methods to represent addition and subtraction.



13 Addition is Commutative

Addition and multiplication can be done in any order; these are **commutative** calculations, for example:



However when subtracting the order does matter, for example:

$$9 - 3 = 6 \quad \text{which is not the same as} \quad 9 - 6 = 3$$

14 Formal Written Methods

Column method:

$$\begin{array}{r} 4261 \\ 3037 \\ + 6422 \\ \hline 13720 \\ \hline 1 \quad 1 \quad 1 \end{array}$$

$$863 - 75$$

$$\begin{array}{r} 863 \\ - 75 \\ \hline 788 \end{array}$$

Remember the place value of each column. When adding you may need to include the exchange in the next column. When subtracting you may need to exchange 10 units to the column below in order to be able to subtract.

15 Formal Methods with Decimals

Column method:

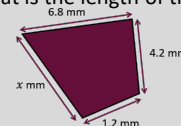
$$7.83 + 16.6$$

Use columns as when adding and subtracting integers. You may find it useful to add a place holder 0 to empty places in the columns. Remember the decimal point acts as a placeholder and aligns the other values.

$$\begin{array}{r} 7.83 \\ + 16.60 \\ \hline 24.43 \\ \hline 1 \quad 1 \end{array}$$

16 Solve Problems with Perimeter

The perimeter is the length around the outside of a shape. For example, the perimeter of the quadrilateral is 16.7 mm. What is the length of the side marked x ?



$$\begin{aligned} P &= 6.8 + 4.2 + 1.2 + x \\ 16.7 &= 12.2 + x \\ x &= 16.7 - 12.2 \\ x &= 4.5 \text{ mm} \end{aligned}$$

17 Solve Problems with Finance

Below is an example of a bank statement.

Date	Description	Credit	Debit	Balance
1 Mar	Opening Balance			254.76
3 Mar	Wages	1,402.11		1,656.87
4 Mar	Phone Bill		34.45	1,622.42

Here we can see the balance is the amount already in the bank account at the beginning of the month. Wages are a credit, as that amount is paid into the account. The phone bill is a debit, so that amount is subtracted from the balance.

18 Tables and Timetables

Distance Tables:

Aberdeen	Cambridge	Leeds	Truro
490			
355	149		
667	343	371	

A distance table shows the distance between two places.

To find the distance between Aberdeen and Leeds follow the arrows to where their row and column intersect to find the distance.

19 Frequency Trees

A frequency tree is made up from part-whole models. One piece of information leads to another.

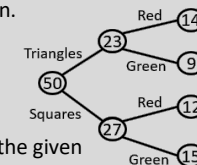
For example: There are 50 plastic triangles and squares in a bag. All of the shapes are red or green.

There are 23 triangles.

12 of the squares are red.

There are 24 green shapes.

To use this information to complete the frequency tree, start by filling in the given information and then fill in the gaps!



19 Standard Form

Writing large numbers in standard form.

$$\begin{aligned} 4,000 &= 4 \times 1,000 \\ &= 4 \times 10^3 \end{aligned}$$

Standard form

Adding numbers in standard form.

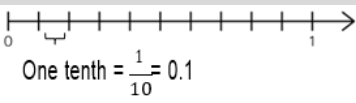
$$\begin{aligned} \text{For example:} \\ 3 \times 10^4 + 4 \times 10^4 \\ &= 30,000 + 40,000 \\ &= 70,000 \\ &= 7 \times 10^4 \end{aligned}$$

Year 7 Key Stage 3 Knowledge Organiser Fraction, decimal and percentage equivalence.

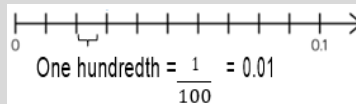
Key Vocabulary:

1	Fraction	A number that compares equal parts of a whole. Each part of the whole is a fraction.
2	Numerator	The top number in a fraction. This tells us how many of the equal parts are required.
3	Denominator	The bottom number in a fraction. It tells us how many equal parts the whole has been split into.
4	Per cent	Parts per hundred
5	Equivalent	Equal in value. E.g. 2+5 is equivalent to 4+1
6	Quotient	The result of a division.
7	Convert	To change from one form to another. E.g. to convert from a fraction to a percentage.
8	Pie chart	A graph in which a circle is divided into sectors that each represent a proportion of the whole.
9	Sector	A part of a circle formed by two radii and a fraction of the circumference.

