



## **ST. ANDREW'S CE PRIMARY SCHOOL**

This Calculation Policy reflects St. Andrew's Church of England Primary School's mission statement, our Christian values and the ethos of the school. It was written with our Christian values of Perseverance and Wisdom in mind.

### **CALCULATION POLICY**

#### **Introduction**

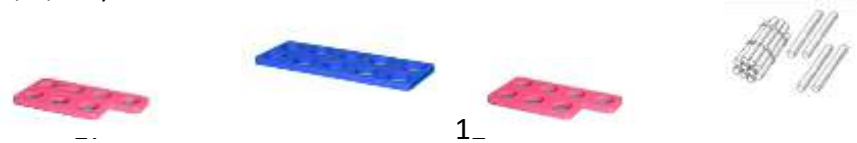
Children are introduced to the processes of calculation through practical, oral and mental activities. As they begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, so that they develop both conceptual understanding and fluency in the fundamentals of mathematics. Whilst interpreting signs and symbols involved with calculation, orally in the first instance, children use models and images to support their mental and written methods of calculation. As children's mental methods are strengthened and refined they begin to work more efficiently, which will support them with using succinct written calculation strategies as they are developed.

#### **From FS to Year 1**

There are fundamental skills that it is important for children to develop an early understanding of as building blocks to future learning in maths, including that linked to calculation. A selection of the skills include:

- Ordinality – 'the ordering of numbers in relation to one another' – e.g. (1, 2, 3, 4, 5...)

- Cardinality – 'understanding the value of different numbers' – e.g. (7 =

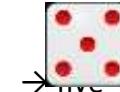


- Equality – ‘seven is the same total as four add three’ – e.g.

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- Subitising – ‘instantly recognizing the number of objects in a small group, without counting them’ – e.g.



- Conservation of number – ‘recognising that a value of objects are the same, even if they are laid out differently’ – e.g.



- One-to-one correspondence – e.g.



- Counting on and back from any number – e.g. ‘five add three more totals eight’



- ‘ten take away three totals seven’



- Using apparatus and objects to represent and communicate thinking – e.g.



- Maths language – using mathematical words verbally in every-day situations – e.g. ‘climb up to the top’ / ‘climb down to the bottom’

The ability to calculate mentally forms the basis of all methods of calculation and has to be maintained and refined. A good knowledge of numbers or a ‘feel’ for numbers is the product of structured practice through progression in relevant practical maths experiences and visual representations.

### Key Stage 1

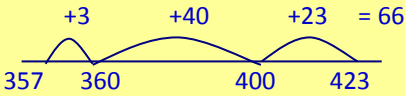
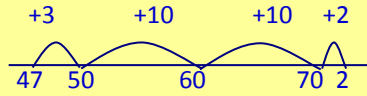
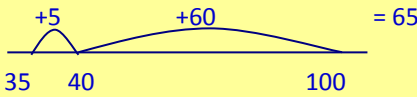
Year		Mental calculation	Written Calculation	Default for ALL children
	<i>Overview of KS1</i>	Children in Years 1 and 2 will be given a really solid foundation in the basic building blocks of mental and written arithmetic. Through being taught place value, they will develop an understanding of how numbers work, so that they are confident in 2-digit numbers and beginning to read and say numbers above 100. A focus on number bonds, first via practical hands-on experiences and subsequently using memorisation techniques, enables a good grounding in these crucial facts, and ensures that all children leave Y2 knowing the pairs of numbers which make all the numbers up to 10 at least. They will also have experienced and been taught pairs to 20. Their knowledge of number facts enables them to add several single-digit numbers, and to add/subtract a single digit number to/from a 2-digit number. Another important conceptual tool is their ability to add/subtract 1 or 10, and to understand which digit changes and why. This understanding is extended to enable children to add and subtract multiples of ten to and from any 2-digit number. The most important application of this knowledge is their ability to add or subtract any pair of 2-digit numbers by counting on or back in tens and ones. Children may extend this to adding by partitioning numbers into tens and ones. Children will be taught to count in 2s, 3s, 5s and 10s, and will have related this skill to repeated addition. They will have met and begun to learn the associated 2x, 3x, 5x and 10x tables. Engaging in a practical way with the concept of repeated addition and the use of arrays enables children to develop a preliminary understanding of multiplication, and asking them to consider how many groups of a given number make a total will introduce them to the idea of division. They will also be taught to double and halve numbers, and will thus experience scaling up or down as a further aspect of multiplication and division. Fractions will be introduced as numbers and as operators, specifically in relation to halves, quarters and thirds.		
		Mental calculation	Written Calculation	Default for ALL children
<b>Year 1</b>	<i>Addition</i>	Number bonds ('story of' 5, 6, 7, 8, 9 and 10) Count on in ones from a given 2-digit number Add two single-digit numbers Add three single-digit numbers spotting doubles or pairs to 10 Count on in tens from any given 2-digit number Add 10 to any given 2-digit number Use number facts to add single-digit numbers to two-digit numbers, e.g. use $4 + 3$ to work out $24 + 3$ , $34 + 3$ ... Add by putting the larger number first	See Appendix A	Pairs with a total of 10 Counting in ones Counting in tens Count on 1 from any given 2-digit number

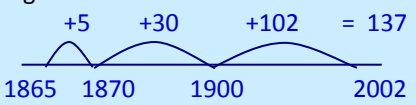
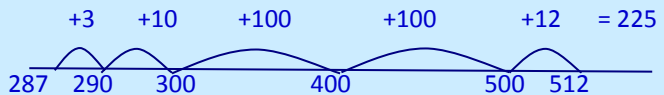
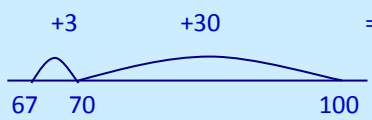
Year		Mental calculation	Written Calculation	Default for ALL children
	<b>Subtraction</b>	Number bonds ('story of' 5, 6, 7, 8, 9 and 10) Count back in ones from a given 2-digit number Subtract one single-digit number from another Count back in tens from any given 2-digit number Subtract 10 from any given 2-digit number Use number facts to subtract single-digit numbers from two-digit numbers, e.g. use $7 - 2$ to work out $27 - 2$ , $37 - 2$ ...	See Appendix A	Pairs with a total of 10 Counting back in ones from 20 to 0 Counting back in tens from 100 to 0 Count back 1 from any given 2-digit number
	<b>Multiplication</b>	Begin to count in 2s, 5s and 10s Begin to say what three 5s are by counting in 5s or what four 2s are by counting in 2s, etc. Double numbers to 10	See Appendix A	Begin to count in 2s and 10s Double numbers to 5 using fingers
	<b>Division</b>	Begin to count in 2s, 5s and 10s Find half of even numbers to 12 and know it is hard to halve odd numbers Find half of even numbers by sharing Begin to use visual and concrete arrays or 'sets of' to find how many sets of a small number make a larger number.	See Appendix A	Begin to count in 2s and 10s Find half of even numbers by sharing
<b>Year 2</b>	<b>Addition</b>	Number bonds – knowing all the pairs of numbers which make all the numbers to 12, and pairs with a total of 20 Count on in ones and tens from any given 2-digit number Add two or three single-digit numbers Add a single-digit number to any 2-digit number using number facts, including bridging multiples of 10. (E.g. $45 + 4$ , $38 + 7$ ) Add 10 and small multiples of 10 to any given 2-digit number Add any pair of 2-digit numbers	See Appendix A	Know pairs of numbers which make each total up to 10 Add two single digit numbers Add a single-digit number to a 2-digit number by counting on in ones Add 10 and small multiples of 10 to a 2-digit number by counting on in tens

Year		Mental calculation	Written Calculation	Default for ALL children
	<b>Subtraction</b>	<p>Number bonds – knowing all the pairs of numbers which make all the numbers to 12</p> <p>Count back in ones and tens from any given 2-digit number</p> <p>Subtract a single-digit number from any 2-digit number using number facts, including bridging multiples of 10, e.g. <math>56 - 3</math>, <math>53 - 5</math>.</p> <p>Subtract 10 and small multiples of 10 from any given 2-digit number</p> <p>Subtract any pair of 2-digit numbers by counting back in tens and ones or by counting up.</p>	See Appendix A	<p>Know pairs of numbers which make each total up to 10</p> <p>Subtract a single-digit number from a 2-digit number by counting back in ones</p> <p>Subtract 10 and small multiples of 10 from a 2-digit number by counting back in tens</p>
	<b>Multiplication</b>	<p>Count in 2s, 5s and 10s</p> <p>Begin to count in 3s.</p> <p>Begin to understand that multiplication is repeated addition and to use arrays (E.g. <math>3 \times 4</math> is three rows of 4 dots)</p> <p>Begin to learn the 2x, 3x, 5x and 10x tables, seeing these as 'lots of', e.g. 5 lots of 2, 6 lots of 2, 7 lots of 2, etc.</p> <p>Double numbers up to 20</p> <p>Begin to double multiples of 5 to 100</p> <p>Begin to double two-digit numbers less than 50 with 1s digits of 1, 2, 3 4 or 5</p>	See Appendix A	<p>Count in 2s, 5s and 10s</p> <p>Begin to use and understand simple arrays, e.g. <math>2 \times 4</math> is two lots of four buns.</p> <p>Double numbers up to 10</p> <p>Double multiples of 10 to 50</p>
	<b>Division</b>	<p>Count in 2s, 5s and 10s</p> <p>Begin to count in 3s</p> <p>Using fingers, say where a given number is in the 2s, 5s or 10s count. (E.g. 8 is the fourth number when I count in twos.)</p> <p>Relate division to grouping. (E.g. how many groups of five in fifteen?)</p> <p>Halve numbers to 20</p> <p>Begin to halve numbers to 40 and multiples of 10 to 100</p> <p>Find <math>\frac{1}{2}</math>, <math>\frac{1}{3}</math>, <math>\frac{1}{4}</math> and <math>\frac{3}{4}</math> of a quantity of objects and of amounts (whole number answers)</p>	See Appendix A	<p>Count in 2s, 5s and 10s</p> <p>Say how many rows in a given array. (E.g. how many rows of 5 in an array of <math>3 \times 5</math>)</p> <p>Halve numbers to 12</p> <p>Find <math>\frac{1}{2}</math> of amounts</p>

