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| **Progression of Skills in: Number -Number and Place value** |

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|  | **Counting** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception (2020)** | **Year 1** | | **Year 2** | | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **Counting** | Assign a number name to each idem being counted ensuring that each item in a group has been counted | count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number | |  | |  | count backwards through zero to include negative numbers | interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero | use negative numbers in context, and calculate intervals across zero |
| Recognise that the when counting number must be said in a certain order | count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens | | count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward | | count from 0 in multiples of 4, 8, 50 and 100; | count in multiples of 6, 7, 9, 25 and 1 000 | count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 |  |
| Understand that the number name assigned to the final object in a group is the total number of objects within that group | given a number, identify one more and one less | |  | | find 10 or 100 more or less than a given number | find 1 000 more or less than a given number |  |  |
|  | Recognize that anything can be counted including things which can not be touched e.g. sounds |  | |  | |  |  |  |  |
|  | Understanding that the order in which a group of items is touched is irrelevant the total amount will always be the same |  | |  | |  |  |  |  |
|  | To subatize small amounts recognizing the total without counting |  | |  | |  |  |  |  |
|  | Verbally count beyond 20, recognizing the pattern of the counting system |  | |  | |  |  |  |  |
|  | **Comparing Numbers** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | **Milestone 2** | | | **Milestone 3** | |
| **Comparing numbers** | **Reception** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| use the language of: more that, fewer than equal than when comparing groups of objects | use the language of: equal to, more than, less than (fewer), most, least | compare and order numbers from 0 up to 100; use <, > and = signs | | compare and order numbers up to 1 000 | | order and compare numbers beyond 1 000 | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit  (appears also in Reading and Writing Numbers) | read, write, order and compare numbers up to  10 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers) |
| Identify groups with more or less than others |  |  | |  | | *compare numbers with the same number of decimal places up to two decimal places*  (copied from Fractions) |  |  |
|  | Compare groups with not identical items identifying groups with more than, less than and groups equal to |  |  | |  | |  |  |  |
|  | **IDENTIFYING, REPRESENTING AND ESTIMATING NUMBERS** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | **Milestone 2** | | | **Milestone 3** | |
| **Identifying, representing and estimating numbers** | **Reception** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| Estimate groups which are unequal identifying groups with have the most or least | identify and represent numbers using objects and pictorial representations including the number line | identify, represent and estimate numbers using different representations, including the number line | | identify, represent and estimate numbers using different representations | | identify, represent and estimate numbers using different representations |  |  |
|  | **READING AND WRITING NUMBERS** (including Roman Numerals) | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | **Milestone 2** | | | **Milestone 3** | |
| **Reading and writing numbers** (including Roman Numerals) | **Reception** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| read and write numbers from 1 to 10 in numerals and words. | read and write numbers from 1 to 20 in numerals and words. | read and write numbers to at least 100 in numerals and in words | | read and write numbers up to 1 000 in numerals and in words | |  | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit  (appears also in Comparing Numbers) | read, write, order and compare numbers up to  10 000 000 and determine the value of each digit  (appears also in Understanding Place Value) |
| Link the number symbol (numeral) with its cardinal number value |  |  | | *tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks*  (copied from Measurement) | | read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value. | read Roman numerals to 1 000 (M) and recognise years written in Roman numerals. |  |
|  | **UNDERSTANDING PLACE VALUE** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | **Milestone 2** | | | **Milestone 3** | |
| **Understanding place value** | **Reception** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| Part whole. Recognising smaller numbers within a number (conceptual subatizing) | Part whole. Recognising smaller numbers within a number (conceptual subatizing) | recognise the place value of each digit in a two-digit number (tens, ones) | | recognise the place value of each digit in a three-digit number (hundreds, tens, ones) | | recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit  (appears also in Reading and Writing Numbers) | read, write, order and compare numbers up to  10 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers) |
| Exploration of different ways in which a number can be partitioned. Incuding the composition of numbers up to 10 | Exploration of different ways in which a number can be partitioned |  | |  | | *find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as units, tenths and hundredths*  (copied from Fractions) | *recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents*  (copied from Fractions) | *identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and*  *1 000 where the answers are up to three decimal places* (copied from Fractions) |
|  | Understanding the ‘one more/one less’ relationship between consecutive numbers |  |  | |  | |  |  |  |
|  | **ROUNDING** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | | **Milestone 2** | | | **Milestone 3** | |
| **Rounding** | **Reception** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
|  |  |  | |  | | round any number to the nearest 10, 100 or 1 000 | round any number up to 1 000 000 to the nearest 10, 100, 1 000, 10 000 and 100 000 | round any whole number to a required degree of accuracy |
|  |  |  | |  | | *round decimals with one decimal place to the nearest whole number*  (copied from Fractions) | *round decimals with two decimal places to the nearest whole number and to one decimal place*  (copied from Fractions) | *solve problems which require answers to be rounded to specified degrees of accuracy* (copied from Fractions) |
|  | **PROBLEM SOLVING** | | | | | | | | |
|  |  | **Early Learning** | | | **Milestone 1** | | | **Milestone 2** | | **Milestone 3** |
|  | **REC** | **Year 1** | **Year 2** | | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| **Problem Solving** | Exploring pattern and representation of pattern within numbers up to 10 |  | use place value and number facts to solve problems | | solve number problems and practical problems involving these ideas. | | solve number and practical problems that involve all of the above and with increasingly large positive numbers | solve number problems and practical problems that involve all of the above | solve number and practical problems that involve all of the above |

