

## St Barnabas

Church of England Primary Academy
a member of CDARI
Our Vision: ‘Achieving great things through learning and growing together in a love-filled Christian family'
'That they shall have life,
life in all its fullness!'John 1
Progression in Calculations
Addition

| Objective and strategies | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Combining two parts to make a whole: part whole model | Use cubes to add two numbers together as a group or in a bar. |  | $\begin{aligned} & 4+3=7 \\ & 10=6+4 \\ & \begin{array}{l} \text { Use the part-part } \\ \text { whole diagram as } \\ \text { shown above to } \\ \text { move into the } \\ \text { abstract. } \end{array} \end{aligned}$ |


| Starting at the bigger number and counting on | Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer. | $12+5=17$ <br> Start at the larger number on the number line and count on in ones or in one jump to find the answer. | $5+12=17$ <br> Place the larger number in your head and count on the smaller number to find your answer. |
| :---: | :---: | :---: | :---: |
| Regrouping to make 10. | $6+5=11$ <br> Start with the bigger number and use the smaller number to make 10. | Use pictures or a number line. Regroup or partition the smaller number to make 10. | $7+4=11$ <br> If I am at seven, how many more do I need to make 10. How many more do I add on now? |


| Adding three single digits | $4+7+6=17$ <br> Put 4 and 6 together to make 10. Add on 7. <br> Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit. | Add together three groups of objects. Draw a picture to recombine the groups to make 10. | $\begin{aligned} 4^{4+7+6} & =10+7 \\ & =17 \end{aligned}$ <br> Combine the two numbers that make 10 and then add on the remainder. |
| :---: | :---: | :---: | :---: |
| Column method- no regrouping | $24+15=$ <br> Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters. | After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. | Calculations $\begin{array}{r} 21+42= \\ 21 \\ +\underline{42} \end{array}$ |



Subtraction

\begin{tabular}{|c|c|c|c|}
\hline Objective and strategies \& Concrete \& Pictorial \& Abstract <br>
\hline Taking away ones \& Use physical objects, counters, cubes etc to show how objects can be taken away.

$6-2=4$ \& Cross out drawn objects to show what has been taken away.

$$
15-3=12
$$ \& \[

$$
\begin{aligned}
& 18-3=15 \\
& 8-2=6
\end{aligned}
$$
\] <br>

\hline Counting back \& | Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. |
| :--- |
| Use counters and move them away from the group as you take them away counting backwards as you go. | \& | Count back on a number line or number track |
| :--- |
| Start at the bigger number and count back the smaller number showing the jumps on the number line. |
| This can progress all the way to counting back using two 2 digit numbers. | \& Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

$$
13-4=9
$$ <br>

\hline
\end{tabular}

| Find the difference | Compare amounts and objects to find the difference. <br> Use cubes to build towers or make bars to find the difference <br> Use basic bar models with items to find the difference | Count on to find the difference. <br> Comparison Bar Models <br> Draw bars to find the difference between 2 numbers. <br> Lisa is 13 years old. Her sister 1222 years old. Find the difference in oge between them. | Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches. $23-15=8$ |
| :---: | :---: | :---: | :---: |
| Part Part Whole Model | Link to addition- use the part whole model to help explain the inverse between addition and subtraction. <br> If 10 is the whole and 6 is one of the parts. What is the other part? $10-6=$ | Use a pictorial representation of objects to show the part part whole model. | Move to using numbers within the part whole model. |
| Make 10 | $14-9=$ <br> Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5 . You are left with the answer of 9. | Start at 13. Take away 3 to reach 10 . Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer. | 16-8= How many do we take off to reach the next 10 ? How many do we have left to take off? |