10 Tenths and hundredths on a number line

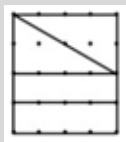


One whole split into 10 equal parts



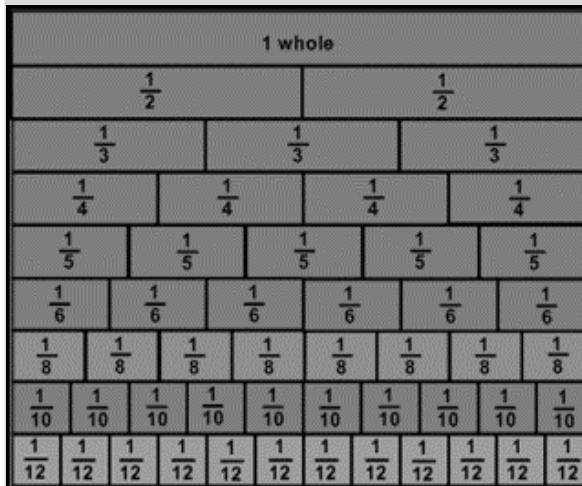
One whole split into 100 equal parts

11 Fractions on a diagram



The denominator is represented by equally sized parts – this shape is split into quarters

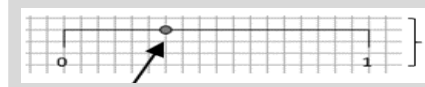
12 Equivalent Fractions



For Example

$$\frac{1}{2} = \frac{2}{4} = \frac{3}{6} = \frac{5}{10}$$

13 Fractions on a number line



This point is the 6th part. 6 is the numerator

One whole split into 18 equal parts. 18 is the denominator

$$\frac{6}{18} = \frac{3}{9} = \frac{1}{3}$$

14 Convert fractions. Decimals and Percentages

$$\frac{70}{100} \rightarrow \text{This also means } 70 \div 100 \rightarrow \begin{matrix} 70 \\ \text{hundredths} \\ = 70\% \end{matrix}$$

Using a calculator

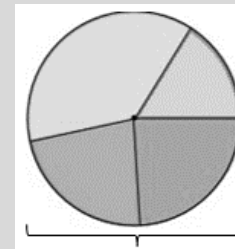


This will give you the answer in the simplest form

S ⇌ D Convert to decimal

X 10 converts to percentage

15 Simple Pie Charts



Split into 10 parts
10% = 36°

Split into 2 parts
50% = 180°

Split into 5 parts
20% = 72°

A pie chart has 360° so all FDP calculations are out of 360.

Year 7 - Spring Term Knowledge Organiser - Solving Problems with Multiplication and Division

Key Vocabulary:		
1	Multiply	The result of multiplying a number by an integer. The times tables of a number
2	Product	The result of a multiplication calculation.
3	Multiples:	Found by multiplying any number by positive integers
4	Factor	Integers that multiply together to get another number.
5	Quotient	The result of a division
6	Divisor	The number we divide by
7	Mean	The average of the all values, whereby all of the values are added together and then divided by the number of values.
8	Equivalent	Something that is essentially the same or equal to something else

9 Factors

A number that divides exactly into another number without a remainder. It is useful to write factors in pairs

Factors of 10
1, 2, 5, 10

The number itself is always a factor

Factors of 4 Factors of 36
1, 2, 4 1, 2, 3, 4, 6, 9, 12, 18, 36

10 Multiples

The result of multiplying a number by an integer. The times tables of a number

Lowest Common Multiples LCM of 9 and 12 The first time their multiples match

9	9, 18, 27, 36, 45, 54
12	12, 24, 36, 48, 60

LCM = 36

11 Multiply and divide integers and decimals by powers of 10

A number that divides exactly into another number without a remainder. It is useful to write factors in pairs

$3 \times 100 = 300$

$0.03 \times 100 = 3$

12 Convert metric units

When we convert from big unit to small unit we multiply and if we convert from small unit to big unit we divide.

13 Use formal methods to multiply integers

Long multiplication column

$$\begin{array}{r}
 326 \times 32 = 10,432 \\
 \begin{array}{r}
 \text{Th} \quad \text{H} \quad \text{T} \quad \text{O} \\
 \times \\
 \hline
 652 \\
 +9780 \\
 \hline
 10432
 \end{array}
 \end{array}$$

Make the unit 0 then carry on multiplying

14 Use formal methods to multiply decimals

Multiply 0.03 by 1.1 = 0.033

Multiply 0.03 by 1.1 = 0.033

the answer should have the same number of decimal places as are in both the numbers you are multiplying.

Multiply without decimal points: $3 \times 11 = 33$

0.03 has 2 decimal places, and 1.1 has 1 decimal place, so the answer has 3 decimal places: 0.033

15 Use formal methods to divide integers and decimals.

$$3584 \div 7 = 512$$

Short division

$$\begin{array}{r}
 512 \\
 7 \overline{) 3584} \\
 \underline{35} \\
 8 \\
 \underline{8} \\
 4 \\
 \underline{4} \\
 0
 \end{array}$$

Division with decimals

The placeholder in division methods is essential – the decimal lines up on the dividend and the quotient

$$24 \div 0.02 \longrightarrow 24 \div 0.2 \longrightarrow 240 \div 2$$

All give the same solution as represent the same proportion .Multiply the values in proportion until the divisor becomes an integer.