## Lower Key stage 2

	<b>Overview of LKS2</b>	<p>In the lower juniors, children build on the concrete and conceptual understandings they have gained in the Infants to develop a real mathematical understanding of the four operations, in particular developing arithmetical competence in relation to larger numbers. In addition and subtraction, they are taught to use place value and number facts to add and subtract numbers mentally and will develop a range of strategies to enable them to discard the 'counting in ones' or fingers-based methods of the infants. In particular, they will learn to add and subtract multiples and near multiples of 10, 100 and 1000, and will become fluent in complementary addition as an accurate means of achieving fast and accurate answers to 3-digit subtractions. Standard written methods for adding larger numbers are taught, learned and consolidated, and written column subtraction is also introduced. This key stage is also the period during which all the multiplication and division facts are thoroughly memorised, including all facts up to the 12 x 12 table. Efficient written methods for multiplying or dividing a 2-digit or 3-digit number by as single-digit number are taught, as are mental strategies for multiplication or division with large but friendly numbers, e.g. when dividing by 5 or multiplying by 20. Children will develop their understanding of fractions, learning to reduce a fraction to its simplest form as well as finding non-unit fractions of amounts and quantities. The concept of a decimal number is introduced and children consolidate a firm understanding of one-place decimals, multiplying and dividing whole numbers by 10 and 100.</p>		
<b>Year 3</b>	<b>Addition</b>	<p>Know pairs with each total to 20            Know pairs of multiples of 10 with a total of 100            Add any two 2-digit numbers by counting on in 10s and 1s or by using partitioning            Add multiples and near multiples of 10 and 100            Perform place value additions without a struggle. (E.g. <math>300 + 8 + 50 = 358</math>)            Use place value and number facts to add a 1-digit or 2-digit number to a 3-digit number. (E.g. <math>104 + 56</math> is 160 since <math>104+50=154</math> and <math>6+4=10</math> and <math>676 + 8</math> is 684 since <math>8=4+4</math> and <math>76+4+4=84</math>)            Add pairs of 'friendly' 3-digit numbers, e.g. <math>320 + 450</math>            Begin to add amounts of money using partitioning.</p>	<p>Use expanded column addition to add two or three 3-digit numbers or three 2-digit numbers            Begin to use compact column addition to add numbers with three digits.            Begin to add like fractions. (E.g. <math>\frac{3}{8} + \frac{1}{8} + \frac{1}{8}</math>)            Recognise fractions that add to 1. (E.g. <math>\frac{1}{4} + \frac{3}{4}</math> or <math>\frac{3}{5} + \frac{2}{5}</math>)</p>	<p>Know pairs of numbers which make each total up to 10, and which total 20            Add two 2-digit numbers by counting on in tens and ones (E.g. <math>56 + 35</math> is <math>56 + 30</math> and then add the 5)            Understand simple place value additions: <math>200 + 40 + 5 = 245</math>            Use place value to add multiples of 10 or 100</p>

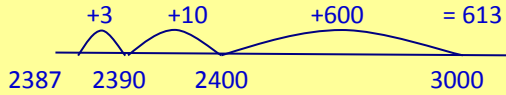
<b>Subtraction</b>	<p>Know pairs with each total to 20</p> <p>Subtract any two 2-digit numbers</p> <p>Perform place value subtractions without a struggle. (E.g. <math>536 - 30 = 506</math>, etc.)</p> <p>Subtract 2-digit numbers from numbers &gt;100 by counting up. (E.g. <math>143 - 76</math> is done by starting at 76, add 4 (80) then add 20 (100) then add 43 making the difference a total of 67)</p> <p>Subtract multiples and near multiples of 10 and 100</p> <p>Subtract, when appropriate, by counting back or taking away, using place value and number facts.</p> <p>Find change from £1, £5 and £10.</p>	<p>Use counting up as an informal written strategy for subtracting pairs of three-digit numbers, e.g. <math>423 - 357</math> is</p>  <p>Begin to subtract like fractions. (E.g. <math>\frac{7}{8} - \frac{3}{8}</math>)</p>	<p>Know pairs of numbers which make each total up to 10, and which total 20</p> <p>Count up to subtract 2-digit numbers: <math>72 - 47</math> is</p>  <p>Subtract multiples of 5 from 100 by counting up</p>  <p>Subtract multiples of 10 and 100</p>
<b>Multiplication</b>	<p>Know by heart all the multiplication facts in the 2x, 3x, 4x, 5x, 8x and 10x tables</p> <p>Multiply whole numbers by 10 and 100</p> <p>Recognise that multiplication is commutative</p> <p>Use place value and number facts in mental multiplication. (E.g. <math>30 \times 5</math> is <math>15 \times 10</math>)</p> <p>Partition teen numbers to multiply by a single-digit number. (E.g. <math>3 \times 14</math> as <math>3 \times 10</math> and <math>3 \times 4</math>)</p> <p>Double numbers up to 50</p>	<p>Use partitioning (grid multiplication) to multiply 2-digit and 3-digit numbers by 'friendly' single digit numbers.</p>	<p>Know by heart the 2x, 3x, 5x and 10x tables</p> <p>Double given tables facts to get others</p> <p>Double numbers up to 25 and multiples of 5 to 50</p>
<b>Division</b>	<p>Know by heart all the division facts derived from the 2x, 3x, 4x, 5x, 8x and 10x tables.</p> <p>Divide whole numbers by 10 or 100 to give whole number answers</p> <p>Recognise that division is not commutative.</p> <p>Use place value and number facts in mental division. (E.g. <math>84 \div 4</math> is half of 42)</p> <p>Divide larger numbers mentally by subtracting the tenth multiple, including those with remainders. (E.g. <math>57 \div 3</math> is <math>10 + 9</math> as <math>10 \times 3 = 30</math> and <math>9 \times 3 = 27</math>)</p> <p>Halve even numbers to 100, halve odd numbers to 20</p>	<p>Perform divisions just above the 10<sup>th</sup> multiple using the written layout and understanding how to give a remainder as a whole number.</p> <p>Find unit fractions of quantities and begin to find non-unit fractions of quantities</p>	<p>Know by heart the division facts derived from the 2x, 3x, 5x and 10x tables</p> <p>Halve even numbers up to 50 and multiples of ten to 100</p> <p>Perform divisions within the tables including those with remainders, e.g. <math>38 \div 5</math>.</p>

<b>Year 4</b>	<b>Addition</b>	<p>Add any two 2-digit numbers by partitioning or counting on Know by heart/quickly derive number bonds to 100 and to £1 Add to the next hundred, pound and whole number. (E.g. <math>234 + 66 = 300</math>, <math>3.4 + 0.6 = 4</math>) Perform place value additions without a struggle. (E.g. <math>300 + 8 + 50 + 4000 = 4358</math>) Add multiples and near multiples of 10, 100 and 1000. Add £1, 10p, 1p to amounts of money Use place value and number facts to add 1-, 2-, 3-and 4-digit numbers where a mental calculation is appropriate'. (E.g. <math>4004 + 156</math> by knowing that <math>6+4=10</math> and that <math>4004+150=4154</math> so total is 4160)</p>	<p>Column addition for 3-digit and 4-digit numbers Add like fractions, e.g. <math>\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}</math>. Be confident with fractions that add to 1 and fraction complements to 1. (E.g. <math>\frac{2}{3} + ? = 1</math>)</p>	<p>Add any 2-digit numbers by partitioning or counting on Number bonds to 20 Know pairs of multiples of 10 with a total of 100 Add friendly larger numbers using knowledge of place value and number facts Use expanded column addition to add 3-digit numbers</p>
	<b>Subtraction</b>	<p>Subtract any two 2-digit numbers Know by heart/quickly derive number bonds to 100 Perform place value subtractions without a struggle. (E.g. <math>4736 - 706 = 4030</math>, etc.) Subtract multiples and near multiples of 10, 100 and 100 Subtract by counting up. (E.g. <math>503 - 368</math> is done by adding: <math>368 + 2 + 30 + 100 + 3</math> so we added 135) Subtract, when appropriate, by counting back or taking away, using place value and number facts. Subtract £1, 10p, 1p from amounts of money Find change from £10, £20 and £50.</p>	<p>Use expanded column subtraction for 3-digit and 4-digit numbers Use complementary addition to subtract amounts of money, and for subtractions where the larger number is a near multiple of 1000 or 100 E.g. <math>2002 - 1865</math> is</p>  <p style="text-align: center;"><math>1865 \quad 1870 \quad 1900 \quad 2002</math></p> <p>Subtract like fractions, e.g. <math>\frac{1}{4} + \frac{1}{8} = \frac{3}{8}</math> Use fractions that add to 1 to find fraction complements to 1, e.g. <math>1 - \frac{2}{3} = \frac{1}{3}</math></p>	<p>Use counting up with confidence to solve most subtractions, including finding complements to multiples of 100. (E.g. <math>512 - 287</math> is done by</p>  <p style="text-align: center;"><math>287 \quad 290 \quad 300 \quad 400 \quad 500 \quad 512</math></p> <p><math>67 + ? = 100</math></p>  <p style="text-align: center;"><math>67 \quad 70 \quad 100</math></p> <p style="text-align: right;"><math>= 33</math></p>