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| **Progression of Skills in: Number –Addition and Subtraction** |

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|  | | **NUMBER BONDS** | | | | | | | |
|  | **Early Learning** | | **Milestone 1** | | **Milestone 2** | | | **Milestone 3** | |
| **Skill** | **Reception** | | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| **Number Bonds** | Knowing which pairs of numbers make a given number within 10 | | represent and use number bonds and related subtraction facts within 20 | recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 |  |  | |  |  |
|  | **MENTAL CALCULATION** | | | | | | | | |
| **Mental calculation** | **Reception** | | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| Recognise one more and one less than any given number to 20 drawing upon the relationship between sequential numbers | | add and subtract one-digit and two-digit numbers to 20, including zero | add and subtract numbers using concrete objects, pictorial representations, and mentally, including:   * a two-digit number and ones * a two-digit number and tens * two two-digit numbers * adding three one-digit numbers | add and subtract numbers mentally, including:   * a three-digit number and ones * a three-digit number and tens * a three-digit number and hundreds |  | | add and subtract numbers mentally with increasingly large numbers | perform mental calculations, including with mixed operations and large numbers |
| Subatize to 10 | | read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs  (appears also in Written Methods) | show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot |  |  | |  | use their knowledge of the order of operations to carry out calculations involving the four operations |
|  | **WRITTEN METHODS** | | | | | | | | |
| **Written Methods** | **Reception** | | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| Use a tens fram and part whole model to combine 2 groups | | read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs  (appears also in Mental Calculation) |  | add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction | add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate | | add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) |  |
|  | **INVERSE OPERATIONS, ESTIMATING AND CHECKING ANSWERS** | | | | | | | | |
| **Inverse operations, estimating and checking answers** | **Reception** | | **Year 1** | **Year 2** | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
| partition a number of things into two groups, and recognize that those groups can be recombined to make the same total | | partition a number of things into two groups, and recognize that those groups can be recombined to make the same total | recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. | estimate the answer to a calculation and use inverse operations to check answers | | estimate and use inverse operations to check answers to a calculation | use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. |
|  | **PROBLEM SOLVING** | | | | | | | | |
| **Problem Solving** | **Reception** | | **Year 1** | **Year 2** | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
|  | | solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as  7 = 🗆 - 9 | solve problems with addition and subtraction:   * using concrete objects and pictorial representations, including those involving numbers, quantities and measures * applying their increasing knowledge of mental and written methods | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | | solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why |
|  | |  | *solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change* (copied from Measurement) |  | |  |  | Solve problems involving addition, subtraction, multiplication and division |

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| **Progression of Skills in: Multiplication and Division** |

