# **Addition**

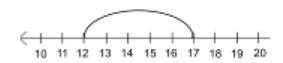
Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-whole model	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7  10= 6 + 4  Use the part-part whole diagram as shown above to move into the abstract.

Starting at the bigger number and counting on



Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.

12 + 5 = 17



Start at the larger number on the number line and count on in ones or in one jump to find the answer.

5 + 12 = 17

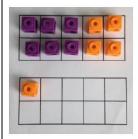
your head and count on the smaller number to find your answer.

Place the larger number in

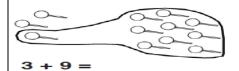
Regrouping to make 10.



6 + 5 = 11

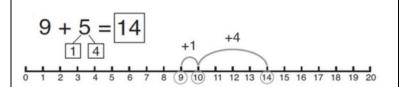


Start with the bigger number and use the smaller number to make 10.



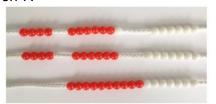
Use pictures or a number line. Regroup or partition the smaller number to make 10. 7 + 4= 11

If I am at seven, how many more do I need to make 10. How many more do I add on now?

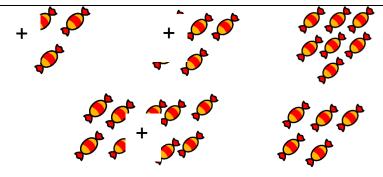


# Adding three single digits

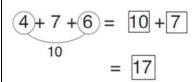
4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7.



Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.

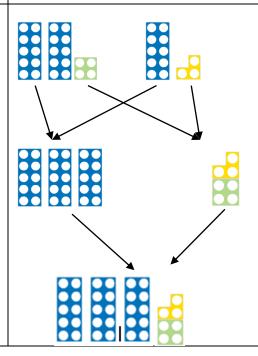


Add together three groups of objects. Draw a picture to recombine the groups to make 10.

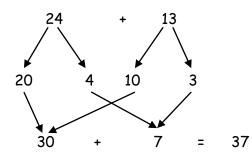


Combine the two numbers that make 10 and then add on the remainder.

