

Our Vision: 'Achieving great things through learning and growing together in a love-filled Christian family' 'That they shall have life, life in all its fullness!'John 1

### **Progression in Calculations**

#### **Addition**

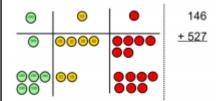
Objective and strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part whole model		yhole 2	4 + 3 = 7 10= 6 + 4
	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	Use the part-part whole diagram as shown above to move into the abstract.

Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17   Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17  Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10.	6 + 5 = 11	Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11  If I am at seven, how many more do I need to make 10. How many more do I add on now?
	Start with the bigger number and use the smaller number to make 10.	9 + 5 = 14 1 4 +4 0 1 2 3 4 5 6 7 8 9 (10) 11 12 13 (14) 15 16 17 18 19 20	

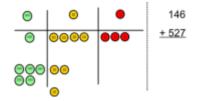
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7.		4+7+6=10+7 $=17$ Combine the two numbers that make 10 and then add on the remainder.
	Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	
Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.	Calculations 21 + 42 = 21 + 42

Column method regrouping

Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10



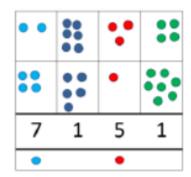
Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added. This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

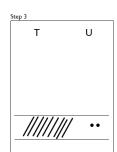
As children move on to decimals, money and decimal place value counters can be used to support learning.

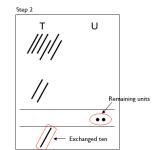




Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.

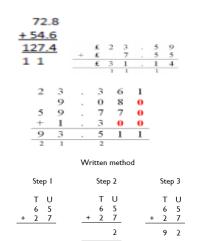






Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

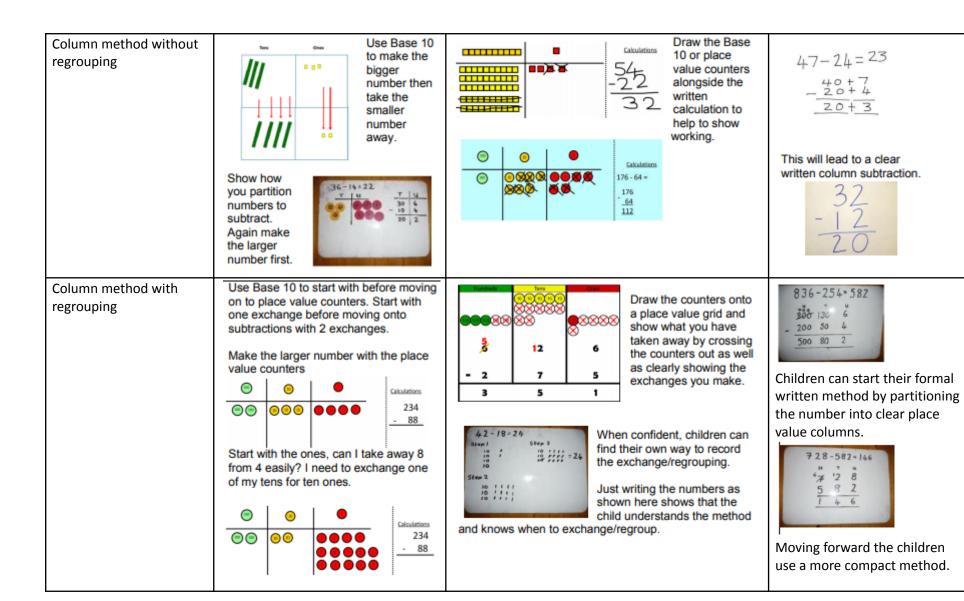
As the children
move on, introduce decimals
with the same number of
decimal places and different.
Money can be used
here.



### Subtraction

Objective and strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away.  6 - 2 = 4	Cross out drawn objects to show what has been taken away.	18 -3= 15 8 - 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.  13 – 4  Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track  9 10 11 12 13 14 15  Start at the bigger number and count back the smaller number showing the jumps on the number line.  This can progress all the way to counting back using two 2 digit numbers.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.  13 – 4 = 9

Find the difference	Compare amounts and objects to find the difference.  Use cubes to build towers or make bars to find the difference  Use basic bar models with items to find the difference	Count on to find the difference.  Comparison Bar Models  Comparison Bar Models  Comparison Bar Models  Comparison Bar Models  Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.  23 – 15 = 8
Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction.  If 10 is the whole and 6 is one of the parts. What is the other part?  10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	Move to using numbers within the part whole model.
Make 10	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 -4 -3  Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?

