

Sharing

12 shared into 3 equal groups

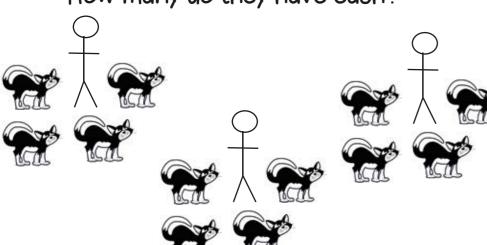
 $12 \div 3 = 4$ 

Grouping

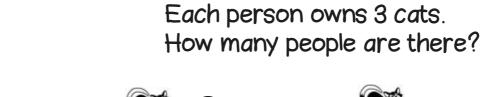
How many groups of 3 are there in 12?

There are 12 cats.

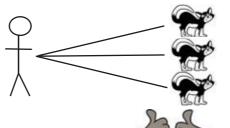
Three people each have the same number of cats. How many do they have each?

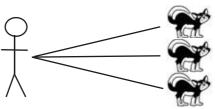


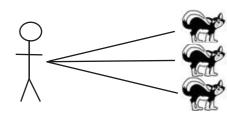
1 for you, 1 for you, 1 for you...



There are 12 cats.





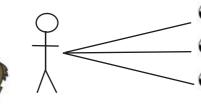


How shall I divide?

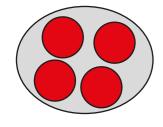
12 can be described as

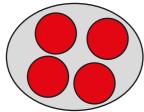
3 columns of 4

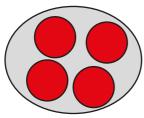
or 4 rows of three



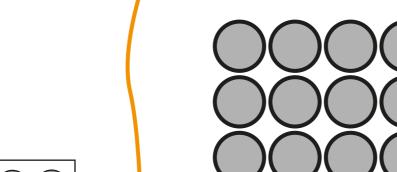
Grab a group of 3 grab a group of 3

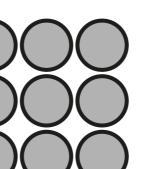


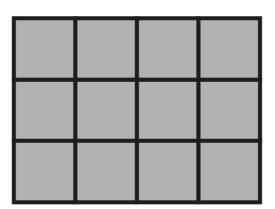


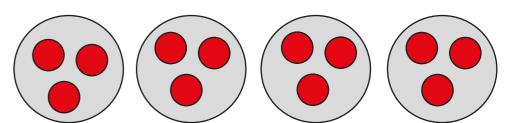


Bar model

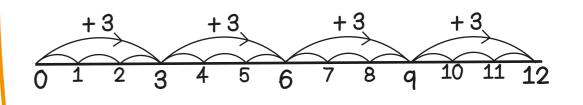




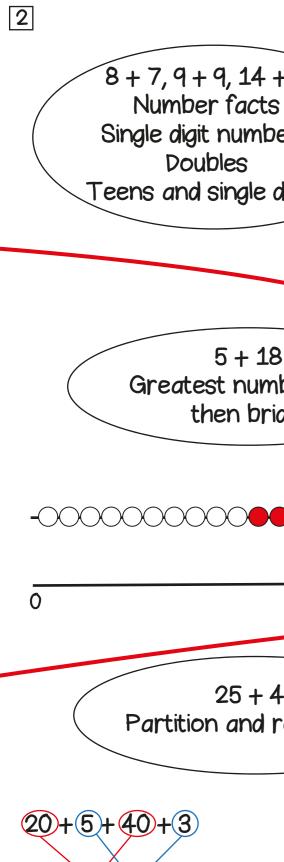








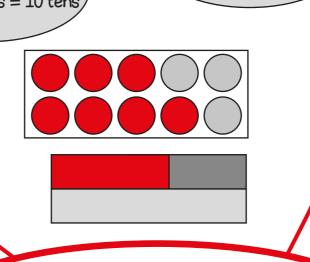




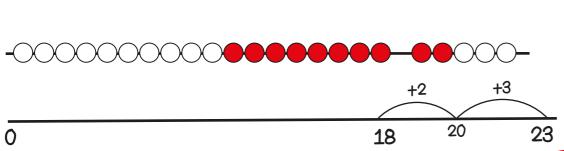
8+7,9+9,14+3 I just knew it! Single digit numbers Teens and single digits

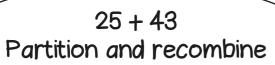
13 + 17Use known facts 30 + 70If I know 3 + 7 = 10then I know If I know 3 + 7 = 1013 + 17 is 2 tens more then I know 3 tens + 7 tens = 10 tens

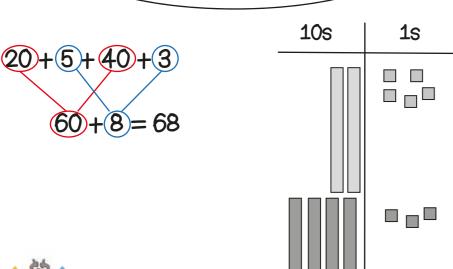
5 + 18Greatest number first then bridge

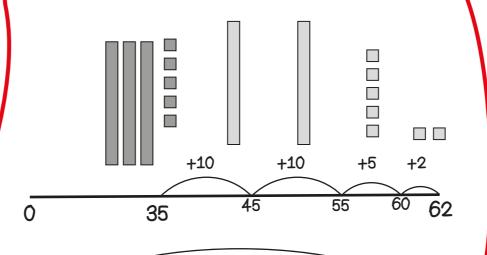


How shall I add?



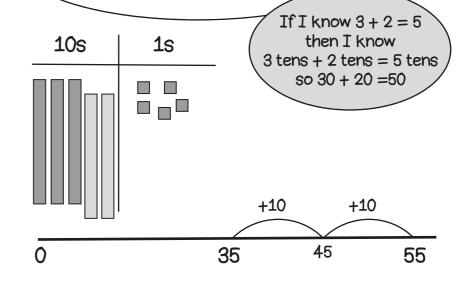


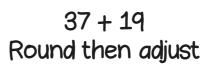


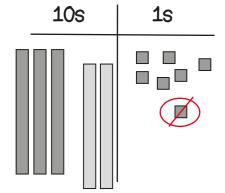


35 + 27Count on in tens then ones

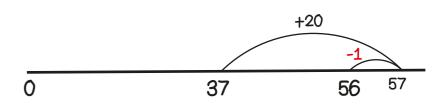
### 35 + 20Add multiples of ten







Add 20 then subtract 1



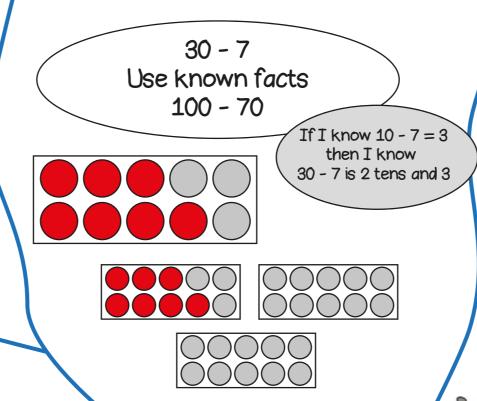




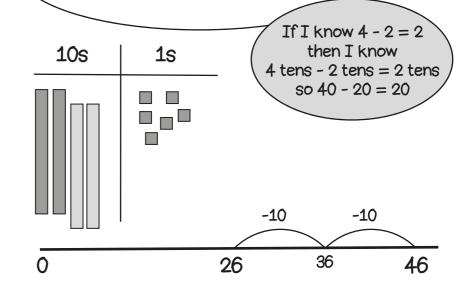
9 - 4, 13 - 5, 18 - 9 ( Number facts Single digit numbers Halves Teens and single digits

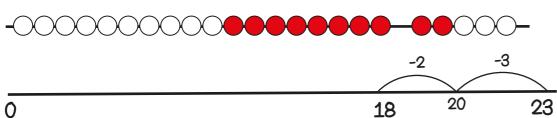
I just knew it!