<b>Multiplication</b>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math>. Recognise factors up to 12 of two-digit numbers. Multiply whole numbers and one-place decimals by 10, 100, 1000 Multiply multiples of 10, 100, 1000 by single digit numbers. (E.g. <math>300 \times 6</math> or <math>4000 \times 8</math>) Use understanding of place value and number facts in mental multiplication. (E.g. <math>36 \times 5</math> is half of <math>36 \times 10</math> and <math>50 \times 60 = 3000</math>) Partition 2-digit numbers to multiply by a single-digit number mentally. (E.g. <math>4 \times 24</math> as <math>4 \times 20</math> and <math>4 \times 4</math>) Multiply near multiples using rounding. (E.g. <math>33 \times 19</math> as <math>33 \times 20 - 33</math>) Find doubles to double 100 and beyond using partitioning Begin to double amounts of money. (E.g. £35.60 doubled = £71.20.)</p>	<p>Use a vertical written method to multiply a one-digit by a 3-digit number (ladder) Use an efficient written method to multiply a 2-digit number by a number between 10 and 20 by partitioning (grid method)</p>	<p>Know by heart multiplication tables up to <math>10 \times 10</math> Multiply whole numbers by 10 and 100 Use grid method to multiply a 2-digit or a 3-digit number by a number up to and including 6</p>
<b>Division</b>	<p>Know by heart all the division facts up to <math>144 \div 12</math>. Divide whole numbers by 10, 100 to give whole number answers or answers with one decimal place Divide multiples of 100 by 1-digit numbers using division facts. (E.g. <math>3200 \div 8 = 400</math>) Use place value and number facts in mental division. (E.g. <math>245 \div 20</math> is double <math>245 \div 10</math>) Divide larger numbers mentally by subtracting the <math>10^{\text{th}}</math> or <math>20^{\text{th}}</math> multiple as appropriate. (E.g. <math>156 \div 6</math> is <math>20 + 6</math> as <math>20 \times 6 = 120</math> and <math>6 \times 6 = 36</math>) Find halves of even numbers to 200 and beyond using partitioning Begin to halve amounts of money. (E.g. Half of £52.40 = £26.20)</p>	<p>Use a written method to divide a 2-digit or a 3-digit number by a single-digit number. Give remainders as whole numbers. Begin to reduce fractions to their simplest forms. Find unit and non-unit fractions of larger amounts.</p>	<p>Know by heart all the division facts up to <math>100 \div 10</math>. Divide whole numbers by 10 and 100 to give whole number answers or answers with one decimal place Perform divisions just above the <math>10^{\text{th}}</math> multiple using the written layout and understanding how to give a remainder as a whole number. Find unit fractions of amounts</p>

**Upper Key stage 2**

	<b>Overview of LKS2</b>	<p>Children move on from dealing mainly with whole numbers to performing arithmetic operations with both decimals and fractions. They will consolidate their use of written procedures in adding and subtracting whole numbers with up to 6 digits and also decimal numbers with up to two decimal places. Mental strategies for adding and subtracting increasingly large numbers will also be taught. These will draw upon children’s robust understanding of place value and knowledge of number facts. Efficient and flexible strategies for mental multiplication and division are taught and practised, so that children can perform appropriate calculations even when the numbers are large, such as <math>40,000 \times 6</math> or <math>40,000 \div 8</math>. In addition, it is in Y5 and Y6 that children extend their knowledge and confidence in using written algorithms for multiplication and division. Fractions and decimals are also added, subtracted, divided and multiplied, within the bounds of children’s understanding of these more complicated numbers, and they will also calculate simple percentages and ratios. Negative numbers will be added and subtracted.</p>		
<b>Year 5</b>	<b>Addition</b>	<p>Know numbers bonds to 1 and to the next whole number            Add to the next 10 from a decimal number, e.g. <math>13.6 + 6.4 = 20</math>            Add numbers with two significant digits only, using mental strategies. (E.g. <math>3.4 + 4.8</math> or <math>23,000 + 47,000</math>)            Add one or two-digit multiples of 10, 100, 1000, 10,000 and 100,000. (E.g. <math>8000 + 7000</math> or <math>600,000 + 700,000</math>)            Add near multiples of 10, 100, 1000, 10,000 and 100,000 to other numbers. (E.g. <math>82,472 + 30,004</math>)            Add decimal numbers which are near multiples of 1 or 10, including money. (E.g. <math>6.34 + 1.99</math> or <math>£34.59 + £19.95</math>)            Use place value and number facts to add two or more friendly numbers including money and decimals. (E.g. <math>3 + 8 + 6 + 4 + 7</math>, <math>0.6 + 0.7 + 0.4</math>, or <math>2,056 + 44</math>)</p>	<p>Use column addition to add two or three whole numbers with up to 5 digits            Use column addition to add any pair of two-place decimal numbers including amounts of money.            Begin to add related fractions using equivalences. (E.g. <math>\frac{1}{2} + \frac{1}{6} = \frac{3}{6} + \frac{1}{6}</math>)            Choose the most efficient method in any given situation</p>	<p>Add numbers with only 2-digits which are not zeros, e.g. <math>3.4 + 5.8</math>            Derive swiftly and without any difficulty number bonds to 100            Add friendly large numbers using knowledge of place value and number facts            Use expanded column addition to add pairs of 4- and 5-digit numbers</p>
	<b>Subtraction</b>	<p>Subtract numbers with two significant digits only, using mental strategies. (E.g. <math>6.2 - 4.5</math> or <math>72,000 - 47,000</math>)            Subtract one or two-digit multiples of 100, 1000, 10,000 and 100,000. (E.g. <math>8000 - 3000</math> or <math>600,000 - 200,000</math>)            Subtract one or two digit near multiples of 100, 1000, 10,000 and 100,000 from other numbers. (E.g. <math>82,472 - 30,004</math>)            Subtract decimal numbers which are near multiples of 1 or 10, including money. (E.g. <math>6.34 - 1.99</math> or <math>£34.59 - £19.95</math>)            Use counting up subtraction, with knowledge of number bonds to 10/100 or £1, as a strategy to perform mental subtraction. (E.g. <math>£10 - £3.45</math> or <math>1000 - 782</math>)            Recognise fraction complements to 1 and to the next whole number. (E.g. <math>1\frac{2}{5} + \frac{3}{5} = 2</math>) <math>4 - 5</math></p>	<p>Use compact or expanded column subtraction to subtract numbers with up to 5 digits.            Use complementary addition for subtractions where the larger number is a multiple or near multiple of 1000.            Use complementary addition for subtractions of decimals with up to two places incl. amounts of money            Begin to subtract related fractions using equivalences. (E.g. <math>\frac{1}{2} - \frac{1}{6} = \frac{2}{6}</math>)            Choose the most efficient method in any given situation</p>	<p>Derive swiftly and without difficulty number bonds to 100            Use counting up with confidence to solve most subtractions, including finding complements to multiples of 1000. (E.g. <math>3000 - 2387</math> is done by</p> 

<b>Multiplication</b>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math>.          Multiply whole numbers and one-and two-place decimals by 10, 100, 1000, 10,000          Use knowledge of factors and multiples in multiplication. (E.g. <math>43 \times 6</math> is double <math>43 \times 3</math>, and <math>28 \times 50</math> is <math>\frac{1}{2}</math> of <math>28 \times 100 = 1400</math>)          Use knowledge of place value and rounding in mental multiplication. (E.g. <math>67 \times 199</math> as <math>67 \times 200 - 67</math>)          Use doubling and halving as a strategy in mental multiplication. (E.g. <math>58 \times 5 =</math> half of <math>58 \times 10</math>, and <math>34 \times 4</math> is 34 doubled twice)          Partition 2-digit numbers, including decimals, to multiply by a single-digit number mentally. (E.g. <math>6 \times 27</math> as <math>6 \times 20</math> (120) plus <math>6 \times 7</math> (42) making 162 or <math>6.3 \times 7</math> as <math>6 \times 7</math> plus <math>0.3 \times 7</math>)          Double amounts of money by partitioning. (E.g. £37.45 doubled = £37 doubled (£74) plus 45p doubled (90p) £74.90)</p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits          Use long multiplication to multiply 3-digit and 4-digit number by a number between 11 and 20          Choose the most efficient method in any given situation          Find simple percentages of amounts (e.g. 10%, 5%, 20%, 155 and 50%)          Begin to multiply fractions and mixed numbers by whole numbers <math>\leq 10</math>, e.g. <math>4 \times \frac{2}{3} = \frac{8}{3} = 2\frac{2}{3}</math>.</p>	<p>Know multiplication tables to <math>11 \times 11</math>          Multiply whole numbers and one-place decimals by 10, 100 and 1000          Use knowledge of factors as aids to mental multiplication. (E.g. <math>13 \times 6 =</math> double <math>13 \times 3</math> and <math>23 \times 5</math> is <math>\frac{1}{2}</math> of <math>23 \times 10</math>)          Use grid method to multiply numbers with up to 4-digits by one-digit numbers.          Use grid method to multiply 2-digit by 2-digit numbers.</p>
<b>Division</b>	<p>Know by heart all the division facts up to <math>144 \div 12</math>.          Divide whole numbers by 10, 100, 1000, 10,000 to give whole number answers or answers with 1, 2 or 3 decimal places          Use doubling and halving as mental division strategies. (E.g. <math>34 \div 5</math> is <math>(34 \div 10) \times 2</math>)          Use knowledge of multiples and factors, also tests for divisibility, in mental division. (E.g. <math>246 \div 6</math> is <math>123 \div 3</math> and we know that 525 divides by 25 and by 3)          Halve amounts of money by partitioning. (E.g. Half of £75.40 = half of £75 (37.50) plus half of 40p (20p) which is £37.70)          Divide larger numbers mentally by subtracting the <math>10^{\text{th}}</math> or <math>100^{\text{th}}</math> multiple as appropriate. (E.g. <math>96 \div 6</math> is <math>10 + 6</math>, as <math>10 \times 6 = 60</math> and <math>6 \times 6 = 36</math>; <math>312 \div 3</math> is <math>100 + 4</math> as <math>100 \times 3 = 300</math> and <math>4 \times 3 = 12</math>)          Reduce fractions to their simplest form.</p>	<p>Use short division to divide a number with up to 4 digits by a number <math>\leq 12</math>.          Give remainders as whole numbers or as fractions.          Find non-unit fractions of large amounts.          Turn improper fractions into mixed numbers and vice versa.          Choose the most efficient method in any given situation</p>	<p>Know by heart division facts up to <math>121 \div 11</math>          Divide whole numbers by 10, 100 or 1000 to give answers with up to one decimal place.          Use doubling and halving as mental division strategies          Use efficient chunking to divide numbers <math>\leq 1000</math> by 1-digit numbers.          Find unit fractions of 2 and 3-digit numbers</p>