16 Order of operations

Break down the calculation using the order of operations.

$$6 \times 4 + 8 \times 2$$

$$24 + 16 = 40$$

$10 - 3 + 5 \longrightarrow 10 - 3 \longrightarrow 7 + 5$

Year 7 - Sequences - Knowledge Organiser- Autumn Term


Key Vocabulary:			8	Describe and continue a sequence given diagrammatically.	11	Recognise the difference between linear and non-linear sequences..									
1	Sequence	A number or picture pattern with a specific rule.	<div style="border: 1px solid black; padding: 5px; display: inline-block;">Count the number of circles or lines in each image</div>			<p>A linear sequence has a constant difference between each term.</p> <p>Example:</p>									
2	Pattern	A systematic arrangement of numbers, shapes or other elements according to a rule	9			Predict and check the next term(s) of a sequence									
3	Term:	Each value in a sequence is called a term.				<p>A non linear sequence has not a constant difference between each term.</p> <p>Example:</p>									
4	Linear / arithmetic sequence	Increase by addition or subtractions and the same amount each time. Produces a straight line when represented as a graph				12		Continue non-linear sequences							
5	Non-linear sequence	Do not increase by a constant amount – quadratic, geometric and Fibonacci. - Do not plot as straight lines on a graph. - The differences between terms can be found by addition, subtraction, multiplication or division.	10			1, 2, 4, 8, 16...									
6	Numerical	Written or shown as numbers.	<p>Position the place in the sequence</p>			<p>How do I know this is a non-linear sequence?</p> <p>It <u>increases by multiplying</u> the previous term by <u>2</u> – this is a geometric sequence because the constant is <u>multiply by 2</u>.</p> <p>You need at least 4 terms to find the constant</p>									
7	Arithmetic sequence	A sequence that increases or decreases by the same number between each term.	<p>In a table:</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>Position</th><td>1</td><td>2</td><td>3</td></tr> <tr><th>Term</th><td>3</td><td>5</td><td>7</td></tr> </table> <p>Graphically:</p>			Position	1	2	3	Term	3	5	7	<p>How do I continue the sequence?</p> <p>You continue to repeat the same difference through the next positions in the sequence.</p>	
Position	1	2	3												
Term	3	5	7												
8	Difference	The common difference of an arithmetic sequence is the difference between two consecutive terms.	<p>13</p> <p>Explain the term-to-term rule</p>			<p>Try to explain this in full sentences, not just with mathematical notation.</p> <p>Use key maths language – doubles, halves, multiply by two, add four to the previous term etc.</p>									
9	Graphical	Represented as a graph.	<p>Because the terms increase by the same addition each time this is linear – as seen in the graph</p>			<p>Must say which number the sequence begins with</p> <p>The next term is found by tripling the previous term. The sequence begins at 4</p>									

Year 7 Mathematics Knowledge Organiser – Algebraic Notation

Key Vocabulary:

1	Operation	A mathematical process. The most common operations are add, subtract, multiply and divide (+, -, ×, ÷) but there are many more, such as square, square root, etc.
2	Inverse Operation	The operation that reverses the effect of another operation. Addition and subtraction are inverse operations. Multiplication and division are inverse operations.
3	Commutative	A calculation is commutative when we get the same answer no matter which order we put the numbers in. Addition and multiplication are commutative.
4	Expression	Numbers, symbols and operators (such as + and ×) grouped together that show the value of something.
5	Variable	A symbol for a value we do not know yet, usually a letter like x or y (but can be others). A variable could be a single value or it could have many values.
6	Substitute	To replace letters with numerical values.
7	Evaluate	To calculate the numerical value of something.


8 Single Function Machines
We can use function machines to find the input and/or the output, using **inverse operations**.

Input →  Output


9 Using Letters to Represent Numbers

- Addition and multiplication can be done in any order; these are **commutative** calculations, for example:
 $5 + 5 + 5$
 3×5
 5×3
- We can represent 4 lots of y in the following ways:
 $y + y + y + y$
 $y \times 4$
 $4 \times y$
 $4y$
- We can represent 20 shared into h number of groups:
 $20 \div h$

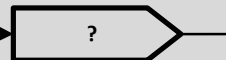
10 Single Function Machines (Algebra)

Input →  Output

a → $10a$
 $3c$ → $30c$

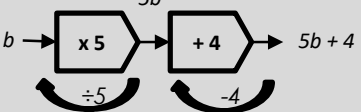
←  ←

11 Finding Functions from Expressions
We can use function machines to find the relationship between the input and output. Sometimes there could be a number of possible functions...