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|  | **MULTIPLICATION & DIVISION FACTS** | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| **Multiplication and division facts** | *Recognizing doubles of given numbers to 10 using concrete resources to aid* | *count in multiples of twos, fives and tens*  (copied from Number and Place Value) | *count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward*  (copied from Number and Place Value) | *count from 0 in multiples of 4, 8, 50 and 100*  (copied from Number and Place Value) | *count in multiples of 6, 7, 9, 25 and 1 000*  (copied from Number and Place Value) | | *count forwards or backwards in steps of powers of 10 for any given number up to*  *1 000 000*  (copied from Number and Place Value) |  |
| Know half of any given number to 10 using concrete materials to aid |  | recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers | recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables | recall multiplication and division facts for multiplication tables up to 12 × 12 | |  |  |
|  | **MENTAL CALCULATION** | | | | | | | |
| **Mental calculation** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| Calculate all doubles to 5 mentally |  |  | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods (appears also in Written Methods) | use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers | | multiply and divide numbers mentally drawing upon known facts | perform mental calculations, including with mixed operations and large numbers |
| Explore and represent double facts to 10 |  | show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot |  | recognise and use factor pairs and commutativity in mental calculations (appears also in Properties of Numbers) | | multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 | *associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8)*  (copied from Fractions) |
|  | **WRITTEN CALCULATION** | | | | | | | |
| **Written calculation** | **Reception** | **Year 1** | **Year 2** | **Year 3** | | **Year 4** | **Year 5** | **Year 6** |
|  |  | calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods (appears also in Mental Methods) | multiply two-digit and three-digit numbers by a one-digit number using formal written layout | | multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers | multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication |
|  |  |  |  |  |  | | divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context | divide numbers up to 4-digits by a two-digit whole number using the formal written method of short division where appropriate for the context divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context |
|  |  |  |  |  |  | |  | *use written division methods in cases where the answer has up to two decimal places* (copied from Fractions (including decimals)) |
|  | **PROPERTIES OF NUMBERS: MULTIPLES, FACTORS, PRIMES, SQUARE AND CUBE NUMBERS** | | | | | | | |
| **Properties of numbers: Multiples, factors, Primes** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
|  |  | recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. | estimate the answer to a calculation and use inverse operations to check answers | estimate and use inverse operations to check answers to a calculation | | use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. |
|  | **PROBLEM SOLVING** | | | | | | | |
| **Problem Solving** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
|  | solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as  7 = 🗆 - 9 | solve problems with addition and subtraction:   * using concrete objects and pictorial representations, including those involving numbers, quantities and measures * applying their increasing knowledge of mental and written methods | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why | | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why |
|  |  | *solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change* (copied from Measurement) |  |  | |  | Solve problems involving addition, subtraction, multiplication and division |

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| **Progression of Skills in: Fractions (including Decimals and Percentages)** |