23 - 5 Count back: bridge through a multiple of ten

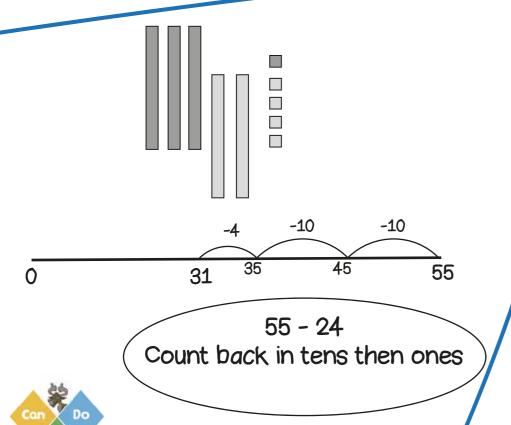


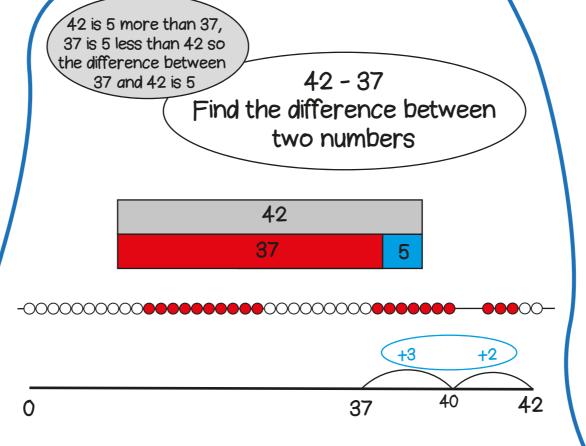
46 - 20 Count back: multiples of ten

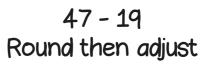


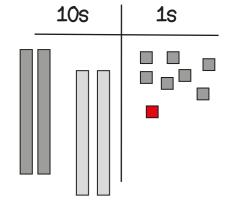


How shall I subtract?

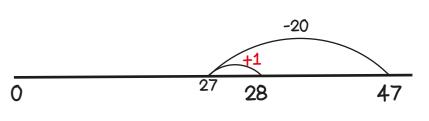






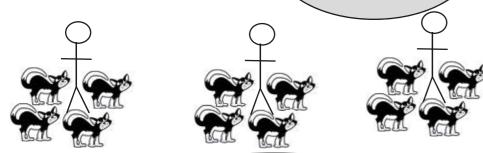


Take away 20 then add 1



Equal groups

There are 3 groups with 4 cats in each group

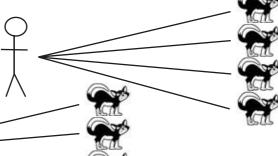


3 people each have 4 cats. How many cats are there in total?

Recall of 2x, 5x and 10x tables

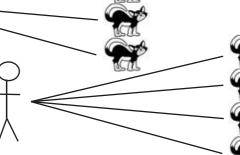
One to many correspondence

If each person has 4 cats, there are 4 times as many cats as people

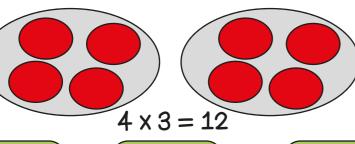


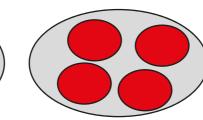






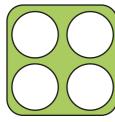
Four cats, multiplied by 3



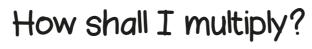


People	Cats
1	4
2 3	8 12
	G



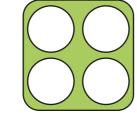


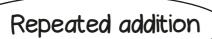


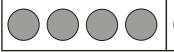














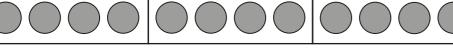






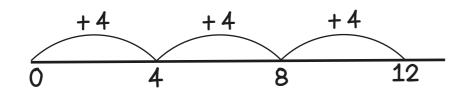






4

4



$$4 + 4 + 4 = 12$$

Count in ones

1, 2, 3, **4**, 5, 6, 7, **8**, 9, 10, 11, **12** 

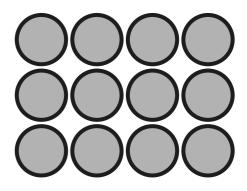
Count in fours

4, 8, 12

Use a known fact

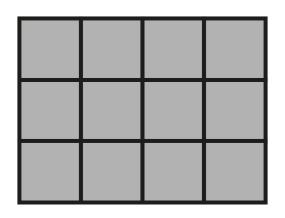
If 2 x 3 is 6, then 4 x 3 is double 6.





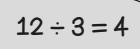
 $4 \times 3 = 12$ 

 $3 \times 4 = 4 \times 3$ 



Sharing

12 shared into 3 equal groups



Grouping

How many groups of 3 are there in 12?

There are 12 cats.

Three people each have the same number of cats.

How many do they have each?



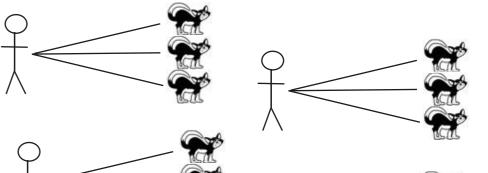
Recall and use 2x, 5x and 10x tables

There are 12 cats. Each person owns 3 cats. How many people are there?

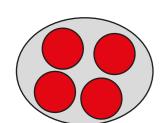


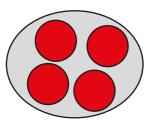
1 for you, 1 for you, 1 for you...

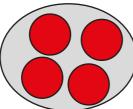
Grab a group of 3 grab a group of 3.