# Partitioning and recombining



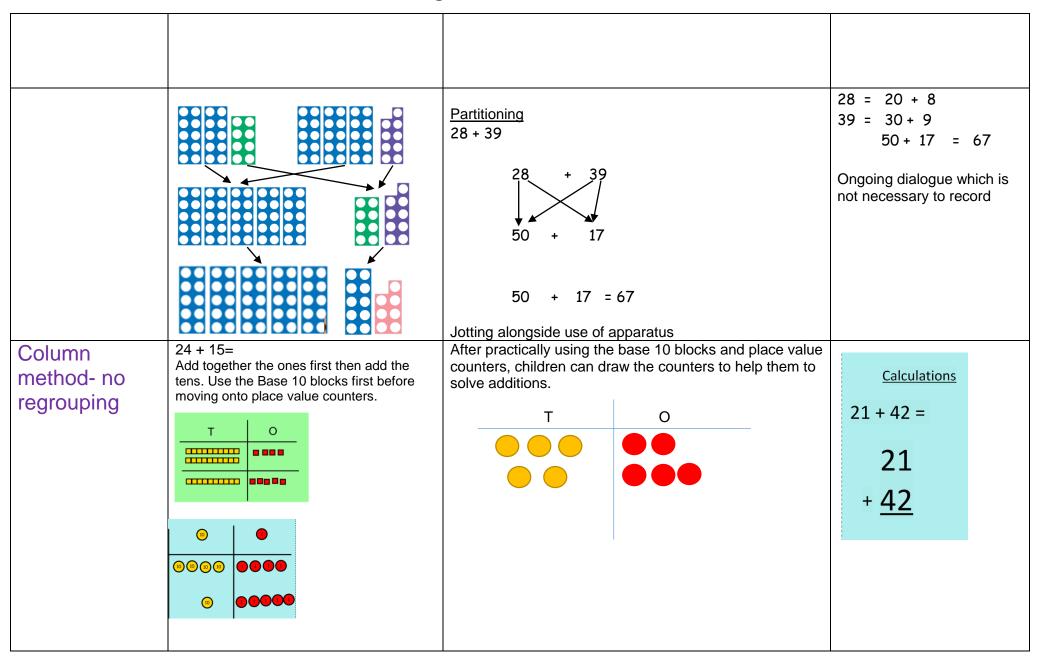
24 + 13



Jotting alongside use of apparatus

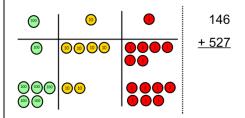
$$24 = 20 + 4$$
 $13 = 10 + 3$ 
 $30 + 7 = 37$ 

Ongoing dialogue which is not necessary to record

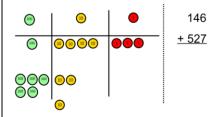


# Column methodregrouping

Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10.

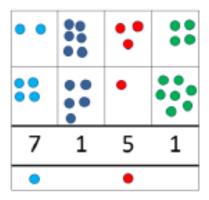


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

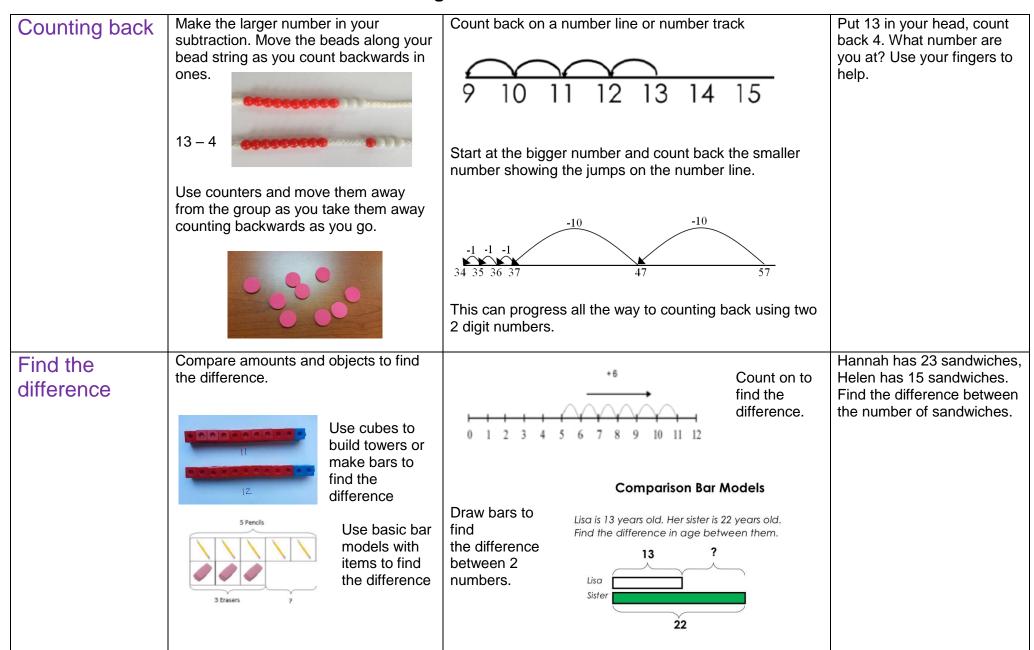
$$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & 8 \\ 60 & + & 13 \end{array} = 73$$

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.  $\frac{+85}{621}$ 

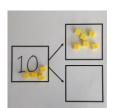
536

# **Subtraction**

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-2=4$	Cross out drawn objects to show what has been taken away.	18 -3= 15 8 - 2 = 6
	Subtraction as 'chopping off'		

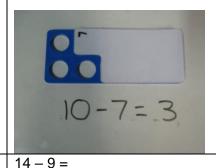


# Part Part Whole Model

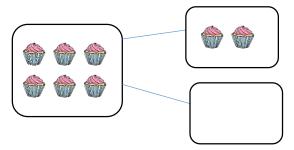


Link to addition- use the part whole model to help explain the inverse between addition and subtraction.