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| **COUNTING IN FRACTIONAL STEPS** | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | **Year 6** |
| **COUNTING IN FRACTIONAL STEPS** |  |  | *Pupils should count in fractions up to 10, starting from any number and using the1/2 and 2/4 equivalence on the number line (Non Statutory Guidance)* | count up and down in tenths | count up and down in hundredths | |  |  |
| **RECOGNISING FRACTIONS** | | | | | | | | |
| **RECOGNISING FRACTIONS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
| Recognising part and whole | recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find, name and write fractions 1/3, 1/4, 2/4 and 3/4 of a length, shape, set of objects or quantity | recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators | recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents  (appears also in Equivalence) | |  |
| Understand that objects can be divided into parts | recognise, find and name a quarter as one of four equal parts of an object, shape or quantity |  | recognise that tenths arise from dividing an object into 10 equal parts and in dividing one – digit numbers or quantities by 10. |  |  | |  |
|  |  |  |  | recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators |  |  | |  |
|  | **COMPARING FRACTIONS** | | | | | | | |
| **COMPARING FRACTIONS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  | compare and order unit fractions, and fractions with the same denominators |  | compare and order fractions whose denominators are all multiples of the same number | | compare and order fractions, including fractions >1 |
|  | **COMPARING DECIMALS** | | | | | | | |
| **COMPARING DECIMALS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  |  | compare numbers with the same number of decimal places up to two decimal places | read, write, order and compare numbers with up to three decimal places | | identify the value of each digit in numbers given to three decimal places |
|  | **ROUNDING INCLUDING DECIMALS** | | | | | | | |
| **ROUNDING INCLUDING DECIMALS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  |  | round decimals with one decimal place to the nearest whole number | round decimals with two decimal places to the nearest whole number and to one decimal place | | solve problems which require answers to be rounded to specified degrees of accuracy |
|  | **EQUIVALENCE (INCLUDING FRACTIONS, DECIMALS AND PERCENTAGES)** | | | | | | | |
| **EQUIVALENCE (INCLUDING FRACTIONS, DECIMALS AND PERCENTAGES)** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  | write simple fractions e.g. 1/2 of 6 = 3 and recognise the equivalence of 2/4 and 1/2. | recognise and show, using diagrams, equivalent fractions with small denominators | recognise and show, using diagrams, families of common equivalent fractions | identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths | | use common factors to simplify fractions; use common multiples to express fractions in the same denomination |
|  |  |  |  | recognise and write decimal equivalents of any number of tenths or hundredths | read and write decimal numbers as fractions (e.g. 0.71 = 71/100) | | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8) |
|  |  |  |  |  | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents | |  |
|  |  |  |  | recognise and write decimal equivalents to 1/4; 1/2; 3/4 | recognise the per cent symbol (%) and understand that per cent relates to “number of parts per hundred”, and write percentages as a fraction with denominator 100 as a decimal fraction | | recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. |
|  | **ADDITION AND SUBTRACTION OF FRACTIONS** | | | | | | | |
| **ADDITION AND SUBTRACTION OF FRACTIONS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
| Put together two halves of an object to make the whole |  |  | add and subtract fractions with the same denominator within one whole (e.g. 5/7 + 1/7 = 6/7) | add and subtract fractions with the same denominator | add and subtract fractions with the same denominator and multiples of the same number | | add and subtract fractions with different denominators and mixed numbers, using the  concept of equivalent fractions |
|  |  |  |  |  | recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number (e.g. 2/5 + 4/5 = 6/5 = 11/5) | |  |
|  | **MULTIPLICATION AND DIVISION OF FRACTIONS** | | | | | | | |
| **MULTIPLICATION AND DIVISION OF FRACTIONS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  |  |  | multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams | | multiply simple pairs of proper fractions, writing the answer in its simplest form (e.g. 1/4 × 1/2 = 1/8) |
|  |  |  |  |  |  | | multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  |  |  |  | | divide proper fractions by whole numbers (e.g. 1/3 ÷ 2 = 1/6 ) |
|  | **MULTIPLICATION AND DIVISION OF DECIMALS** | | | | | | | |
| **ADDITION AND SUBTRACTION OF FRACTIONS** | **reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  |  |  |  | | multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  |  | find the effect of dividinga one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths |  | | multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  |  | | identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100  and 1000 where the answers are up to three decimal places |
|  |  |  |  |  |  |  | | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction  (e.g. 3/8) |
|  |  |  |  |  |  |  | | use written division methods in cases where the answer has up to two decimal places |
|  | **PROBLEM SOLVING** | | | | | | | |
| **PROBLEM SOLVING** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** |
|  |  |  | solve problems that involve all of the above | solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | solve problems involving numbers up to three decimal places | |  |
|  |  |  |  | solve simple measure and money problems involving fractions and decimals to two decimal places. | solve problems which require knowing percentage and decimal equivalents of 1/2, 1/4, 1/5, 2/5, 4/5 and those with a denominator of a multiple of 10 or 25. | |  |

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| **Progression of Skills in: Ratio and Proportion** |

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|  | **Statements only appear in Year 6 but should be connected to previous learning, particularly fractions and multiplication and division** | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **Ratio and Proportion** | *Sort objects to show twice as many* | *Sort objects and recognise twice as many using diagrams such as a bar model Non statutory* | *Use bar models to represent simple proportional problems Non statutory* | *Use bar models to represent Non statutory proportional problems Non statutory* | *Use bar models to represent simple proportional problems Non statutory* | *Use bar models to represent multi-step proportional problems Non statutory* | solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts |
|  |  |  |  |  |  | solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison |
|  |  |  |  |  |  |  | solve problems involving similar shapes where the scale factor is known or can be found |
|  |  |  |  |  |  | solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. |

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| **Progression of Skills in: Measurement** |