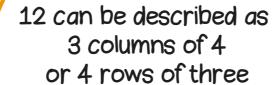


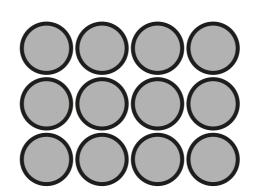


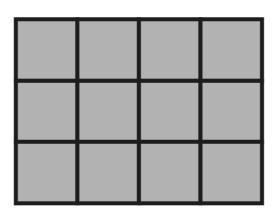




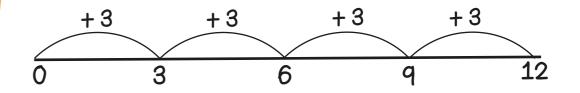
Bar model





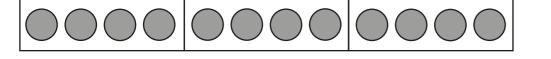






If I know  $3 \times 4 = 12$ then I know  $12 \div 3 = 4$ 

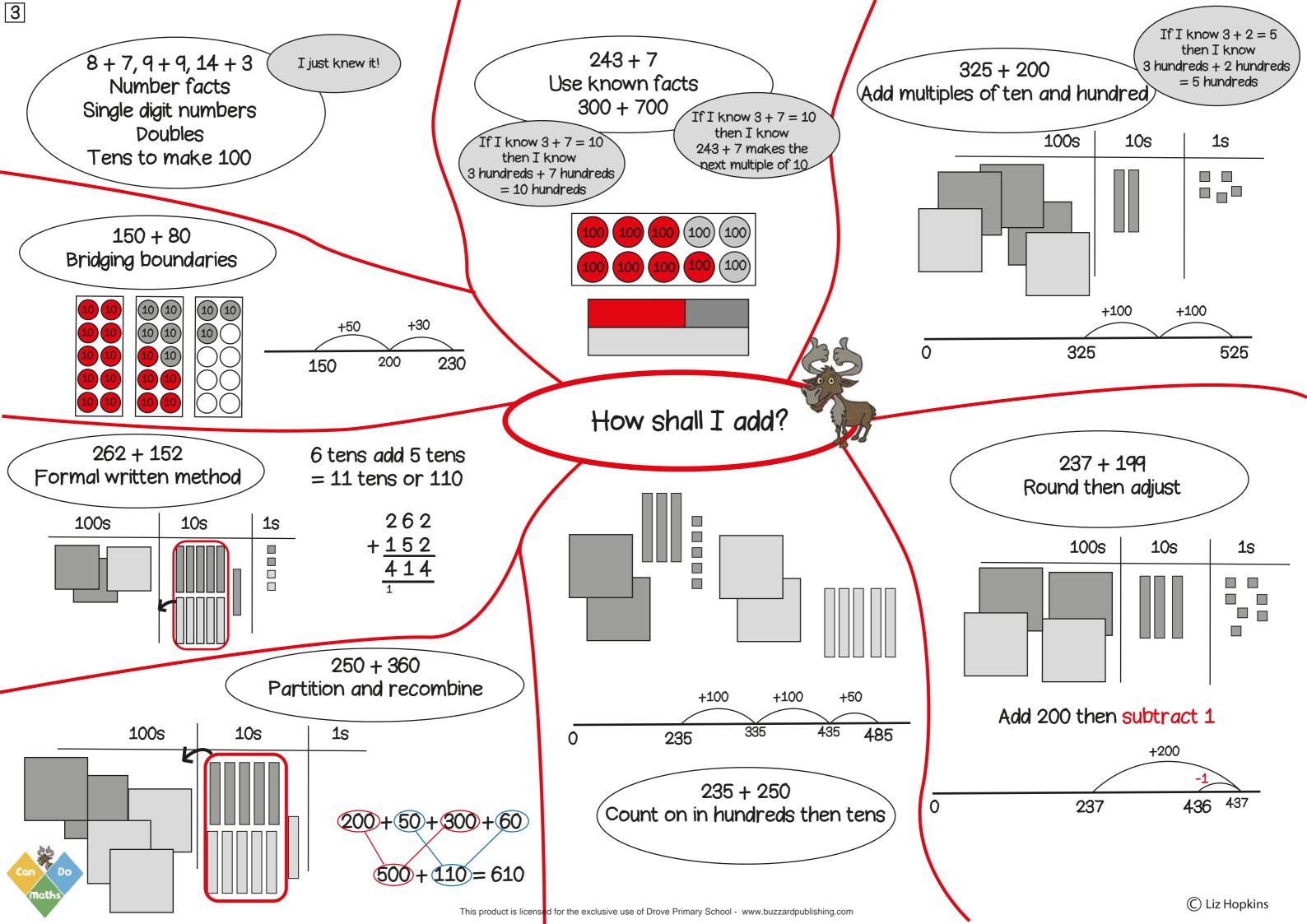




	12	
4	4	4

Link to fractions. One third of 12 is 4







15 - 8, 18 - 5 Number facts Single digit numbers Teens and single digits

230 - 80

Bridging boundaries

by counting back in efficient steps

10 10

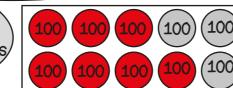
10 10

10 10

I just knew it!

240 - 7 Use known facts 1000 - 700

If I know 10 - 7 = 3then I know 10 hundreds - 7 hundreds = 3 hundreds

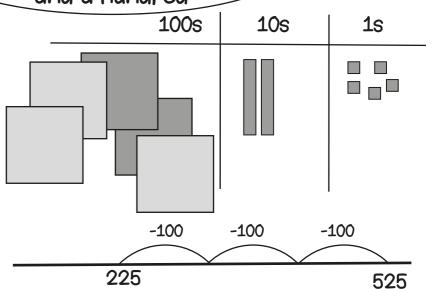


then I know any multiple of 10, take away 7 leaves 3 in the ones.

If I know 10 - 7 = 3

525 - 300 Take away multiples of ten and a hundred

If I know 5 - 3 = 2then I know 5 hundreds - 3 hundreds = 2 hundreds



234 - 152 Formal written method

<sup>1</sup>2 <sup>1</sup>3 4 -<u>152</u> 182

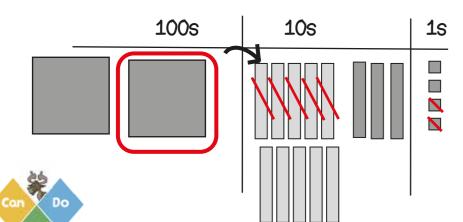
230 - 30 - 50 = 150

150

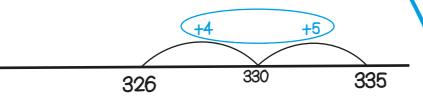
200

230

234 = 100 + 130 + 4



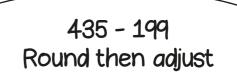
How shall I subtract?

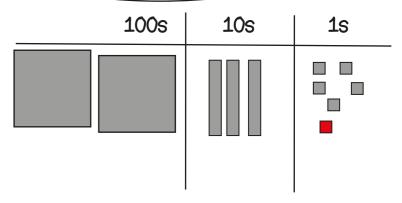


335 - 326 Find the difference between two numbers

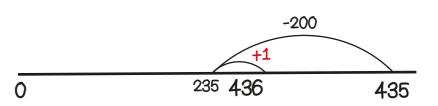
> 335 is 9 more than 326 326 is 9 less than 335 so the difference between them is 9