$7x$ →  $14x$

...possible functions could be $+ 7x$ or $\times 2!$

12 Two Step Function Machines

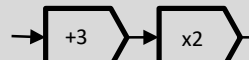
b →  $5b + 4$

(Arrows below the boxes indicate inverse operations: $\div 5$ and $- 4$)

13 Substituting into Expressions

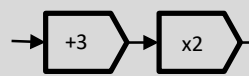
If $y = 7...$
 $4y$ means 4 lots of y, so the expression is asking for 4 lots of 7
 4×7 OR $7 + 7 + 7 + 7$ OR $7 \times 4 = \underline{28}$
 $y - 2$ means y subtract 2, so $7 - 2 = \underline{5}$

If $x = 10...$
 $2(x+3)$ means take the input, add 3, then multiply by 2

input →  output

$10 + 3 = 13$ $13 \times 2 = \underline{26}$

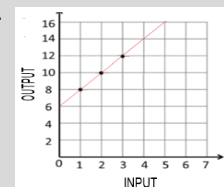
14 Representing Functions Graphically
Using the function $2(x + 3)$

input →  output

To represent graphically, the input becomes x coordinates and the output becomes y coordinates.
 $y = 2(x + 3)$

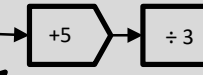
INPUT (x)	1	2	3
OUTPUT (y)	8	10	12


This becomes a coordinate pair.



15 Finding Functions from Expressions

$\frac{f+5}{3}$ is different to the expression $\frac{f}{3} + 5$

f →  → $\frac{f+5}{3}$

f →  → $\frac{f}{3} + 5$

Callouts: "I add 5 then divide by 3" (pointing to the first machine), "I divide by 3 then add 5" (pointing to the second machine).

Sometimes it helps to explain the expression in words first!

16 Forming a Sequence
The term that we want to find in the sequence is the input value. The answer we get when we substitute the input value gives us the output values, which become our sequence.

INPUT	1	2	3	
OUTPUT	8	10	12	← This is the sequence.

Year 7 - Summer Term Knowledge Organiser - Solving Problems with Multiplication and Division

Key Vocabulary:

1	Multiply	The result of multiplying a number by an integer. The times tables of a number
2	Product	The result of a multiplication calculation.
3	Multiples:	Found by multiplying any number by positive integers
4	Factor	Integers that multiply together to get another number.
5	Quotient	The result of a division
6	Divisor	The number we divide by
7	Mean	The average of the all values, whereby all of the values are added together and then divided by the number of values.
8	Equivalent	Something that is essentially the same or equal to something else

9 Factors

A number that divides exactly into another number without a remainder. It is useful to write factors in pairs

Factors of 10

1, 2, 5, 10

The number itself is always a factor

Factors of 4

1, 2, 4

Factors of 36

1, 2, 3, 4, 6, 9, 12, 18, 36

10 Multiples

The result of multiplying a number by an integer. The times tables of a number

Lowest Common Multiples

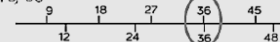
LCM of 9 and 12

The first time their multiples match

9: 9, 18, 27, 36, 45, 54

LCM = 36

12: 12, 24, 36, 48, 60



11 Multiply and divide integers and decimals by powers of 10

A number that divides exactly into another number without a remainder. It is useful to write factors in pairs



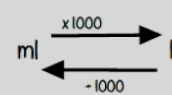
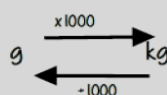
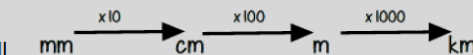
$$3 \times 100 = 300$$



$$0.03 \times 100 = 3$$

12 Convert metric units

When we convert from big unit to small unit we multiply and if we convert from small unit to big unit we divide.



13 Use formal methods to multiply integers

Long multiplication column

$$326 \times 32 = 10,432$$

	Th	H	T	O
326	3	2	6	
× 32				
6	1	5	2	
+	9	7	8	0
1	0	4	3	2
	1	1		

Make the unit 0 then carry on multiplying

14 Use formal methods to multiply decimals

Multiply 0.03 by 1.1 = 0.033

Multiply 0.03 by 1.1 = 0.033

the answer should have the same number of decimal places as are in both the numbers you are multiplying.

Multiply without decimal points: $3 \times 11 = 33$

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15 Use formal methods to divide integers and decimals.

$$3584 \div 7 = 512$$

Short division

	5	1	2
7	3	5	8
			4

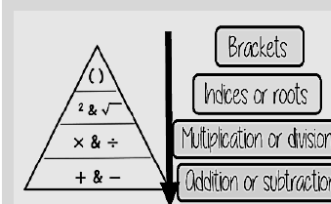
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