<b>Year 6</b>	<b>Addition</b>	<p>Know by heart number bonds to 100 and use these to derive related facts. (E.g. <math>3.46 + 0.54 = 4</math>)</p> <p>Derive quickly and without difficulty, number bonds to 1000</p> <p>Add small and large whole numbers where the use of place value or number facts makes the calculation do-able 'in our heads'. (E.g. <math>34,000 + 8000</math>.)</p> <p>Add multiples of powers of ten and near multiples of the same. (E.g. <math>6345 + 199</math>.)</p> <p>Add negative numbers in a context such as temperature where the numbers make sense.</p> <p>Add two 1-place decimal numbers or two 2-place decimal numbers less than 1 (E.g. <math>4.5 + 6.3</math> or <math>0.74 + 0.33</math>)</p> <p>Add positive numbers to negative numbers, e.g. calculate a rise in temperature, or continue a sequence beginning with a negative number</p>	<p>Use column addition to add numbers with up to 5 digits.</p> <p>Use column addition to add decimal numbers with up to 3-digits</p> <p>Add mixed numbers and fractions with different denominators.</p>	<p>Derive swiftly and without difficulty, number bonds to 100</p> <p>Use place value and number facts to add friendly large or decimal numbers, e.g. <math>3.4 + 6.6</math> or <math>26,000 + 5,400</math></p> <p>Use column addition to add numbers with up to 4-digits.</p> <p>Use column addition to add pairs of two-place decimal numbers.</p>
	<b>Subtraction</b>	<p>Use number bonds to 100 to perform mental subtraction of any pair of integers by complementary addition. (E.g. <math>1000 - 654</math> as <math>46 + 300</math> in our heads)</p> <p>Use number bonds to 1 and 10 to perform mental subtraction of any pair of one-place or two-place decimal numbers using complementary addition and including money. (E.g. <math>10 - 3.65</math> as <math>0.35 + 6</math>, <math>£50 - £34.29</math> as <math>71p + £15</math>)</p> <p>Use number facts and place value to perform mental subtraction of large numbers or decimal numbers with up to two places. (E.g. <math>467,900 - 3,005</math> or <math>4.63 - 1.02</math>)</p> <p>Subtract multiples of powers of ten and near multiples of the same.</p> <p>Subtract negative numbers in a context such as temperature where the numbers make sense.</p>	<p>Use column subtraction to subtract numbers with up to 6 digits.</p> <p>Use complementary addition for subtractions where the larger number is a multiple or near multiple of 1000 or 10,000.</p> <p>Use complementary addition for subtractions of decimal numbers with up to three places including money.</p> <p>Subtract mixed numbers and fractions with different denominators.</p>	<p>Use number bonds to 100 to perform mental subtraction of numbers up to 1000 by complementary addition. (E.g. <math>1000 - 654</math> as <math>46 + 300</math> in our heads.)</p> <p>Use complementary addition for subtraction of integers up to 10,000. E.g. <math>2504 - 1878</math> as</p> <div style="text-align: center;"> <p><math>1878 \quad 1880 \quad 1900 \quad 2000 \quad 2504</math></p> <p><math>+2 \quad +20 \quad +100 \quad +504 \quad = 626</math></p> </div> <p>Use complementary addition for subtractions of one-place decimal numbers and amounts of money. (E.g. <math>£7.30 - £3.55</math> as</p> <div style="text-align: center;"> <p><math>£3.55 \quad £3.60 \quad £4.00 \quad £7.30</math></p> <p><math>+5p \quad +40p \quad +£3.30 \quad = £3.75</math></p> </div>

	<b>Multiplication</b>	<p>Know by heart all the multiplication facts up to 12 x 12.          Multiply whole numbers and decimals with up to three places by 10, 100 or 1000, e.g. <math>234 \times 1000 = 234,000</math> and <math>0.23 \times 1000 = 230</math>)          Identify common factors, common multiples and prime numbers and use factors in mental multiplication. (E.g. <math>326 \times 6</math> is <math>652 \times 3</math> which is 1956)          Use place value and number facts in mental multiplication. (E.g. <math>40,000 \times 6 = 24,000</math> and <math>0.03 \times 6 = 0.18</math>)          Use doubling and halving as mental multiplication strategies, including to multiply by 2, 4, 8, 5, 20, 50 and 25 (E.g. <math>28 \times 25</math> is <math>\frac{1}{4}</math> of <math>28 \times 100 = 700</math>)          Use rounding in mental multiplication. (<math>34 \times 19</math> as <math>(20 \times 34) - 34</math>)          Multiply one and two-place decimals by numbers up to and including 10 using place value and partitioning. (E.g. <math>3.6 \times 4</math> is <math>12 + 2.4</math> or <math>2.53 \times 3</math> is <math>6 + 1.5 + 0.09</math>)          Double decimal numbers with up to 2 places using partitioning e.g. <i>36.73 doubled is double 36 (72) plus double 0.73 (1.46)</i></p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits          Use long multiplication to multiply a 2-digit by a number with up to 4 digits          Use short multiplication to multiply a 1-digit number by a number with one or two decimal places, including amounts of money.          Multiply fractions and mixed numbers by whole numbers.          Multiply fractions by proper fractions.          Use percentages for comparison and calculate simple percentages.</p>	<p>Know by heart all the multiplication facts up to 12 x 12.          Multiply whole numbers and one-and two-place decimals by 10, 100 and 1000.          Use an efficient written method to multiply a one-digit or a teens number by a number with up to 4-digits by partitioning (grid method).          Multiply a one-place decimal number up to 10 by a number <math>\leq 100</math> using grid method.</p>
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<b>Division</b>	<p>Know by heart all the division facts up to <math>144 \div 12</math>.          Divide whole numbers by powers of 10 to give whole number answers or answers with up to three decimal places.          Identify common factors, common multiples and prime numbers and use factors in mental division. (E.g. <math>438 \div 6</math> is <math>219 \div 3</math> which is 73)          Use tests for divisibility to aid mental calculation.          Use doubling and halving as mental division strategies, e.g. to divide by 2, 4, 8, 5, 20 and 25. (E.g. <math>628 \div 8</math> is halved three times: 314, 157, 78.5)          Divide one and two place decimals by numbers up to and including 10 using place value. (E.g. <math>2.4 \div 6 = 0.4</math> or <math>0.65 \div 5 = 0.13</math>, <math>\pounds 6.33 \div 3 = \pounds 2.11</math>)          Halve decimal numbers with up to 2 places using partitioning  <i>e.g. Half of 36.86 is half of 36 (18) plus half of 0.86 (0.43)</i>          Know and use equivalence between simple fractions, decimals and percentages, including in different contexts.          Recognise a given ratio and reduce a given ratio to its lowest terms.</p>	<p>Use short division to divide a number with up to 4 digits by a 1-digit or a 2-digit number          Use long division to divide 3-digit and 4-digit numbers by 'friendly' 2-digit numbers.          Give remainders as whole numbers or as fractions or as decimals          Divide a one-place or a two-place decimal number by a number <math>\leq 12</math> using multiples of the divisors.          Divide proper fractions by whole numbers.</p>	<p>Know by heart all the division facts up to <math>144 \div 12</math>.          Divide whole numbers by 10, 100, 1000 to give whole number answers or answers with up to two decimal places.          Use efficient chunking involving subtracting powers of 10 times the divisor to divide any number of up to 1000 by a number <math>\leq 12</math>. (E.g. <math>836 \div 11</math> as <math>836 - 770</math> (<math>70 \times 11</math>) leaving 66 which is <math>6 \times 11</math>. So that we have <math>70 + 6 = 76</math> as the answer).          Divide a one-place decimal by a number <math>\leq 10</math> using place value and knowledge of division facts.</p>
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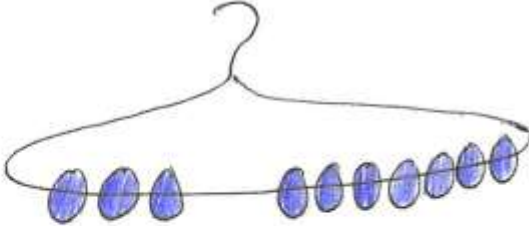
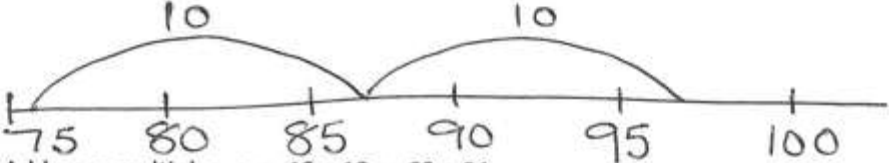
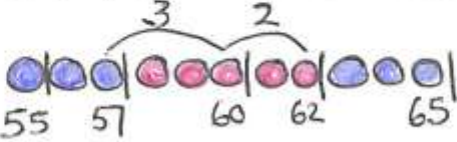
Signed:..... Chair of Governors