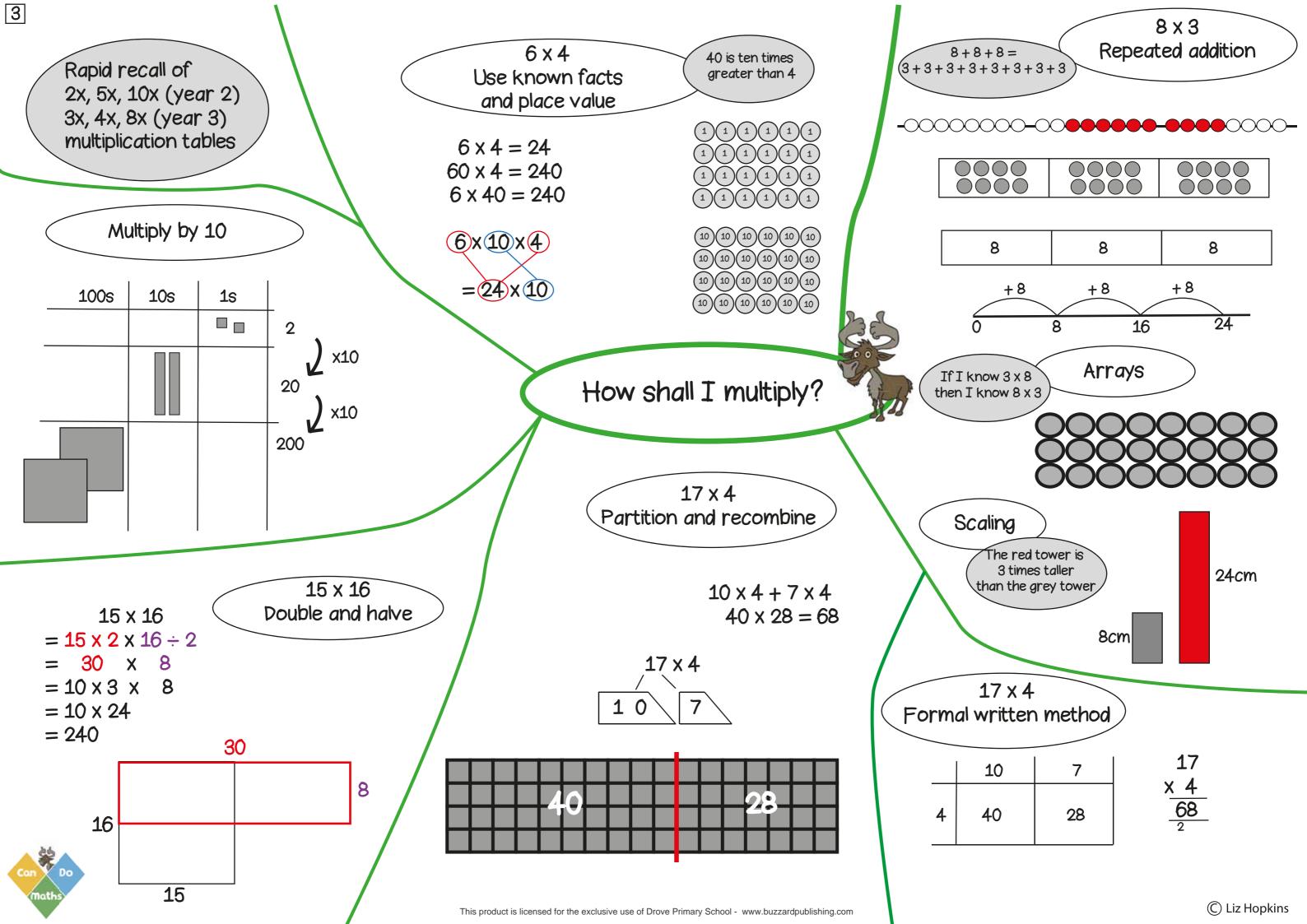
335 326





Take away 200 then add 1







Known facts:
Use 2x, 5x, 10x (year 2)
3x, 4x, 8x (year 3)
multiplication tables to
derive division facts

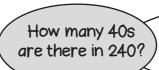
24 ÷ 4 Use known facts and place value

240 is ten times greater than 24

 $24 \div 4 = 6$ 

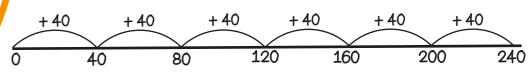
 $240 \div 40 = 6$  $240 \div 4 = 60$  24 biscuits shared between 4 people means they will get 6 biscuits each.

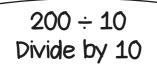
If there are 10 times as many people and 10 times as many biscuits, how many biscuits each now?

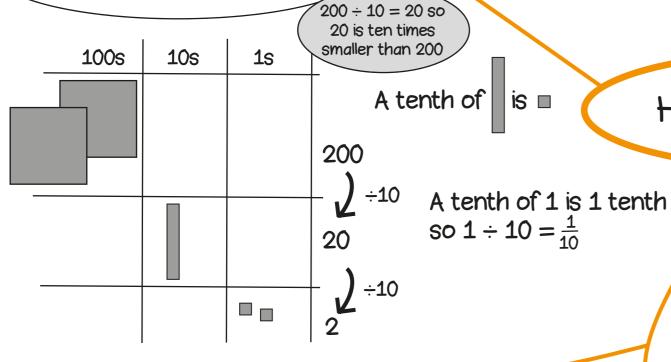


240 ÷ 40 Repeated addition

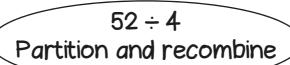
 $240 \div 40 = 6$ How many steps of 40 make 240?

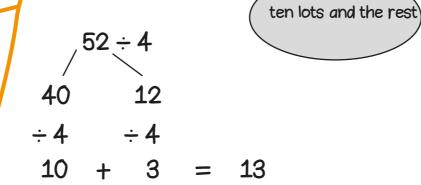




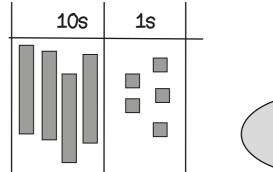


## How shall I divide?

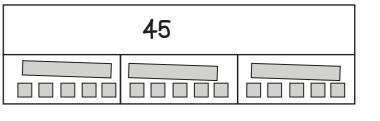




#### 45 ÷ 3 Sharing equally



Ten for you, ten for you, ten for you...

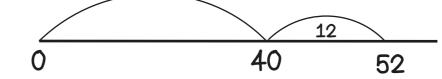


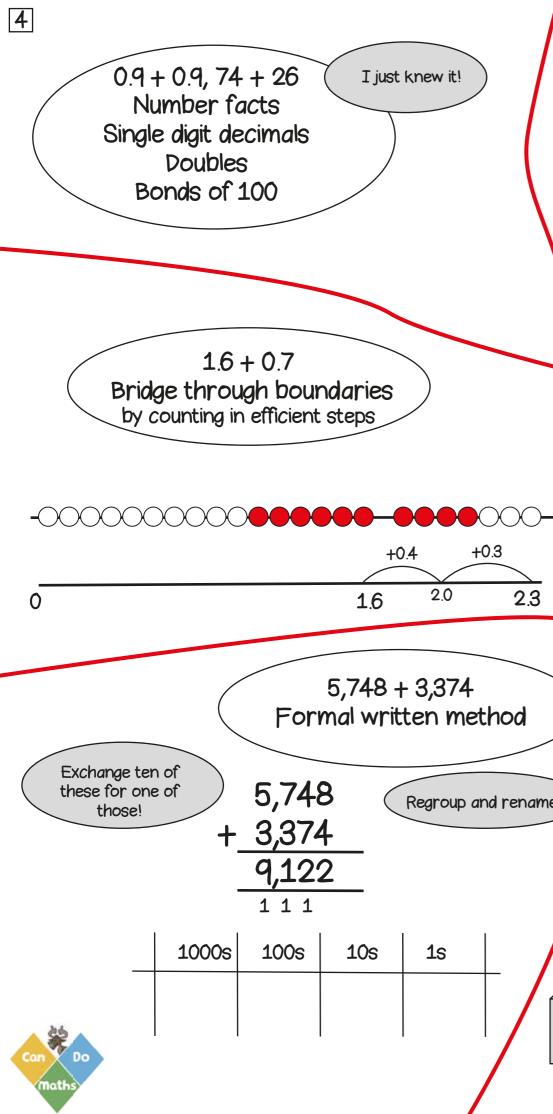
Link to fractions

42 ÷ 6 Double and halve If there are half as many biscuits and half as many people...