| Column method without regrouping |  <br> Use Base 10 to make the bigger number then take the smaller number away. <br> Show how you partition numbers to subtract. <br> Again make the larger number first. |  | $\begin{gathered} 47-24=23 \\ -20+7 \\ -20+4 \\ \hline 20+3 \\ \hline \end{gathered}$ <br> This will lead to a clear written column subtraction. $\begin{array}{r} 32 \\ -12 \\ -20 \\ \hline \end{array}$ |
| :---: | :---: | :---: | :---: |
| Column method with regrouping | Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. <br> Make the larger number with the place value counters <br> Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones. | Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. <br> When confident, children can find their own way to record the exchange/regrouping. <br> Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup. | Children can start their formal written method by partitioning the number into clear place value columns. <br> Moving forward the children use a more compact method. |


|  | Now I can subtract my ones. <br> Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens. <br> Now I can take away eight tens and complete my subtraction <br> Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount. |  | This will lead to an understanding of subtracting any number including decimals. $\begin{array}{rrrr}  & 512 & 1 \\ 26 & 6 & 0 \\ & 2 & 6 & 5 \\ \hline 2 & 3 & 6 & 5 \end{array}$ |
| :---: | :---: | :---: | :---: |

## Multiplication

| Objective and strategies | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Doubling | Use practical activities to show how to double a number. | Draw pictures to show how to double a number. <br> Double 4 is 8 | Partition a number and then double each part before recombining it back together. |
| Counting in multiples | Count in multiples supported by concrete objects in equal groups. | Use a number line or pictures to continue support in counting in multiples. <br> 1 2 3 4 5 6 7 8 9 <br> 11 12 13 14 5 16 17 18 19 <br> $\begin{array}{llllllllllll}11 & 12 & 13 & 14 & 15 & 16 & 17 & 18 & 19 & 20\end{array}$ <br> 21 22 23 24 25 26 27 28 29 30 <br> 31 32 33 34 35 36 37 38 39 40 <br>  <br> $\begin{array}{llllllllll}51 & 52 & 53 & 54 & 55 & 56 & 57 & 58 & 59 & 60\end{array}$ <br> $\begin{array}{llllllllll}61 & 62 & 63 & 64 & 65 & 66 & 67 & 68 & 69 & 70\end{array}$ <br> $\begin{array}{llllllllll}71 & 72 & 74 & 75 & 76 & 77 & 78 & 79 & 80\end{array}$ <br> 81 82 83 84 85 86 87 88 <br> 9 89 90      <br> 91 92 93 94 95 96 97 98 <br> 99 100       <br> 979899100 | Count in multiples of a number aloud. <br> Write sequences with multiples of numbers. $2,4,6,8,10$ <br> $5,10,15,20,25,30$ |


| Repeated addition | Use different objects to add equal groups. | There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? <br> 2 add 2 add 2 equals 6$5+5+5=15$1 26 3 46 5 8 7 8 9 <br> 11 12 13 14 15 16 17 18 19 <br> 21 22 23 24 25 26 27 28 29 | Write addition sentences to describe objects and pictures. |
| :---: | :---: | :---: | :---: |
| Arrays showing commutative multiplication | Create arrays using counters/ cubes to show multiplication sentences. e.g. 4 rows of $6=24$ | Draw arrays in different rotations to find commutative multiplication sentences. $\begin{aligned} & 0000^{4 \times 2=8} \\ & 0000^{2 \times 4-8} \\ & 00^{2 \times 4=8} \\ & 00^{2 \times 2} \\ & 00 \\ & 4 \times 2=8 \end{aligned}$ <br> Link arrays to area of rectangles. | Use an array to write multiplication sentences and reinforce repeated addition. $\begin{aligned} & 5+5+5=15 \\ & 3+3+3+3+3=15 \\ & 5 \times 3=15 \\ & 3 \times 5=15 \end{aligned}$ |



| Column multiplication | Children can continue to be supported by place value counters at the stage of multiplication. <br> It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. | Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods. $\square$ <br> 250 ch ! $\longrightarrow$ $4+4+8+8+16$ $5=8=40 j 496$ | Start with long multiplication, reminding the children about lining up their numbers clearly in columns. <br> If it helps, children can write out what they are solving next to their answer. <br> This moves to the more compact method. |
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## Division