If 10 is the whole and 6 is one of the parts. What is the other part?



Use a pictorial representation of objects to show the part part whole model.



10

Move to using numbers within the part whole model.

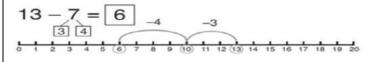
#### Make 10







Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.



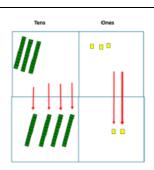
Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.

16 – 8=

How many do we take off to reach the next 10?

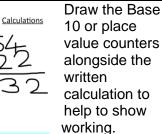
How many do we have left to take off?

Column method without regrouping



Use Base 10 to make the bigger number then take the smaller number away.

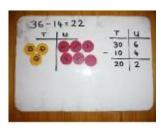
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47 - 24 = 23  $-\frac{40 + 7}{20 + 3}$ 

Show how you partition numbers to subtract. Again make the larger

number first.



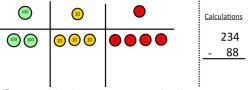
Calculations
176 - 64 =
176
- 64
- 112

This will lead to a clear written column subtraction.

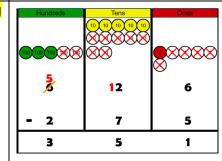
32 - 12 20

Column method with regrouping Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters



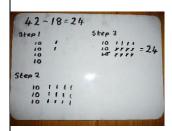
Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



Children can start their formal written method by partitioning the number into clear place value columns.

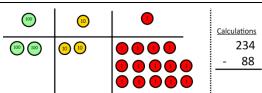


When confident, children can find their own way to record the exchange/regrouping.

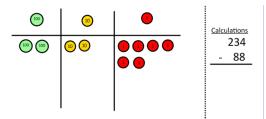
Just writing the numbers as shown here shows that the child understands the method and

knows when to exchange/regroup.

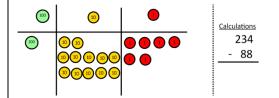




Now I can subtract my ones.

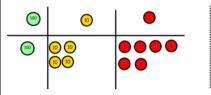


Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

Calculations 1**23**4



Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

Moving forward the children use a more compact method.

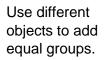
This will lead to an understanding of subtracting any number including decimals.

# **Multiplication**

Objective and	Concrete	Pictorial	Abstract
Strategies Doubling	Use practical activities to show how to double a number.  double 4 is 8 $4 \times 2 = 8$	Draw pictures to show how to double a number.  Double 4 is 8	16 10 6 1x2 20 12 Partition a number and then double each part before recombining it back together.
Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud.  Write sequences with multiples of numbers.  2, 4, 6, 8, 10  5, 10, 15, 20, 25, 30

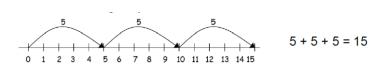




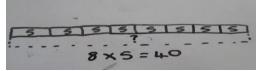


There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?

2 add 2 add 2 equals 6



Children can record this as a bar model:



The dotted line shows the unknown quantity. Children could then replace the question mark with the number 40.

Write addition sentences to describe objects and pictures.