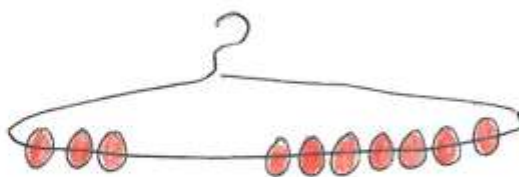
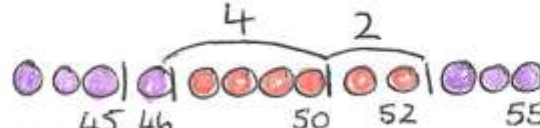
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Review: December 2018

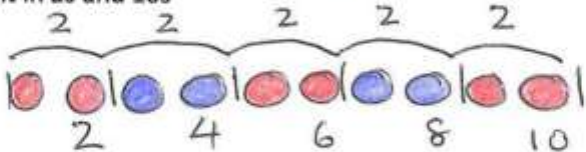

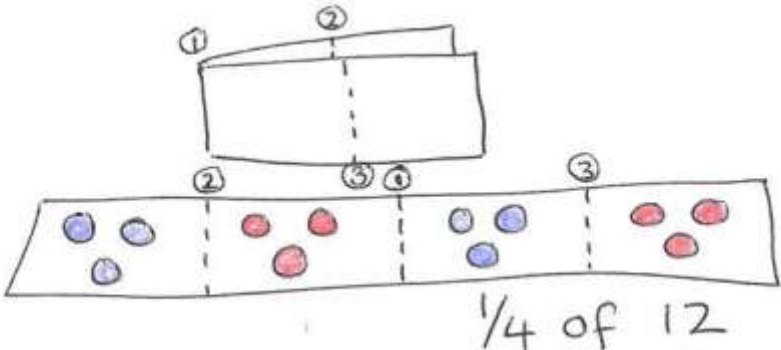
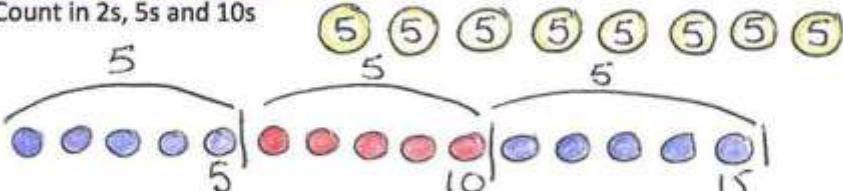

Appendix A

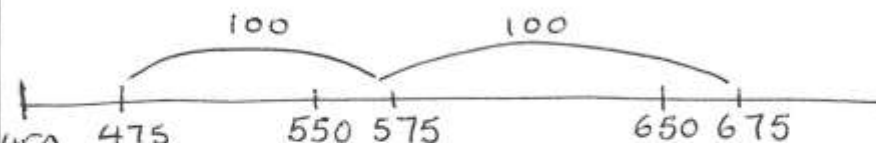


Mental And Written Calculation Examples


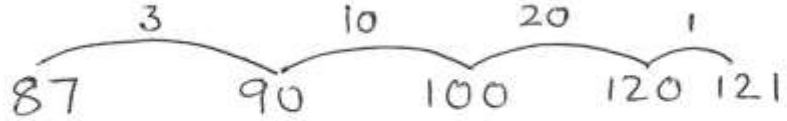



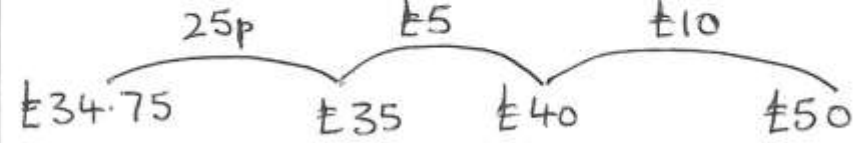
	Year 1	Year 2																																								
Mental Addition	<p><b>Using Place value</b> Count in ones / Counting in tens, e.g. knowing <math>45 + 1</math> or <math>45 + 10</math> without counting on in ones</p> <p><math>23 + 10</math></p> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td></td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td></td></tr> <tr><td>41</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> </table> <p><b>Counting on</b> Count on in ones, e.g. <math>11 + 2 = 7 + 4 =</math></p> <p>Count on in tens, e.g. <math>45 + 20</math> as 45, 55, 65</p> <p><b>Using number facts</b> 'Story' of 4, 5, 6, 7, 8 and 9, e.g. <math>7 = 7 + 0</math> or <math>6 + 1</math> or <math>5 + 2</math> or <math>4 + 3</math> Number bonds to 10, e.g. <math>5 + 5, 6 + 4, 7 + 3, 8 + 2, 9 + 1, 10 + 0</math></p>   <p>Patterns using known facts, e.g. <math>4 + 3 = 7</math> so we know <math>24 + 3, 44 + 3, 74 + 3,</math> etc.</p>	1	2	3	4	5	6	7	8	11	12	13	14	15	16	17	18	21	22	23	24	25	26	27		31	32	33	34	35	36	37		41								<p><b>Using Place value</b> Know 1 more or 10 more than any number, e.g. 1 more than 67 or 10 more than 85</p> <p>Partitioning, e.g. <math>55 + 37</math> as <math>50 + 30</math> and <math>5 + 7</math> finally combining the two totals: <math>80 + 12</math></p> <p><math>\boxed{50} \triangleright + \boxed{30} \triangleright = 80</math> <math>\boxed{5} \triangleright + \boxed{7} \triangleright = 12</math> <math>80 + 12 = 92</math></p> <p><b>Counting on</b> Add ten and multiples of ten, e.g. <math>76 + 20</math> as 76, 86, 96 or in one hop <math>76 + 20</math> Add two 2-digit numbers by counting on in tens then in ones, e.g. <math>55 + 37</math> as 55 add 30 (85) add 7 (92)</p>  <p>Add near multiples, e.g. <math>46 + 19</math> or <math>63 + 21</math></p> <p><b>Using number facts</b> Know pairs of numbers which make the numbers up to and including 10, e.g. <math>8 = 4 + 4, 3 + 5, 2 + 6, 1 + 7</math> and <math>10 = 5 + 5, 4 + 6, 3 + 7, 2 + 8, 1 + 9, 0 + 10</math> Patterns of known facts, e.g. <math>6 + 3 = 9</math>, so we know <math>36 + 3 = 39, 66 + 3 = 69, 53 + 6 = 59</math> Bridging ten, e.g. <math>57 + 5</math> as 57 add 3 then add 2 more</p>  <p>Adding three or more single-digit numbers, spotting bonds to 10 or doubles, e.g. <math>6 + 7 + 4 + 2</math> as <math>10 + 7 + 2</math></p>
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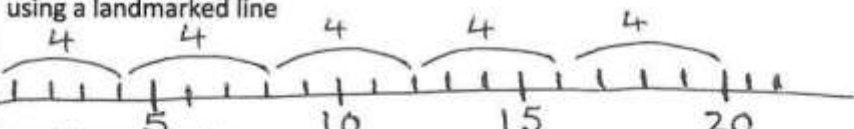
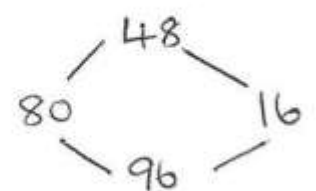
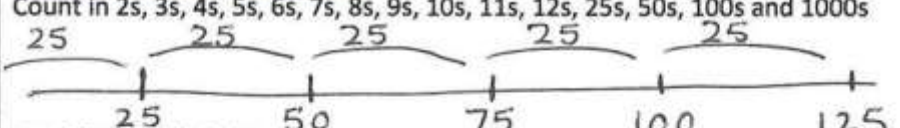
	Year 1	Year 2																								
<b>Mental Subtraction</b>	<p><b>Using Place value</b> Count back in ones / Count back in tens, e.g. knowing <math>53 - 1</math> or <math>53 - 10</math> without counting back in ones</p> <p><math>33 - 10</math></p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td></td></tr> </table>	1	2	3	4	5	6	11	12	13	14	15	16	21	22	23	24	25	26	31	32	33	34	35		<p><b>Using Place value</b> Know 1 less or 10 less than any number, e.g. 1 less than 74 or 10 less than 82 Partitioning, e.g. <math>55 - 32</math> as <math>50 - 30</math> and <math>5 - 2</math> combining the answers: <math>20 + 3</math></p> <p><math>50 - 30 = 20</math> <math>5 - 2 = 3</math> <math>\underline{23}</math></p>
	1	2	3	4	5	6																				
	11	12	13	14	15	16																				
	21	22	23	24	25	26																				
31	32	33	34	35																						
<p><b>Taking away</b> Count back in ones, e.g. <math>11 - 3 =</math>    <math>15 - 4 =</math></p> <p>Count back in tens, e.g. <math>53 - 20</math> as 53, 43, 33</p> 	<p><b>Taking away</b> Subtract ten and multiples of ten, e.g. <math>76 - 20</math> as 76, 66, 56 or in one hop <math>76 - 20 = 56</math> Subtract two 2-digit numbers by counting back in tens then in ones, e.g. <math>67 - 33</math> as 67 subtract 30 (37) then count back 3 (34) Subtracting near multiples, e.g. <math>74 - 21</math> or <math>57 - 19</math></p>																									
<p><b>Using number facts</b> 'Story' of 4, 5, 6, 7, 8 and 9, e.g. <math>7 - 1 = 6</math>, <math>7 - 2 = 5</math>, <math>7 - 3 = 4</math>, etc. Number bonds to 10, e.g. <math>10 - 1 = 9</math>, <math>10 - 2 = 8</math>, <math>10 - 3 = 7</math>, etc.</p> 	<p><b>Using number facts</b> Know pairs of numbers which make the numbers up to and including 10, e.g. <math>10 - 6 = 4</math>, <math>8 - 3 = 5</math>, <math>5 - 2 = 3</math>, etc. Patterns of known facts, e.g. <math>9 - 6 = 3</math>, so we know <math>39 - 6 = 33</math>, <math>69 - 6 = 63</math>, <math>89 - 6 = 83</math> Bridge ten, e.g. <math>52 - 6</math> as 52 subtract 2 then subtract 4 more</p> 																									
<p>Patterns using known facts, e.g. <math>7 - 3 = 4</math> so we know <math>27 - 3 =</math>, <math>47 - 3 =</math>, <math>77 - 4 =</math>, etc.</p>	<p><b>Counting up</b> Find a difference between two numbers on a line, e.g. <math>51 - 47</math></p>																									