| Objective and strategies | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Sharing objects into groups | I have 10 cubes, can you share them equally in 2 groups? | Children use pictures or shapes to share quantities. | Share 9 buns between three people. $9 \div 3=3$ |
| Division as grouping | Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. | Use a number line to show jumps in groups. The number of jumps equals the number of groups. <br> Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. $\begin{aligned} & 20 \div 5=? \\ & 5 \times ?=20 \end{aligned}$ | $28 \div 7=4$ <br> Divide 28 into 7 groups. How many are in each group? |


| Division within arrays | Link division to multiplication by creating an array and thinking about the number sentences that can be created. $\begin{array}{rr} \mathrm{Eg} 15 \div 3=5 & 5 \times 3=15 \\ 15 \div 5=3 & 3 \times 5=15 \end{array}$ | Draw an array and use lines to split the array into groups to make multiplication and division sentences. | Find the inverse of multiplication and division sentences by creating four linking number sentences. $\begin{aligned} & 7 \times 4=28 \\ & 4 \times 7=28 \\ & 28 \div 7=4 \\ & 28 \div 4=7 \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| Division with a remainder | $14 \div 3=$ <br> Divide objects between groups and see how much is left over | Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. <br> Draw dots and group them to divide an amount and clearly show a remainder. | Complete written divisions and show the remainder using $r$. |


| Division by Subtraction (Chunking) | $48 \div 4=12\binom{\text { groups }}{\text { of } 4}$ <br> 48 CIM <br> $44=50$ <br> 40 ERE <br> 360100 <br> 005 <br> 28 -ana <br> 4 - <br> 20 푸붑 <br> $16 \square 104$ <br> $12 \square$ <br> 8 <br> 4 <br> 0 | $\begin{aligned} 48+4 & =10(\text { groups of } 4)+2(\text { groups of } 4) \\ & =12(\text { groups of } 4) \end{aligned}$ | Progressing to: <br> If children have full conceptual understanding and are proficient with chunking method, they may be taught short (bus stop) and long division. |
| :---: | :---: | :---: | :---: |


| Short division |  <br> Use place value counters to divide using the bus stop method alongside <br> Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over. <br> We exchange this ten for ten ones and then share the ones equally among the groups. <br> We look how much in 1 group so the answer is 14. | Children can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. <br> Encourage them to move towards counting in multiples to divide more efficiently | Begin with divisions that divide equally with no remainder <br> Move onto divisions with a remainder. <br> Finally move into decimal places to divide the total accurately. |
| :---: | :---: | :---: | :---: |


| Long division | 2544 + 12 <br> How many groups of 12 thousands do we have? None <br> Exchange 2 thousand for 20 hundreds. $1 2 \longdiv { 2 5 4 4 }$ <br> How many groups of 12 are in 25 hundreds? 2 groups. Circle them. We have grouped 24 hundreds so can take them off and we are left with one. <br> Exchange the one hundred for ten tens so now we have 14 tens. How many groups of 12 are in 14 ? 1 remainder 2 $\text { 12 } \begin{array}{r} \frac{021}{2544} \\ \frac{24}{14} \\ \frac{12}{2} \end{array}$ <br> Exchange the two tens for twenty ones so now we have 24 ones. How many groups of 12 are in 24? 2 | Instead of using physical counters, children can draw the counters and circle the groups on a whiteboard or in their books. <br> Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process. | $20 \begin{array}{rrrr} 0 & 3 & 1 & 8 \\ 6 & 3 & 6 & 5 \\ -6 & 0 & \downarrow & 1 \\ -3 & 6 \\ -2 & 1 \\ 2 & 0 & 1 \\ -1 & 6 & 5 \\ -1 & 6 & 0 \\ \hline \end{array}$ |
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