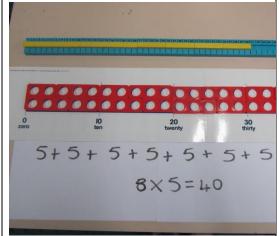


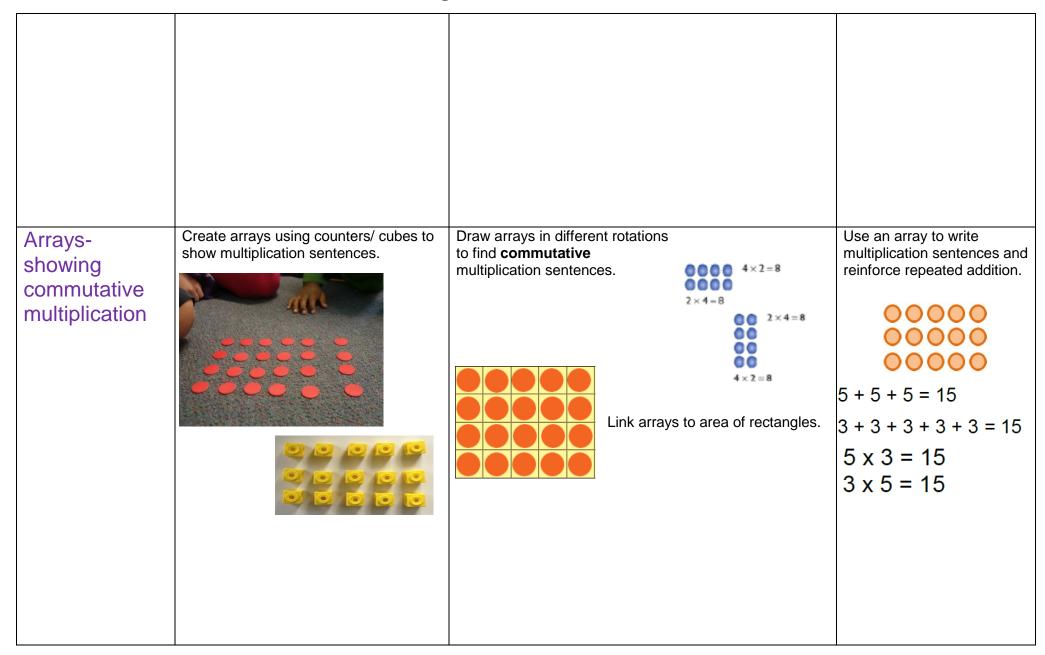
Children can then record this onto an empty number line:

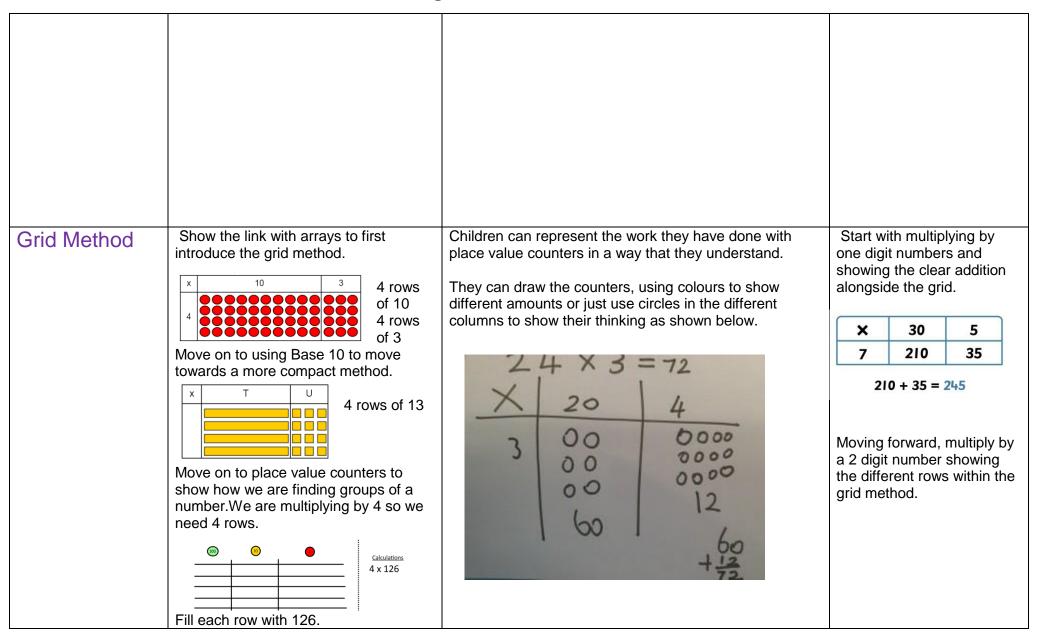
5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40