	Year 1	Year 2
Mental Division	<p data-bbox="230 204 656 236"><b>Counting in steps ('Clever' counting)</b></p> <p data-bbox="230 239 459 268">Count in 2s and 10s</p>  <p data-bbox="230 446 481 475"><b>Doubling and halving</b></p> <p data-bbox="230 478 1108 542">Find half of even numbers up to 12 including realising that it is hard to halve an odd number</p>  <p data-bbox="230 758 347 786"><b>Grouping</b></p> <p data-bbox="230 790 1041 853">Begin to use visual and concrete arrays and 'sets of' objects to find the answers to 'how many towers of 3 can I make with 12 cubes?'</p> <p data-bbox="230 893 324 922"><b>Sharing</b></p> <p data-bbox="230 925 1086 989">Begin to find half of a quantity using sharing, e.g. half of 16 cubes by giving one each repeatedly to two children</p> 	<p data-bbox="1149 204 1574 236"><b>Counting in steps ('Clever' counting)</b></p> <p data-bbox="1149 239 1422 268">Count in 2s, 5s and 10s</p>  <p data-bbox="1149 446 1400 475"><b>Doubling and halving</b></p> <p data-bbox="1149 478 2027 582">Find half of numbers up to 40, including realising that half of an odd number gives a remainder of 1 or an answer containing a 1/2 Begin to know half of multiples of 10 to 100, e.g. half of 70 is 35</p> <p data-bbox="1149 622 1265 651"><b>Grouping</b></p> <p data-bbox="1149 654 2016 758">Relate division to multiplication by using arrays or towers of cubes to find answers to division, e.g. how many towers of five cubes can I make from 20 cubes as <math>\square \times 5 = 20</math> and also as <math>20 \div 5 = ?</math></p>  <p data-bbox="1149 861 2016 925">Relate to division to 'clever' counting and hence to multiplication, e.g. how many 5s do I count to get to 20?</p> <p data-bbox="1149 965 1243 994"><b>Sharing</b></p> <p data-bbox="1149 997 2049 1061">Begin to find half or a quarter of a quantity using sharing, e.g. 1/4 of 16 cubes by sorting the cubes into four piles</p> <p data-bbox="1149 1069 1512 1098">Find 1/4, 1/2, 3/4 of small quantities</p> <p data-bbox="1149 1244 1377 1273"><b>Using number facts</b></p> <p data-bbox="1149 1276 1556 1305">Know halves of even numbers to 24</p> <p data-bbox="1149 1308 1534 1337">Know 2x, 5x and 10x division facts</p> <p data-bbox="1149 1340 1500 1369">Begin to know 3x division facts</p>

	Year 3	Year 4																																														
Mental Addition	<p><b>Using Place value</b> Count in hundreds, e.g. knowing <math>475 + 200</math> as 475, 575, 675</p>  <p>Add multiples of 10, 100 and £1, e.g. <math>746 + 200</math> or <math>746 + 40</math> or <math>£6.34 + £5</math> as <math>£6 + £5</math> and <math>34p</math> Partitioning, e.g. <math>68 + 74</math> as <math>60 + 70</math> and <math>8 + 4</math> and combine the totals: <math>130 + 12 = 142</math> or <math>£8.50 + £3.70</math> as <math>£8 + £3</math> and <math>50p + 70p</math> and combine: <math>£11 + £1.20</math></p> <p><b>Counting on</b> Add two 2-digit numbers by adding the multiple of ten then the ones, e.g. <math>67 + 55</math> as 67 add 50 (117) add 5 (122) Add near multiples of 10 and 100, e.g. <math>67 + 39</math> or <math>364 + 199</math> Count on from 3-digit nos, e.g. <math>247 + 34</math> as <math>247 + 30</math> (277) then <math>277 + 4 = 281</math></p> <p><b>Using number facts</b> Number bonds to 100, e.g. <math>35 + 65</math>, <math>46 + 54</math>, <math>73 + 27</math>, etc. Add to next ten and next hundred, e.g. <math>176 + 4 = 180</math>, <math>435 + 65 = 500</math>, etc.</p>	<p><b>Using Place value</b> Count in thousands, e.g. knowing <math>746 + 200</math> as 746, 946, 1146 Partitioning, e.g. <math>746 + 203</math> as <math>700 + 200</math> and <math>46 + 3</math> or <math>134 + 707</math> as <math>130 + 700</math> and <math>4 + 7</math></p> <p><b>Counting on</b> Add two 2-digit numbers by adding the multiple of ten then the ones, e.g. <math>67 + 55</math> as 67 add 50 (117) add 5 (122) Add near multiples of 10, 100 and 1000, e.g. <math>467 + 199</math> or <math>3462 + 2999</math></p>  <p>Count on to add 3-digit numbers and money, e.g. <math>463 + 124</math> as <math>463 + 100</math> (563) <math>+20</math> (583) <math>+4 = 587</math> or <math>£4.67 + £5.30</math> as <math>£9.67</math> add <math>30p</math></p> <p><b>Using number facts</b> Number bonds to 100 and to next multiple of 100, e.g. <math>463 + 37</math>, <math>1353 + 47</math></p>  <p>Number bonds to £1 and to the next whole pound, e.g. <math>£3.45 + 55p</math> Add to next whole number, e.g. <math>4.6 + 0.4</math>, <math>7.2 + 0.8</math></p>																																														
	<p><b>Written Addition</b></p> <p>Build on partitioning to develop expanded column addition with two 3-digit numbers</p> <table border="1" data-bbox="716 941 963 1085"> <tr><td>400</td><td>60</td><td>6</td></tr> <tr><td>+300</td><td>50</td><td>8</td></tr> <tr><td>700</td><td>110</td><td>14</td></tr> </table> <p>Expanded column addition with 'carrying'</p> <table border="1" data-bbox="604 1117 851 1292"> <tr><td>400</td><td>60</td><td>6</td></tr> <tr><td>+300</td><td>50</td><td>8</td></tr> <tr><td>100</td><td>10</td><td></td></tr> <tr><td>800</td><td>20</td><td>4</td></tr> </table> <table border="1" data-bbox="918 1117 1075 1340"> <tr><td>347</td></tr> <tr><td>286</td></tr> <tr><td>495</td></tr> <tr><td>21</td></tr> <tr><td>1128</td></tr> </table> <p>Compact column addition with two or more 3-digit numbers or towers of 2-digit numbers</p> <p>Compact column addition with 3-digit and 4-digit numbers</p> <p>Recognise fractions which add to 1, e.g. <math>\frac{1}{4} + \frac{3}{4}</math> or <math>\frac{2}{5} + \frac{3}{5}</math></p>	400	60	6	+300	50	8	700	110	14	400	60	6	+300	50	8	100	10		800	20	4	347	286	495	21	1128	<p>Build on expanded column addition to develop compact column addition with larger numbers.</p> <table border="1" data-bbox="1590 957 1926 1133"> <tr><td>1000</td><td>400</td><td>60</td><td>6</td></tr> <tr><td>+4000</td><td>800</td><td>60</td><td>8</td></tr> <tr><td>1000</td><td>100</td><td>10</td><td></td></tr> <tr><td>6000</td><td>300</td><td>30</td><td>4</td></tr> </table> <p>Compact column addition with larger numbers.</p> <table border="1" data-bbox="1612 1149 1769 1388"> <tr><td>5347</td></tr> <tr><td>2286</td></tr> <tr><td>+1495</td></tr> <tr><td>121</td></tr> <tr><td>9128</td></tr> </table> <p>Use expanded and compact column addition to add amounts of money.</p> <p>Add like fractions, e.g. <math>\frac{3}{8} + \frac{1}{8} + \frac{1}{8}</math></p>	1000	400	60	6	+4000	800	60	8	1000	100	10		6000	300	30	4	5347	2286	+1495	121
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	Year 3	Year 4			
Mental Subtraction	<p><b>Taking away</b> Use place value to subtract, e.g. <math>348 - 300</math> or <math>348 - 40</math> or <math>348 - 8</math> Taking away multiples of 10, 100 and £1, e.g. <math>476 - 40 = 436</math>, <math>476 - 300 = 176</math>, <math>£4.76 - £2 = £2.76</math> Partitioning, e.g. <math>68 - 42</math> as <math>60 - 40</math> and <math>8 - 2</math> or <math>£6.84 - £2.40</math> as <math>£6 - £2</math> and <math>80p - 40p</math> Count back in hundreds, tens then ones, e.g. <math>763 - 121</math> as <math>763 - 100</math> (663) then subtract 20 (643) then subtract 1 (642) Subtract near multiples, e.g. <math>648 - 199</math> or <math>86 - 39</math></p> <p><b>Counting up</b>  <math>348 - 40 = 308</math> Find a difference between two numbers by counting up from the smaller to the larger, e.g. <math>121 - 87</math></p>  <p><b>Using number facts</b> Number bonds to 100, e.g. <math>100 - 35 = 65</math>, <math>100 - 48 = 52</math>, etc.</p>	<p><b>Taking away</b> Use place value to subtract, e.g. <math>4748 - 4000</math> or <math>4748 - 8</math>, etc. Take away multiples of 10, 100, 1000, £1, 10p or 0.1, e.g. <math>8392 - 50</math> or <math>6723 - 3000</math> or <math>£3.74 - 30p</math> or <math>5.6 - 0.2</math> Partitioning, e.g. <math>£5.87 - £3.04</math> as <math>£5 - £3</math> and <math>7p - 4p</math> or <math>7493 - 2020</math> as <math>7000 - 2000</math> and <math>90 - 20</math> Count back, e.g. <math>6482 - 1301</math> as <math>6482 - 1000</math> then <math>- 300</math> then <math>- 1</math> (5181) Subtract near multiples, e.g. <math>3522 - 1999</math> or <math>£34.86 - £19.99</math></p> <p><b>Counting up</b> Find a difference between two numbers by counting up from the smaller to the larger, e.g. <math>506 - 387</math></p>  <p><b>Using number facts</b> Number bonds to 10, 100 and derived facts, e.g. <math>100 - 76 = 24</math>, <math>1.0 - 0.6 = 0.4</math> Number bonds to £1 and £10, e.g. <math>£1.00 - 86p = 14p</math> or <math>£10 - £3.40 = £6.60</math></p>			
	Written Subtraction	<p>Develop counting up subtraction</p>  <p>Use counting up subtraction to find change from £1 and £10</p>  <p>Recognise complements of any fraction to 1, e.g. <math>1 - \frac{1}{4} = \frac{3}{4}</math> or <math>1 - \frac{2}{3} = \frac{1}{3}</math></p>	<p>Expanded column subtraction      Begin to use compact column subtraction</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: right; padding-right: 20px;"> <math display="block">\begin{array}{r} 600 \\ - 300 \\ \hline 300 \end{array}</math> </td> <td style="text-align: right; padding-right: 20px;"> <math display="block">\begin{array}{r} 110 \\ - 50 \\ \hline 60 \end{array}</math> </td> <td style="text-align: right;"> <math display="block">\begin{array}{r} 16 \\ - 8 \\ \hline 8 \end{array}</math> </td> </tr> </table> <p>Use counting up subtraction to find change from £10, £20, £50 and £100</p>  <p>Subtract like fractions, e.g. <math>\frac{3}{8} - \frac{1}{8} = \frac{2}{8}</math></p>	$\begin{array}{r} 600 \\ - 300 \\ \hline 300 \end{array}$	$\begin{array}{r} 110 \\ - 50 \\ \hline 60 \end{array}$
$\begin{array}{r} 600 \\ - 300 \\ \hline 300 \end{array}$	$\begin{array}{r} 110 \\ - 50 \\ \hline 60 \end{array}$	$\begin{array}{r} 16 \\ - 8 \\ \hline 8 \end{array}$			