$$42 \div 6 = 21 \div 3$$

			42		
7	7	7	7	7	7
	21				
7	7	7			





0.9 + 0.9, 74 + 26I just knew it! Number facts Single digit decimals Doubles Bonds of 100

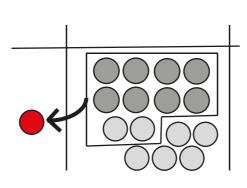
1.6 + 0.7

7 + 8

Use known facts

If I know 7 + 8 = 15then I know 0.7 + 0.8 = 1.5

$$70 + 80 = 150$$
  
 $700 + 800 = 1,500$ 



2,403 + 3,020Use place value to add

If I know 2+3=5then I know 2000 + 3000 = 5000

I have noticed, one number has no hundreds or ones, the other has no tens

1000s 100s 10s 1s	

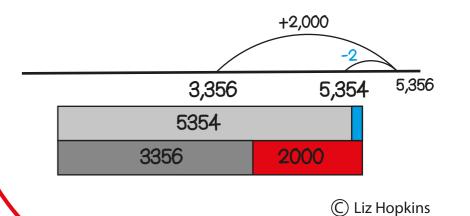
# How shall I add?

5,250 + 2,360Partition and recombine

#### 3,356 + 1,998 Round then adjust

1000s	100s	10s	<b>1</b> s

Add 2,000 then take away 2 100s 10s **1**s



Regroup and rename

+0.3

2.3

2.0

1.6

5,748 + 3,374

Formal written method

9,122 1 1 1

1000s	100s	10s	1s

5,748

+ 3,374

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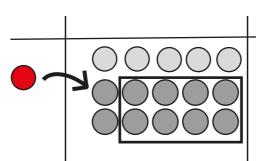
1000s

1.3 - 5, 1.8 - 0.8 Number facts Single digit numbers Halves Wholes and tenths

15 - 8 = 7I just knew it! Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

$$150 - 80 = 70$$
  
 $1500 - 800 = 700$ 



6,342 - 3,020

By using place value counters it is easy to see how to take away

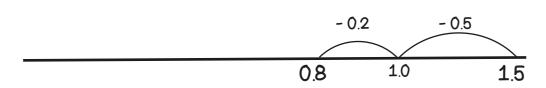
1s

**10s** 

Use place value to subtract

1000s

1.5 - 0.7Bridge through boundaries by counting in efficient steps



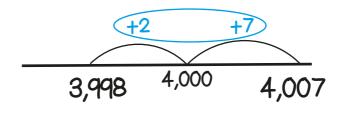
How shall I subtract?

4.56 - 1.99 Round then adjust

100s

1s	$\frac{1}{10}$ S	100 s

Find the difference between two numbers



4007-3998

4,007 3,998

Exchange ten of

these for one of

those!

5,352 2,436

Regroup and rename

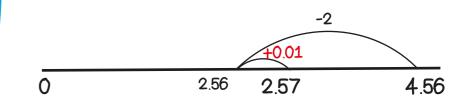
5,352 - 2,136

Formal written method

2,916

1000s	100s	10s	<b>1</b> s	

Take away 2 then add one hundredth







Known facts: Rapid recall of all multiplication tables up to 12 x 12

#### 6 x 4 Use known facts and place value

$$6 \times 4 = 24$$
  
 $60 \times 4 = 240$ 

$$60 \times 40 = 2400$$



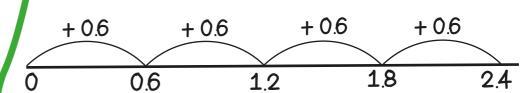
40 is ten times

greater than 4

0.6 is ten times smaller than 6

6 x 4 Use known facts and place value

$$0.6 \times 4 = 2.4$$
  
4 jumps of  $0.6$ 



2.34 x 100 Multiply by 10, 100

$$6 \times 10 \times 4 \times 10$$
= 24 × 100

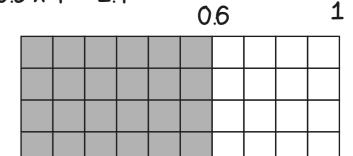
 $0.6 \times 4 = 24 \text{ tenths}$  $0.6 \times 4 = 2.4$ 

4

36

30

210

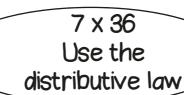


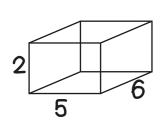


100 S 1 10 S 100s 1000s 10s 1s  $\bigcirc\bigcirc$ 

2.34 x10 23.4 x100 x10 234

How shall I multiply?





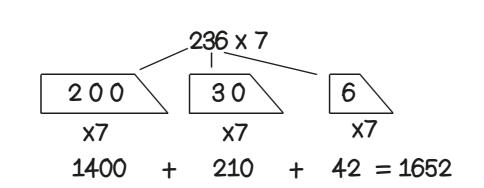
 $2 \times (5 \times 6) = (2 \times 5) \times 6$  $2 \times 30 = 10 \times 6$ 

45 x 6  $=5\times9\times6$  $=5\times6\times9$  $= 30 \times 9$ = 270

45 x 6 Use factors and commutativity

> Write as factors then re-order

7 x 36) 7  $= 7 \times 30 + 7 \times 6$ = 210 + 42= 252



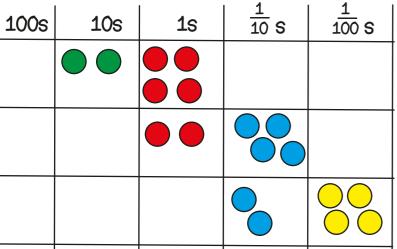
36 x 7 Formal written method

	30	6	
7	210	42	
$\neg$			

36

Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

> 24 ÷ 100 Divide by 10, 100



24 ÷ 4 Use known facts and place value

$$24 \div 4 = 6$$
  
 $240 \div 40 = 6$   
 $2400 \div 400 = 6$ 

$$2400 \div 400 = \frac{24 \times 100}{4 \times 100}$$
$$\frac{24}{4} = 6$$

240 is ten times greater than 24

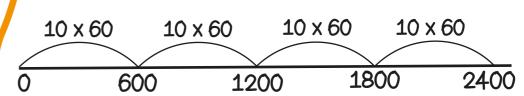
> 24 biscuits shared between 4 people means they will get 6 biscuits each.

If there are 100 times as many people and 100 times as many biscuits, how many biscuits each now?