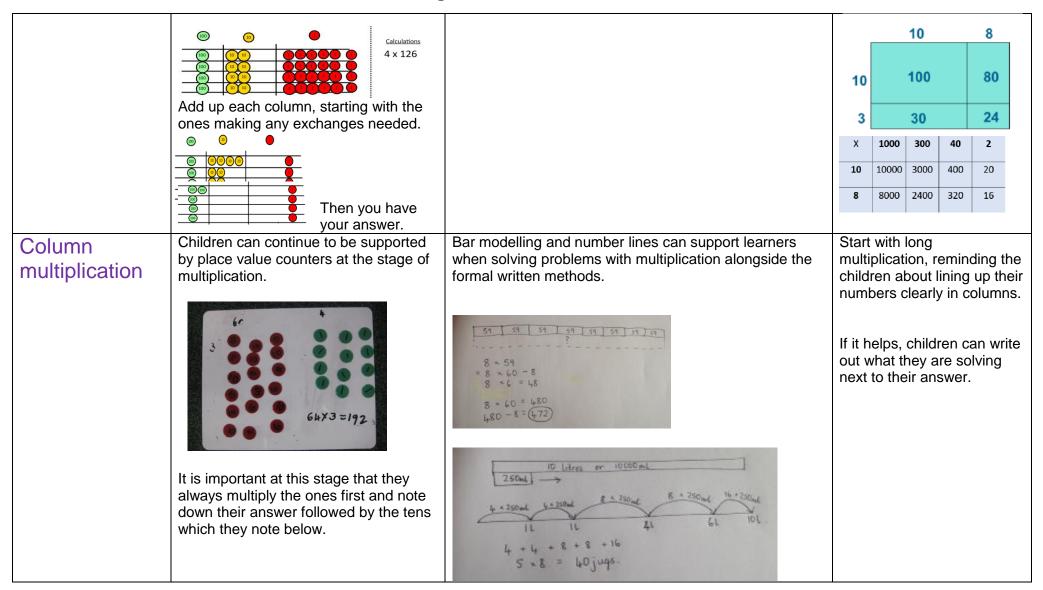
0 5 10 15 20 25 30 35 40

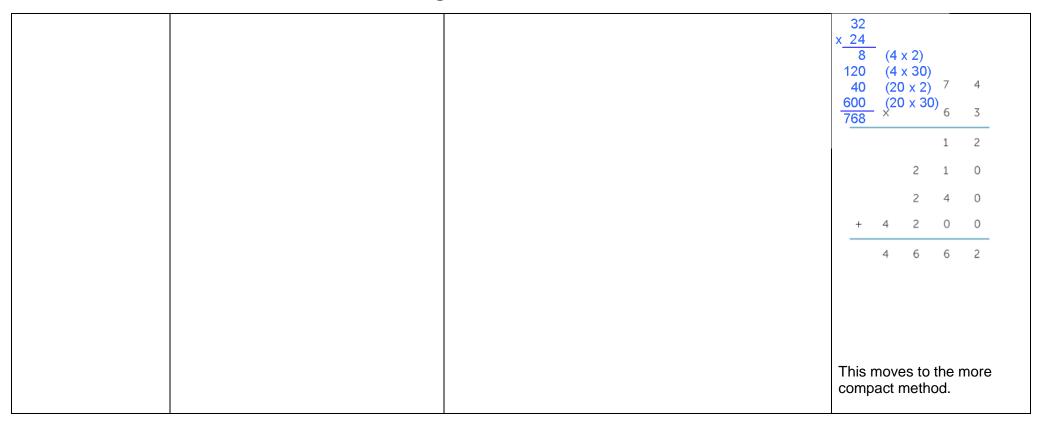
 $8 \times 5 = 40$ 











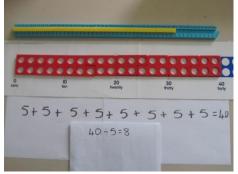
	2 3 1
	1342
	x 18
	13420
	10736
	24156

# **Division**

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups.  0 1 2 3 4 5 6 7 8 9 10 11 12	28 ÷ 7 = 4  Divide 28 into 7 groups.  How many are in each group?
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
		20 ? 20 ÷ 5 = ? 5 x ? = 20	

Te

Ten divided into two equal groups

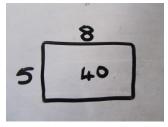


How many 5's in 40?