Mental Division	<p><b>Counting in steps ('Clever' counting)</b> Count in 2s, 3s, 4s, 5s, 8s and 10s by colouring numbers on the 1-100 grid or using a landmarked line</p>  <p><b>Doubling and halving</b> Find half of even numbers to 100 using partitioning. Use halving as a strategy in dividing by 2. E.g. <math>36 \div 2</math> is half of 36</p>  <p><b>Grouping</b> Recognise that division is not commutative, e.g. <math>16 \div 8</math> does not equal <math>8 \div 16</math> Relate division to multiplications 'with holes in', e.g. <math>\square \times 5 = 30</math> is the same calculation as <math>30 \div 5 = ?</math> thus we can count in 5s to find the answer Divide multiples of 10 by single digit numbers, e.g. <math>240 \div 8 = 30</math></p> <p><b>Using number facts</b> Know halves of even numbers to 40 Know halves of multiples of 10 to 200, e.g. half of 170 is 85 Know 2x, 3x, 4x, 5x, 8x, 10x division facts Use division facts to find unit and simple non-unit fractions of amounts within the times tables, e.g. <math>\frac{3}{4}</math> of 48 is <math>3 \times (48 \div 4)</math></p>	<p><b>Counting in steps – sequences</b> Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s</p>  <p><b>Doubling and halving</b> Find halves of even numbers to 200 and beyond using partitioning. Begin to half amounts of money. E.g. £9 halved is £4.50 Use halving as a strategy in dividing by 2, 4 and 8, e.g. <math>164 \div 4</math> is half of 164 (82) halved again (41)</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto; margin-right: auto;"> <p><math>45 \div 3 = \square</math></p> <p><math>\square \times 3 = 45</math></p> <p><math>10 \times 3 = 30</math></p> <p style="padding-left: 100px;">15</p> <p><math>5 \times 3 = 15</math></p> </div> <p><b>Grouping</b> Use multiples of 10 times the divisor to divide by number <math>\leq 9</math> above the tables facts, e.g. <math>45 \div 3</math> Divide multiples of 100 by single digit numbers using division facts, e.g. <math>3200 \div 8 = 400</math></p> <p><b>Using number facts</b> Know times tables up to <math>12 \times 12</math> and all related division facts Use division facts to find unit and non-unit fractions of amounts within the times tables, e.g. <math>\frac{7}{8}</math> of 56 is <math>7 \times (56 \div 8)</math></p>
	Written Division	

	Year 5	Year 6																																																
<b>Mental Addition</b>	<p><b>Using Place value</b> Count in 0.1s, 0.01s, e.g. knowing what 0.1 more than 0.51 is</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>100s</td> <td>10s</td> <td>1s</td> <td>0.1s</td> <td>0.01s</td> <td>0.001s</td> </tr> <tr> <td></td> <td></td> <td></td> <td>.5</td> <td>1</td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>.1</td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>.6</td> <td>1</td> <td></td> </tr> </table> <p>Partitioning, e.g. <math>2.4 + 5.8</math> as <math>2 + 5</math> and <math>0.4 + 0.8</math> and combine the totals: <math>7 + 1.2 = 8.2</math></p> $  \begin{array}{r}  2.4 + 5.8 \\  \hline  7 + 1.2 = 8.2  \end{array}  $ <p><b>Counting on</b> Add two decimal numbers by adding the ones then the tenths/hundredths, e.g. <math>5.72 + 3.05</math> as <math>5.72</math> add <math>3</math> (<math>8.72</math>) then add <math>0.05</math> (<math>8.77</math>) Add near multiples of 1, e.g. <math>6.34 + 0.99</math> or <math>5.63 + 0.9</math> Count on from large numbers, e.g. <math>6834 + 3005</math> as <math>9834 + 5</math></p> <p><b>Using number facts</b> Number bonds to 1 and to the next whole number, e.g. <math>0.4 + 0.6</math> or <math>5.7 + 0.3</math></p> <p>Add to next ten from a decimal number, e.g. <math>7.8 + 2.2 = 10</math></p>	100s	10s	1s	0.1s	0.01s	0.001s				.5	1					.1						.6	1		<p><b>Using Place value</b> Count in 0.1s, 0.01s, 0.001s, e.g. knowing what 0.001 more than 6.725 is</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>100s</td> <td>10s</td> <td>1s</td> <td>0.1s</td> <td>0.01s</td> <td>0.001s</td> </tr> <tr> <td></td> <td></td> <td>6</td> <td>7</td> <td>2</td> <td>5</td> </tr> <tr> <td></td> <td></td> <td>,</td> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td></td> <td></td> <td>6</td> <td>7</td> <td>2</td> <td>6</td> </tr> </table> <p><b>Counting on</b> Add two decimal numbers by adding the ones then the tenths/hundredths or thousandths, e.g. <math>6.314 + 3.006</math> as <math>6.314</math> add <math>3</math> (<math>9.314</math>) then add <math>0.006</math> (<math>9.32</math>) Add near multiples of 1, e.g. <math>6.345 + 0.999</math> or <math>5.673 + 0.9</math> Count on from large numbers, e.g. <math>16,375 + 12,003</math></p> <p><b>Using number facts</b> Number bonds to 1 and to next multiple of 1, e.g. <math>0.63 + 0.37</math> or <math>2.355 + 0.645</math> Add to next ten, e.g. <math>4.62 + 0.38</math></p> $  \begin{array}{c}  \text{0.38} \\  \text{-----} \\    \quad   \quad   \quad   \\  4 \quad 4.5 \quad 4.62 \quad 5  \end{array}  $	100s	10s	1s	0.1s	0.01s	0.001s			6	7	2	5			,	0	0	1			6	7	2	6
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	Year 5	Year 6	
<b>Written Addition</b>	Expanded column addition for money leading to compact column addition for adding several amounts of money	$  \begin{array}{r}  \text{£}14 \quad 60\text{p} \quad 4\text{p} \\  \text{£}28 \quad 70\text{p} \quad 8\text{p} \\  + \text{£}12 \quad 20\text{p} \quad 6\text{p} \\  \hline  \text{£}1 \quad 10\text{p} \\  \hline  \text{£}55 \quad 60\text{p} \quad 8\text{p}  \end{array}  $	Compact column addition for adding several large numbers and decimal numbers with up to two places
	Compact column addition to add Pairs of 5-digit numbers		$  \begin{array}{r}  \text{£}14.64 \\  + \text{£}28.78 \\  \hline  \text{£}12.26 \\  \hline  \text{£}55.68  \end{array}  $
	Continue to use column addition to add towers of several larger numbers.	$  \begin{array}{r}  15.68 \\  + 27.86 \\  \hline  43.54  \end{array}  $	
	Use compact addition to add decimal numbers with up to two places		Compact column addition with money
	Adding fractions with related denominators, e.g. $\frac{1}{4} + \frac{3}{8} = \frac{5}{8}$		Add fractions with unlike denominators, e.g. $\frac{3}{4} + \frac{1}{3} = 1 \frac{1}{12}$ or $\frac{13}{12}$ $2 \frac{1}{4} + 1 \frac{1}{3} = 3 \frac{7}{12}$