60 is ten times areater than 6

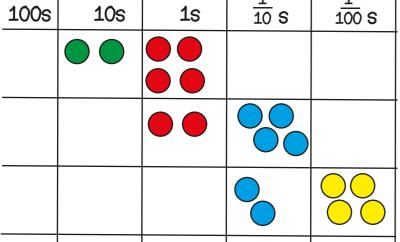
2400 ÷ 60 Use known facts and place value

 $2400 \div 60 = 40$ How many steps of 60 make 2400?



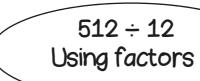
732 ÷ 6

Formal written method

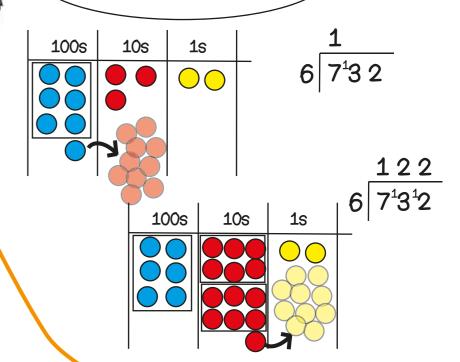


24 2.4 ÷100 0.24

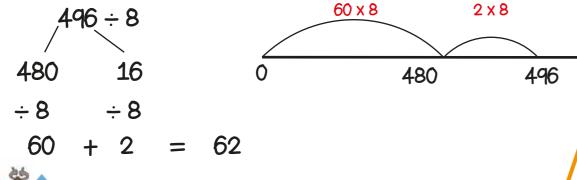
How shall I divide?

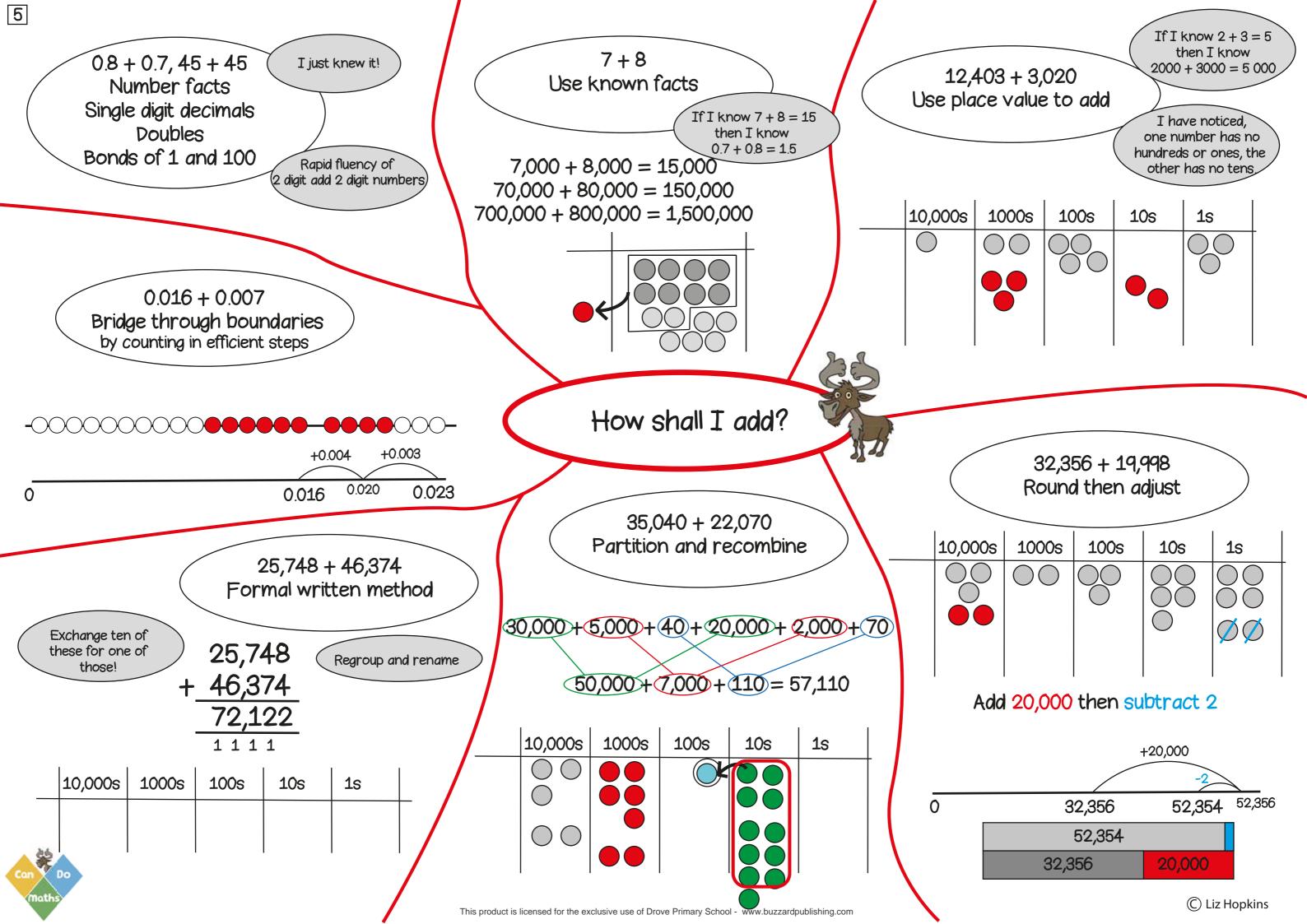


512										
172					17	'2		17	'2	
43	43	43	43							



#### 496 ÷ 8 Partition and recombine





9 - 4, 13 - 5, 18 - 9

Number facts

Single digit decimals

Halves

Subtract from 1 and 100

I just knew it!

Rapid fluency of

2 digit subtract

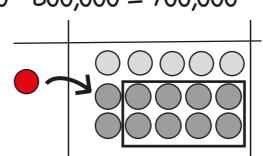
2 digit numbers

15 - 8 = 7 Use known facts

> If I know 15 - 8 = 7 then I know 1.5 - 0.8 = 0.7

15,000 - 8,000 = 7,000

150,000 - 80,000 = 70,000 1,500,000 - 800,000 = 700,000



40,012 - 3,005 Use place value to subtract

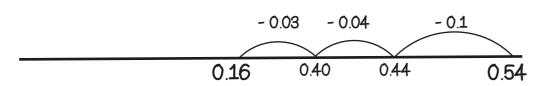
5 less than 12 is 7 Now it is easy to take away 3000

If I know 40 - 3 = 37 then I know that 40 thousand take away 3 thousand is 37 thousand

40,000 = 4 tens of thousands or 40 thousands 12 = 1 ten and 2 ones or 12 ones

40,012 = 40 thousands and 12 ones take away 3 thousands and 5 ones equals 37 thousands and 7 ones.

0.54 - 0.17
Bridge through boundaries
by counting in efficient steps



How shall I subtract?

45,748 - 26,374 Formal written method

Exchange ten of these for one of those!