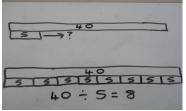
Children can use Cuisenaire or Numicon to work this out using grouping.



Children can then take the Cuisenaire from the rod track and rearrange it into an array.



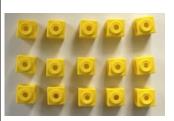
Children should be taught to represent this as a bar model:



This can then be recorded on an empty number line:

$$40 \div 5 = 8$$

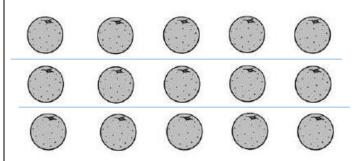
# Division within arrays



Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

Eg 
$$15 \div 3 = 5$$
  $5 \times 3 = 15$   
 $15 \div 5 = 3$   $3 \times 5 = 15$ 



Draw an array and use lines to split the array into groups to make multiplication and division sentences.

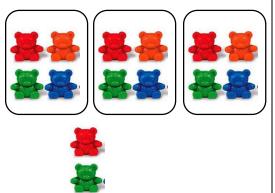
Find the inverse of multiplication and division sentences by creating four linking number sentences.

$$7 \times 4 = 28$$
  
 $4 \times 7 = 28$   
 $28 \div 7 = 4$   
 $28 \div 4 = 7$ 

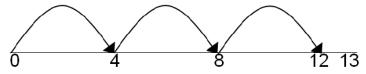
# Division with a remainder

14 ÷ 3 =

Divide objects between groups and see how much is left over



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.





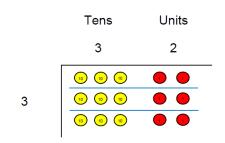




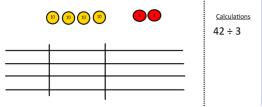
Complete written divisions and show the remainder using r.

$$29 \div 8 = 3$$
 REMAINDER 5  $\uparrow$  vidend divisor quotient remainder

#### Short division

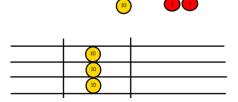


Use place value counters to divide using the bus stop method alongside



 $42 \div 3 =$ 

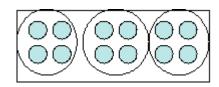
Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



We exchange this ten for ten ones and then share the ones equally among the groups.

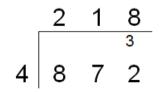


Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.



Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.

Long division	24 × 16 becomes	124 × 26 becomes	124 × 26 becomes
	2	1 2	1 2
	2 4	1 2 4	1 2 4
	× 1 6	× 2 6	× 2 6
	2 4 0	2 4 8 0	7 4 4
	1 4 4	7 4 4	2 4 8 0
	3 8 4	3 2 2 4	3 2 2 4
		1 1	1 1
	Answer: 384	Answer: 3224	Answer: 3224
	432 ÷ 15 becomes	432 ÷ 15 becomes	432 ÷ 15 becomes
	2 8 r 12	2 8	2 8 · 8
	1 5 4 3 2	1 5 4 3 2	1 5 4 3 2 0
	3 0 0	3 0 0 15×20	3 0 ↓
	1 3 2	1 3 2	1 3 2
	1 2 0	1 2 0 <sup>15×8</sup>	1 2 0
	1 2	1 2	1 2 0
			1 2 0
		$\frac{12}{15} = \frac{4}{5}$	0
	Answer: 28 remainder 12	Answer: 28 <del>4</del> 5	Answer: 28⋅8