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|  | **COMPARING AND ESTIMATING** | | | | | | | | | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | | **Year 6** | |
| **COMPARING AND ESTIMATING** | Recognise bigger an smaller lengths | compare, describe and solve practical problems for:   * lengths and heights [e.g. long/short, longer/shorter, tall/short, double/half] * mass/weight [e.g. heavy/light, heavier than, lighter than] * capacity and volume [e.g. full/empty, more than, less than, half, half full, quarter] * time [e.g. quicker, slower, earlier, later] | compare and order lengths, mass, volume/capacity and record the results using >, < and = |  | estimate, compare and calculate different measures, including money in pounds and pence  (also included in Measuring) | | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm2) and square metres (m2) and estimate the area of irregular shapes (also included in measuring) | | calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm3) and cubic metres (m3), and extending to other units such as mm3 and km3. | |
|  |  |  |  |  | | estimate volume (e.g. using 1 cm3 blocks to build cubes and cuboids) and capacity (e.g. using water) | |  | |
| Begin to sequence events in chronological order using language [e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] | sequence events in chronological order using language [e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] | compare and sequence intervals of time | compare durations of events, for example to calculate the time taken by particular events or tasks |  | |  | |  | |
|  |  |  |  | estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o’clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight (appears also in Telling the Time) |  | |  | |  | |
| **MEASURING and CALCULATING** | | | | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | | **Milestone 3** | | | | |
| **MEASURING and CALCULATING** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | | | **Year 6** | |
| Compare length, weight and capacity | measure and begin to record the following:   * **lengths and heights** * **mass/weight** * **capacity and volume** * **time** (hours, minutes, seconds**)** | choose and use appropriate standard units to estimate and measure **length/height** in any direction (m/cm); **mass** (kg/g); **temperature** (°C); **capacity** (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels | measure, compare, add and subtract: **lengths** (m/cm/mm); **mass** (kg/g); **volume/capacity** (l/ml) | estimate, compare and calculate **different measures,** including **money in pounds and pence**  (appears also in Comparing) | | use all four operations to solve problems involving measure (e.g. **length, mass, volume, money**) using decimal notation including scaling. | | | solve problems involving the calculation and conversion of **units of measure**, using decimal notation up to three decimal places where appropriate  (appears also in Converting) | |
|  |  |  | measure the **perimeter** of simple 2-D shapes | measure and calculate the **perimeter** of a rectilinear figure (including squares) in centimetres and metres | | measure and calculate the **perimeter** of composite rectilinear shapes in centimetres and metres | | | recognise that shapes with the same areas can have different **perimeters** and vice versa | |
|  |  | recognise and know the value of different denominations of **coins and notes** | recognise and use symbols for pounds **(£) and pence (p)**; combine amounts to make a particular value | add and subtract amounts of **money** to give change, using both £ and p in practical contexts |  | |  | | |  | |
|  |  | find different combinations of coins that equal the same amounts of money |  |  | |  | | |  | |
|  |  | **solve simple problems** in a practical context involving addition and subtraction of money of the same unit, including giving change |  |  | |  | | |  | |
|  |  |  |  | find the area of rectilinear shapes by counting squares | | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm2) and square metres (m2) and estimate the area of irregular shapes  *recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3)*  (copied from Multiplication and Division) | | | calculate the area of parallelograms and triangles | |
|  |  |  |  |  |  | |  | | | calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) and cubic metres (m3), and extending to other units [e.g. mm3 and km3]. | |
|  |  |  |  |  | |  | | | recognise when it is possible to use formulae for area and volume of shapes | |
| **TELLING THE TIME** | | | | | | | | | | | | |
| **TELLING THE TIME** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | | **Year 5** | | | **Year 6** | | |
| Know that there are seven days in a week and recite these inorder | tell the time to the hour and half past the hour and draw the hands on a clock face to show these times. | tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times. | tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks | read, write and convert time between analogue and digital 12 and 24-hour clocks  (appears also in Converting) | |  | | |  | | |
| Recognise that there ate 12 months which total a year | recognise and use language relating to dates, including days of the week, weeks, months and years | know the number of minutes in an hour and the number of hours in a day.  (appears also in Converting) | estimate and read  time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o’clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight  (appears also in Comparing and Estimating) |  | |  | | |  | | |
| Begin to describe sequence of events, real or fictional using words such as first, then… |  |  |  | solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days  (appears also in Converting) | | solve problems involving converting between units of time | | |  | | |
|  | **CONVERTING** | | | | | | | | | | |
| **CONVERTING** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | | **Year 6** | | | | |
|  |  | know the number of minutes in an hour and the number of hours in a day.  (appears also in Telling the Time) | know the number of seconds in a minute and the number of days in each month, year and leap year | convert between different units of measure (e.g. kilometre to metre; hour to minute) | convert between different units of metric measure (e.g. kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) | | use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places | | | | |
|  |  |  |  |  | read, write and convert time between analogue and digital 12 and 24-hour clocks  (appears also in Converting) | solve problems involving converting between units of time | | solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate  (appears also in Measuring and Calculating) | | | | |
|  |  |  |  | solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days  (appears also in Telling the Time) | understand and use equivalences between metric units and common imperial units such as inches, pounds and pints | | convert between miles and kilometres | | | | |