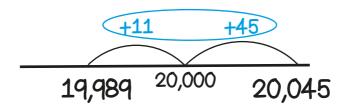
345,748 26.374

Regroup and rename

- <u>26,374</u> <u>19,374</u>

10,000s	1000s	100s	10s	<b>1</b> s	

20,045 - 19,989 Find the difference between two numbers

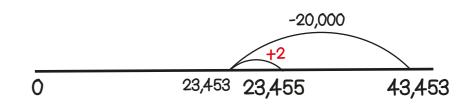


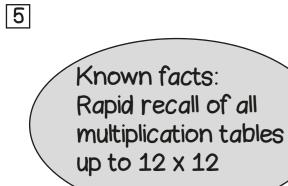
20,045	
19,989	56

43,453 - 19,998 Round then *adjust* 

10,000s	1000s	100s	10s	<b>1</b> s	

Take away 20,000 then add 2





100s

 $\bigcirc\bigcirc$ 

1000s

6 x 4 Use known facts and place value

40 is ten times greater than 4

1 1 1 1 1 1

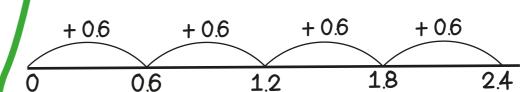


0.6 is ten times

smaller than 6

6 x 4 Use known facts and place value

$$0.6 \times 4 = 2.4$$
  
4 jumps of  $0.6$ 



2.34 x 1000 Multiply by 10, 100, 1000



 $6 \times 4 = 24$ 

 $60 \times 4 = 240$ 

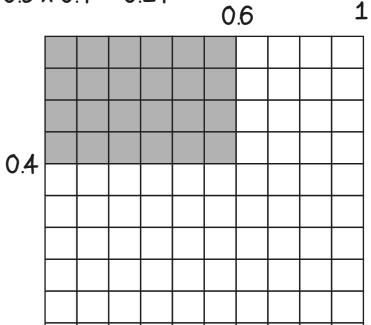
 $60 \times 40 = 2400$ 

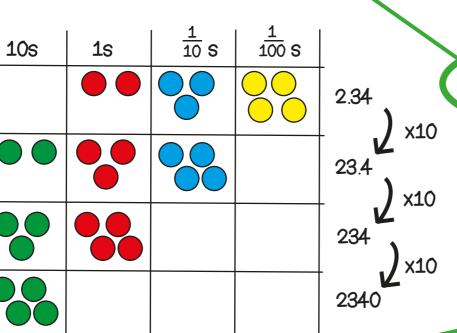
 $=24 \times 100$ 

10 10 10 10 10 10 10 10 10 10 10 10 10 10 10

10 10 10 10 10

 $0.6 \times 0.4 = 24$  hundredths  $0.6 \times 0.4 = 0.24$ 



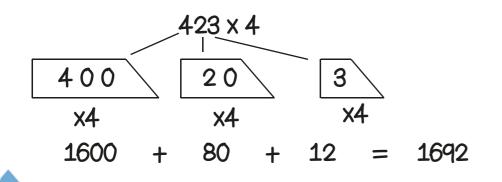


How shall I multiply?

15 x 42 Using factors and distributive law

15 x 48  $= 15 \times 6 \times 8$  $= 90 \times 8$ = 720

423 x 4 Partition and recombine



15 x 14)  $= 15 \times 6 + 15 \times 8$ = 90 + 120= 210

427 x 38 Formal written method

	400	20	7
30	12,000	600	210
8	3,200	160	56

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Include calcuations where remainders occur

24 ÷ 4 Use known facts and place value

24,000 is a thousand times greater than 24

24 biscuits shared between

4 people means they will get

biscuits, how many biscuits

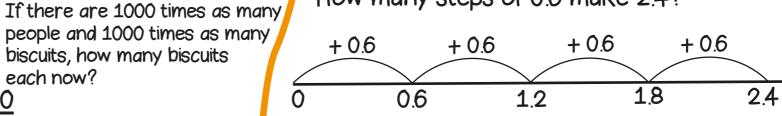
6 biscuits each.

0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



5724 ÷ 4

Formal written method

up to 12 x 12 to derive division facts

multiplication tables

Known facts:

Use recall of all

24 ÷ 1000 Divide by 10, 100, 1000

 $2400 \div 400 = 6$  $24,000 \div 4000 = 6$ 

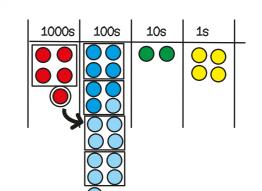
each now?  $24,000 \div 400 = 24 \times 1000$ 4 x 100 <u>240</u> = 60

 $24 \div 4 = 6$ 

 $240 \div 40 = 6$ 

100s	10s	<b>1</b> s	10 s	100 S	1 1000 s	
						24
						2.4 ÷10
						0.24 )÷10
				00	00	0.024

How shall I divide?



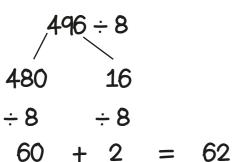
1512 ÷ 24 Using factors

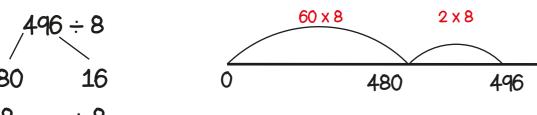
 $1512 \div 6 \div 4$ 

1000s	100s	10s	1s	
			<u>SS</u>	1431
				4 5 <sup>1</sup> 7 <sup>1</sup> 2 4
		88		

	1512																					
252				252					252			252				252			252			
63	63	63	63																			

#### 496 ÷ 8 Partition and recombine









44 + 56, 27 + 27 Number facts Single digit decimals Doubles Bonds of 1 and 100

I just knew it!

Rapid fluency of

(2 digit add 2 digit numbers)

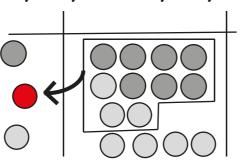
17 + 17 Use known facts

If I know 17 + 17 = 34 then I know

17,000 + 17,000 = 34,000

170,000 + 170,000 = 340,000

1,700,000 + 1,700,000 = 3,400,000



1,102,403 + 50,020 Use place value to add

I have noticed, one number has no hundreds or ones, the other has no tens

1,000,000s	100,000s	10,000s	1000s	100s	10s	<b>1</b> s
					••	

# 0.028 + 0.015 Bridge through boundaries by counting in efficient steps

# 

+0.01 +0.002 +0.003 0.028 0.038 0.040 0.043

> 325,748 + 246,374 Formal written method

> > Regroup and rename

Exchange ten of these for one of those!

0

325,748 + 246,374 572,122

100,000s	10,000s	1000s	100s	10s	<b>1</b> s	

# How shall I add?

307,040 + 206,070 Partition and recombine

300,000 + 7,000 + 40 + 200,000 + 6,000 + 70

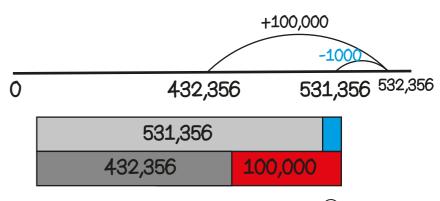
500,000 + 13,000 + 110 = 513,110

100,000s	10,000s	1000s	100s	10s	<b>1</b> s	
ı						

432,356 + 99,000 Round then adjust

100,000s	10,000s	1000s	100s	10s	<b>1</b> s
	00	<b>Ø</b>		000	000

Add 100,000 then take away 1,000



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0.9 - 0.4, 100 - 65 Number facts Single digit decimals Halves

Bonds of 1 and 100

Rapid fluency of 2 digit subtract 2 digit numbers

I just knew it!