	Year 5	Year 6
<b>Mental Subtraction</b>	<p><b>Taking away</b>            Use place value to subtract decimals, e.g. <math>4.58 - 0.08</math> or <math>6.26 - 0.2</math>, etc.            Take away multiples of powers of 10, e.g. <math>15,672 - 300</math> or <math>4.82 - 2</math> or <math>2.71 - 0.5</math> or <math>4.68 - 0.02</math>            Partition or count back, e.g. <math>3964 - 1051</math> or <math>5.72 - 2.01</math>            Subtract near multiples, e.g. <math>86,456 - 9999</math> or <math>3.58 - 1.99</math></p>	<p><b>Taking away</b>            Use place value to subtract decimals, e.g. <math>7.782 - 0.08</math> or <math>16.263 - 0.2</math>, etc.            Take away multiples of powers of 10, e.g. <math>132,956 - 400</math> or <math>686,109 - 40,000</math> or <math>7.823 - 0.5</math>            Partition or count back, e.g. <math>3964 - 1051</math> or <math>5.72 - 2.01</math>            Subtract near multiples, e.g. <math>360,078 - 99,998</math> or <math>12.831 - 0.99</math></p>
	<p><b>Counting up</b>            Find a difference between two numbers by counting up from the smaller to the larger, e.g. <math>2009 - 869</math></p> <p>Find change using shopkeepers' addition, e.g. buy toy for £6.89 using £10</p>	<p><b>Counting up</b>            Count up to subtract numbers from multiples of 10, 100, 1000, 10,000            Find a difference between two decimal numbers by counting up from the smaller to the larger, e.g. <math>1.2 - 0.87</math></p>
	<p><b>Using number facts</b>            Derived facts from number bonds to 10 and 100, e.g. <math>2 - 0.45</math> using <math>45 + 55 = 100</math> or <math>3.00 - 0.86</math> using <math>86 + 14 = 100</math></p>	<p><b>Using number facts</b>            Derived facts from number bonds to 10 and 100, e.g. <math>0.1 - 0.075</math> using <math>75 + 25 = 100</math> or <math>5 - 0.65</math> using <math>65 + 35 = 100</math></p>
	<p>Number bonds to £1, £10 and £100, e.g. <math>£4.00 - £3.86p = 14p</math> or <math>£100 - £66</math> using <math>66 + 34 = £100</math></p>	<p>Number bonds to £1, £10 and £100, e.g. <math>£7.00 - £4.37</math> or <math>£100 - £66.20</math> using <math>20p + 80p = £1</math> and <math>£67 + £33 = £100</math>.</p>

	Year 5	Year 6
Written Subtraction	<p>Compact column subtraction for numbers with up to 5 digits</p> $\begin{array}{r} 01513114 \\ \cancel{1}\cancel{8}\cancel{7}\cancel{2}\cancel{1} \\ - \quad 8516 \\ \hline 7808 \end{array}$	<p>Compact column subtraction for large numbers</p> $\begin{array}{r} 214715 \\ \cancel{2}\cancel{4}\cancel{6}\cancel{8}\cancel{7} \\ - 16458 \\ \hline 18227 \end{array}$
	<p>Continue to use counting up subtraction for subtractions involving money, including finding change or, e.g. £50 - £28.76</p> <p> <math>24p</math>   <math>£1</math>   <math>£20</math>  <math>£28.76</math>   <math>£29</math>   <math>£30</math>   <math>£50</math> </p>	<p>Use counting up subtraction when dealing with money, e.g. £100 - £78.56 or £45.23 - £27.57</p> <p> <math>44p</math>   <math>£1</math>   <math>£20</math>  <math>£78.56</math>   <math>£79</math>   <math>£80</math>   <math>£100</math> </p>
	<p>Use counting up subtraction to subtract decimal numbers, e.g. 4.2 - 1.74</p> <p> <math>0.06</math>   <math>0.2</math>   <math>2.2</math>  <math>1.74</math>   <math>1.80</math>   <math>2.0</math>   <math>4.2</math> </p>	<p>Use counting up subtraction to subtract decimal numbers, e.g. 13.1 - 2.37</p> <p> <math>0.13</math>   <math>0.50</math>   <math>10.1</math>  <math>2.37</math>   <math>2.50</math>   <math>3.00</math>   <math>13.1</math> </p>
	<p>Subtracting fractions with like denominators, e.g. <math>1\frac{1}{8} - \frac{3}{8}</math> as <math>1\frac{2}{8} - \frac{3}{8}</math> or <math>\frac{10}{8} - \frac{3}{8} = \frac{7}{8}</math></p>	<p>Subtracting fractions with unlike denominators, e.g. <math>1\frac{1}{3} - \frac{2}{3}</math> as <math>1\frac{3}{12} - \frac{8}{12}</math> or <math>\frac{15}{12} - \frac{8}{12} = \frac{7}{12}</math></p>



	Year 5	Year 6												
<b>Mental Division</b>	<p><b>Doubling and halving</b> Halve amounts of money using partitioning, e.g. half of £14.84 as half of £14 and half of 84p</p> <p>Use doubling and halving as a strategy in dividing by 2, 4, 8, 5 and 20, e.g. <math>115 \div 5</math> as double <math>115</math> (<math>230</math>) <math>\div 10</math></p> <p><b>Grouping</b> Divide numbers by 10, 100, 1000 to obtain decimal answers with up to three places, e.g. <math>340 \div 100 = 3.4</math>. Use the <math>10^{\text{th}}</math>, <math>20^{\text{th}}</math>, <math>30^{\text{th}}</math>... multiple of the divisor to divide friendly 2-digit and 3-digit numbers by single-digit numbers, e.g. <math>186 \div 6</math> as <math>30 \times 6</math> (180) and <math>1 \times 6</math> (6) Find unit &amp; non-unit fractions of large amounts, e.g. <math>\frac{3}{5}</math> of 265 is <math>3 \times (265 \div 5)</math></p> <p><b>Using number facts</b> Use division facts from the times tables up to <math>12 \times 12</math> to divide multiples of powers of ten of the divisor, e.g. <math>3600 \div 9</math> using <math>36 \div 9</math> Know square numbers and cube numbers</p>	<p><b>Doubling and halving</b> Halve decimal numbers with up to 2-places using partitioning, e.g. half of 36.86 is half of 36 (18) plus half of 0.86 (0.43)</p> <p>Use doubling and halving as strategies in mental division, e.g. <math>216 \div 4</math> is half of 216 (108) and half of 108 (54)</p> <p><b>Grouping</b> Use <math>10^{\text{th}}</math>, <math>20^{\text{th}}</math>, <math>30^{\text{th}}</math>, ... or <math>100^{\text{th}}</math>, <math>200^{\text{th}}</math>, <math>300^{\text{th}}</math>... multiples of the divisor to divide large numbers, e.g. <math>378 \div 9</math> as <math>40 \times 9 = 360</math> and <math>2 \times 9 = 18</math> so the answer is 42 Use tests for divisibility, e.g. 135 divides by 3 as <math>1 + 3 + 5 = 9</math> and 9 is in the 3x table</p> <p><b>Using number facts</b> Use division facts from the times tables up to <math>12 \times 12</math> to divide decimal numbers by single-digit numbers, e.g. <math>1.17 \div 3</math> is <math>\frac{1}{100}</math> of <math>117 \div 3</math> (0.39)</p>												
	<b>Written Division</b>	<p>Written version of a mental strategy for 3-digit <math>\div</math> 1 digit numbers</p> <p>Short division of 3-digit and 4-digit numbers by single-digit numbers</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math display="block">\begin{array}{r} \square \times 6 = 326 \\ 50 \times 6 = \underline{300} \\ 26 \\ 4 \times 6 = \underline{24} \\ 2 \\ 54 \text{ r}2 \end{array}</math> </div> <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-top: 10px;"> <math display="block">\begin{array}{r} 1 \ 2 \ 6 \ 4 \\ 6 \overline{) 7 \ 1 \ 5 \ 3 \ 8 \ 2 \ 4} \end{array}</math> </div>	<p>Short division of 3-digit and 4-digit numbers by single-digit numbers</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math display="block">\begin{array}{r} 1 \ 2 \ 6 \ 4 \\ 6 \overline{) 7 \ 1 \ 5 \ 3 \ 8 \ 2 \ 4} \end{array}</math> </div> <p>Long division of 3-digit and 4-digit numbers by two-digit numbers</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <table style="border-collapse: collapse;"> <tr> <td style="padding-right: 10px;"><math>200 + 50 + 1</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">15</td> </tr> <tr> <td><math>15 \overline{) 3765}</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">30</td> </tr> <tr> <td><math>\underline{3000}</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">45</td> </tr> <tr> <td><math>765</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">60</td> </tr> <tr> <td><math>\underline{750}</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">75</td> </tr> <tr> <td><math>15</math></td> <td style="border-left: 1px solid black; padding-left: 10px;">90</td> </tr> </table> </div> <p>Divide fractions by whole numbers, e.g. <math>\frac{1}{4} \div 3 = \frac{1}{12}</math></p>	$200 + 50 + 1$	15	$15 \overline{) 3765}$	30	$\underline{3000}$	45	$765$	60	$\underline{750}$	75	$15$
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TN August 2015