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| **Progression of Skills in: Geometry-Properties of Shapes** |

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| **IDENTIFYING SHAPES AND THIER PROPERTIES** | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **IDENTIFYING SHAPES AND THIER PROPERTIES** | Recognise different 3D shapes from different perspectives developing spatial awareness | recognise and name common 2-D and 3-D shapes, including:   * 2-D shapes [e.g. rectangles (including squares), circles and triangles] * 3-D shapes [e.g. cuboids (including cubes), pyramids and spheres]. | identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line |  | identify lines of symmetry in 2-D shapes presented in different orientations | identify 3-D shapes, including cubes and other cuboids, from 2-D representations | recognise, describe and build simple 3-D shapes, including making nets  (appears also in Drawing and Constructing) |
| Explore the different attributes of shape  and to select shapes to fulfil a particular need |  | identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces |  |  |  | illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius |
| Identifying similarities between shapes |  | identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] |  |  |  |  |
|  | Talk about and explore 2D and 3D shapes using informal mathematical language |  |  |  |  |  |  |
| **DRAWING AND CONSTRUCTING** | | | | | | | |
| **DRAWING AND CONSTRUCTING** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| Draw shapes using simple representations | Draw shapes using simple representations |  | draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them | complete a simple symmetric figure with respect to a specific line of symmetry | draw given angles, and measure them in degrees (o) | draw 2-D shapes using given dimensions and angles |
| Combine shapes to make new ones |  |  |  |  |  | recognise, describe and build simple 3-D shapes, including making nets (appears also in Identifying Shapes and Their Properties) |
| **COMPARING AND CLASSIFYING** | | | | | | | |
| **COMPARING AND CLASSIFYING** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| Begin to describe shape using their properties using both formal and informal language | compare and sort common 2-D and 3-D shapes and everyday objects |  | compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes | use the properties of rectangles to deduce related facts and find missing lengths and angles | compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons |  |
|  |  |  |  |  |  | distinguish between regular and irregular polygons based on reasoning about equal sides and angles |  |
| **ANGLES** | | | | | | | |
| **ANGLES** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| Manipulate shapes to develop spatial reasoning |  |  | recognise angles as a property of shape or a description of a turn |  | know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles |  |
|  |  |  |  | identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle | identify acute and obtuse angles and compare and order angles up to two right angles by size | identify:   * angles at a point and one whole turn (total 360o) * angles at a point on a straight line and ½ a turn (total 180o) * other multiples of 90o | recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles |
|  |  |  |  | identify horizontal and vertical lines and pairs of perpendicular and parallel lines |  |  |  |

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| **Progression of Skills in: Geometry-Position and Direction** |