0.054 - 0.017 Bridge through boundaries by counting in efficient steps

- 0.004 - 0.01 - 0.03 0.040 0.044 0.054 0.037

> 445,748 - 126,374 Formal written method

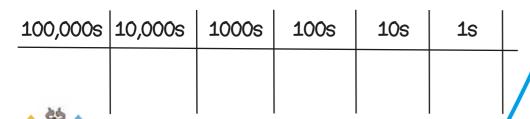
> > Regroup and rename

Exchange ten of these for one of those!

445,748

+ 126,374

319,374



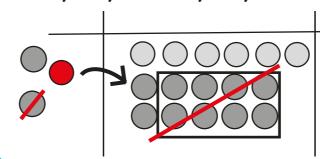
36 - 18 = 18Use known facts

> If I know 36 - 18 = 18then I know 3.6 - 1.8 = 1.8

36,000 - 18,000 = 18,000

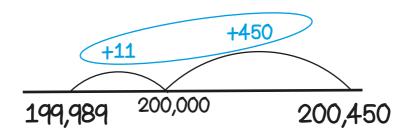
360,000 - 180,000 = 180,000

3,600,000 - 1,800,000 = 1,800,000



How shall I subtract?

200,450 - 199,989 Find the difference between two numbers



200,450 461 199,989

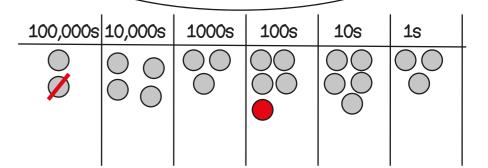
400,032 - 30,005 Use place value to subtract 5 less than 32 is 27

400,000 = 4 hundreds of thousands or 400 thousands

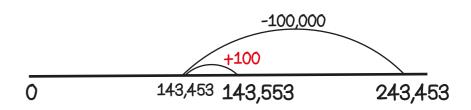
400 - 30 = 370 so 400,000 - 3,000 = 370,000

400,032 = 400 thousands and 32 ones take away 30 thousands and 5 ones = 370,027

> 243,453 - 99,900 Round then adjust



Take away 100,000 then add 100





up to 12 x 12

100s

 $\bigcirc\bigcirc$ 

1000s

6 x 4 Use known facts and place value

**x10** 

40 is ten times greater than 4

$$60 \times 40 = 2400$$

$$600 \times 400 = 240,000$$

6x10x4x10

2.34 x 1000 Multiply by 10, 100, 1000

10s

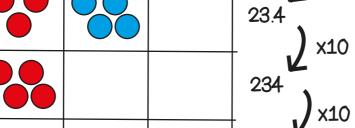


# 2.34

4203 x 4

Partition and recombine

1s



100 S

1 10 S

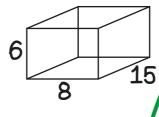
How shall I multiply?

Using factors and distributive law 15 x 48

$$= 15 \times 6 \times 8$$

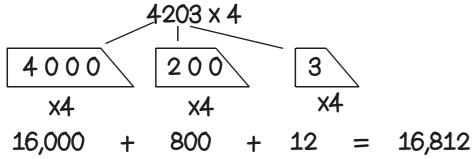
$$= 90 \times 8$$
  
= 720

15 x 42

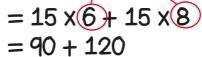




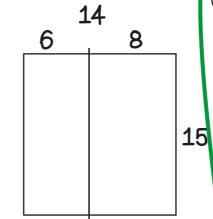
2340



15 x 14)



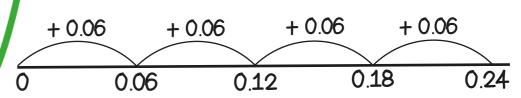
= 210



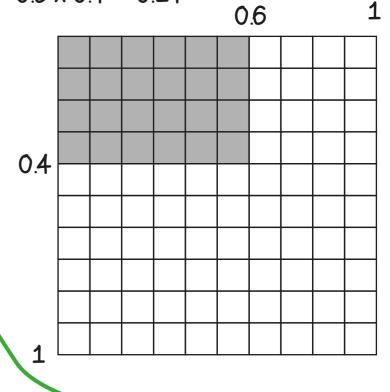
0.6 is ten times smaller than 6

6 x 4 Use known facts and place value

$$0.06 \times 4 = 2.4$$
  
4 jumps of  $0.06$ 



 $0.6 \times 0.4 = 24$  hundredths  $0.6 \times 0.4 = 0.24$ 



2427 x 38 Formal written method

6 Known facts: Use recall of all multiplication tables up to 12 x 12 to

derive division facts

24 ÷ 1000

Divide by 10, 100, 1000

Include calcuations where remainders occur

#### $24 \div 4$ Use known facts

240 is ten times greater than 24

and place value

If there are 10 times as many people and 10 times as many biscuits, how many biscuits

$$2,400,000 \div 400,000 = 6$$
 each now?

 $240 \div 40 = 6$ 

 $2400 \div 400 = 6$ 

 $24,000 \div 4000 = 6$ 

 $240,000 \div 40,000 = 6$ 

÷10

÷10

$$240,000 \div 400 = \underbrace{24 \times 10,000}_{4 \times 100}$$

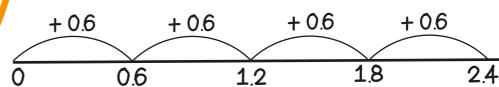
$$\frac{2400}{4} = 600$$

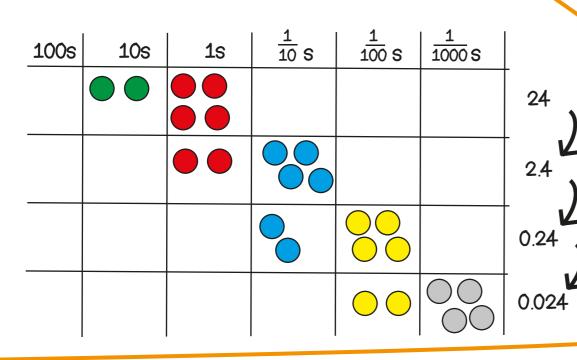
0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



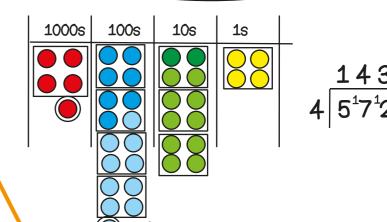


How shall I divide?

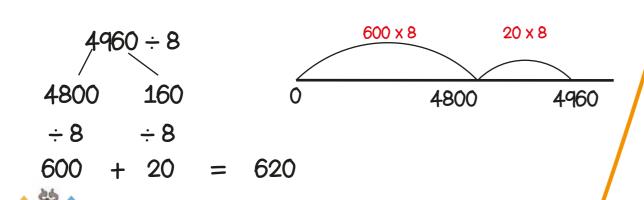
1512 ÷ 24

Using factors

7182 ÷ 21 Formal written method



#### 496 ÷ 8 Partition and recombine



 $1512 \div 6 \div 4$ 

	1512																						
	252 252 252												25	52	252				252				
[	63	63	63	63																			