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| **POSITION, DIRECTION AND MOVEMENT** | | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **POSITION, DIRECTION AND MOVEMENT** | Develop spatial vocabulary position: 'in', 'on', 'under' direction: 'up', 'down', 'across'. | describe position, direction and movement, including half, quarter and three-quarter turns. | use mathematical vocabulary to describe position, direction and movement including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and  anti-clockwise) |  | describe positions on a  2-D grid as coordinates in the first quadrant | identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed | describe positions on the full coordinate grid (all four quadrants) |
| use terms which are relative to the viewpoint:’in front of', 'behind', 'forwards',' backward's ('left' and 'right' to be used later on as ideas develop). |  |  |  | describe movements between positions as translations of a given unit to the left/right and up/down |  | draw and translate simple shapes on the coordinate plane, and reflect them in the axes. |
| Draw information from a simple map |  |  |  | plot specified points and draw sides to complete a given polygon |  |  |
| **PATTERN** | | | | | | | |
| **PATTERN** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| to see a pattern, to talk about what they can see, and to continue a pattern. |  | order and arrange combinations of mathematical objects in patterns and sequences |  |  |  |  |
| Making patterns:  AB pattern and spotting error within  Continuing an ABC pattern  Making own ABB,ABAB and ABBC patterns  Continuing a pattern which ends mid unit |  |  |  |  |  |  |
| Record simple patterns |  |  |  |  |  |  |
| Make patterns around a pace |  |  |  |  |  |  |
| Study patterns within our environment |  |  |  |  |  |  |
| gain experience of symbolising patterns, develop experience of pattern structure and identify the unit of repeat and express it, Use this knowledge to create a pattern in a different medium, which follows the same structure. |  |  |  |  |  |  |

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| **Progression of Skills in: Statistics** |

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|  | **INTERPRETING, CONSTRUCTING AND PRESENTING DATA** | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **INTERPRETING, CONSTRUCTING AND PRESENTING DATA** | Experiment with their own symbols and marks as well as numerals |  | interpret and construct simple pictograms, tally charts, block diagrams and simple tables | interpret and present data using bar charts, pictograms and tables | interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs | complete, read and interpret information in tables, including timetables | interpret and construct pie charts and line graphs and use these to solve problems |
|  |  | ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity |  |  |  |  |
|  |  | ask and answer questions about totalling and comparing categorical data |  |  |  |  |
| **SOLVING PROBLEMS** | | | | | | | |
| **SOLVING PROBLEMS** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
|  |  |  | solve one-step and two-step questions [e.g. ‘How many more?’ and ‘How many fewer?’] using information presented in scaled bar charts and pictograms and tables. | solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs. | solve comparison, sum and difference problems using information presented in a line graph | calculate and interpret the mean as an average |

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| **Progression of Skills in: Algebra** |

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|  | **EQUATIONS** | | | | | | |
|  | **Early Learning** | **Milestone 1** | | **Milestone 2** | | **Milestone 3** | |
| **Skill** | **Reception** | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
| **EQUATIONS** |  | *solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and* ***missing number problems*** *such as*  *7 =* 🗆 *- 9*  (copied from Addition and Subtraction) | *recognise and use the inverse relationship between addition and subtraction and use this to check calculations and* ***missing number*** *problems.*  (copied from Addition and Subtraction) | solve problems, *including* ***missing number*** *problems, using number facts, place value, and more complex addition and subtraction.* (copied from Addition and Subtraction) |  | *use the properties of rectangles to deduce related facts and find* ***missing lengths and angles***  (copied from Geometry: Properties of Shapes) | express missing number problems algebraically |
|  |  |  | *solve problems, including* ***missing number*** *problems, involving multiplication and division, including integer scaling*  (copied from  Multiplication and Division) |  |  |  |
|  |  | *recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100*  (copied from Addition and Subtraction) |  |  |  | find pairs of numbers that satisfy number sentences involving two unknowns |
| **FORMULAE** | | | | | | | |
| **FORMULAE** |  | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
|  |  |  |  | *Perimeter can be expressed algebraically as 2(a + b) where a and b are the dimensions in the same unit.*  *(Copied from NSG measurement)* |  | use simple formulae |
|  |  |  |  |  |  | *recognise when it is possible to use* ***formulae*** *for area and volume of shapes*  (copied from Measurement) |
| **SEQUENCES** | | | | | | | |
| **SEQUENCES** |  | **Year 1** | **Year 2** | **Year 3** | **Year 4** | **Year 5** | **Year 6** |
|  | *sequence events in chronological order using language such as: before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening*  (copied from Measurement) | *compare and sequence intervals of time*  (copied from Measurement) |  |  |  | generate and describe linear number sequences |
|  |  |  | *order and arrange combinations of mathematical objects in patterns*  (copied from Geometry: position and direction) |  |  |  |  |