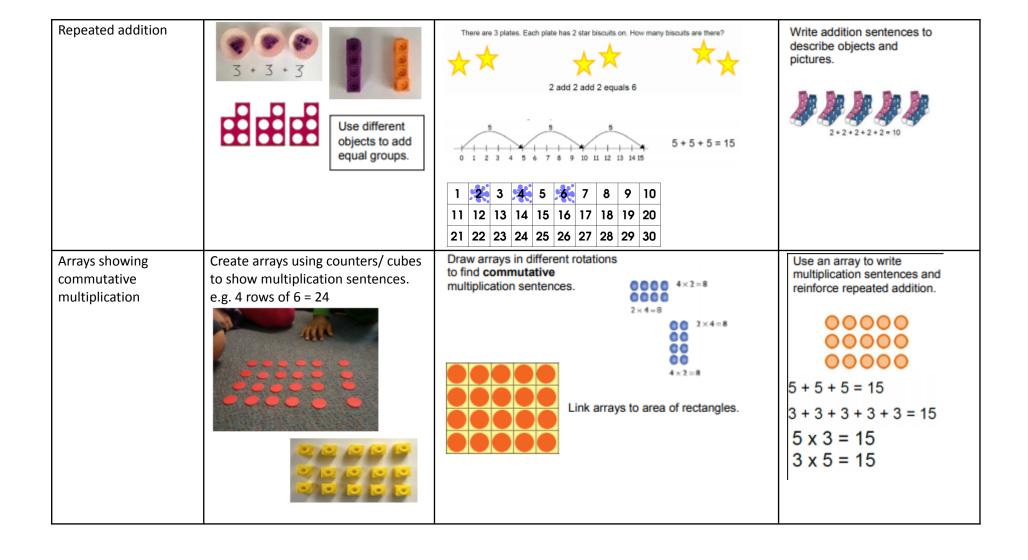


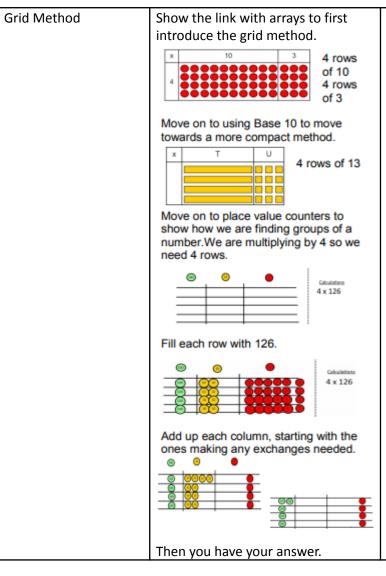
Now I can subtract my ones. Calculations 234 00 00 - 88 Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens. Calculations 234 - 88 000000 00000 Now I can take away eight tens and complete my subtraction Calculations 1234 - 88 Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

This will lead to an understanding of subtracting any number including decimals.

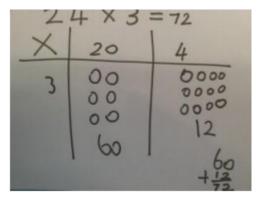
# Multiplication

Objective and strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.  double 4 is 8  4×2=8	Draw pictures to show how to double a number.  Double 4 is 8	16 10 6 1 x2 1 x2 20 12  Partition a number and then double each part before recombining it back together.
Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.  1 2 3 4 \$ 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 54 64 74 84 99 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 78 00 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100	Count in multiples of a number aloud.  Write sequences with multiples of numbers.  2, 4, 6, 8, 10  5, 10, 15, 20, 25, 30





Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

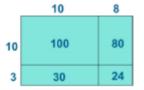


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

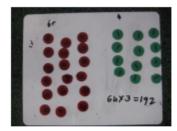
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

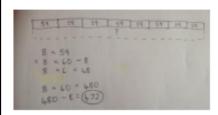
Column multiplication

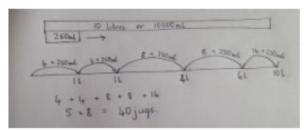
Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.





Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

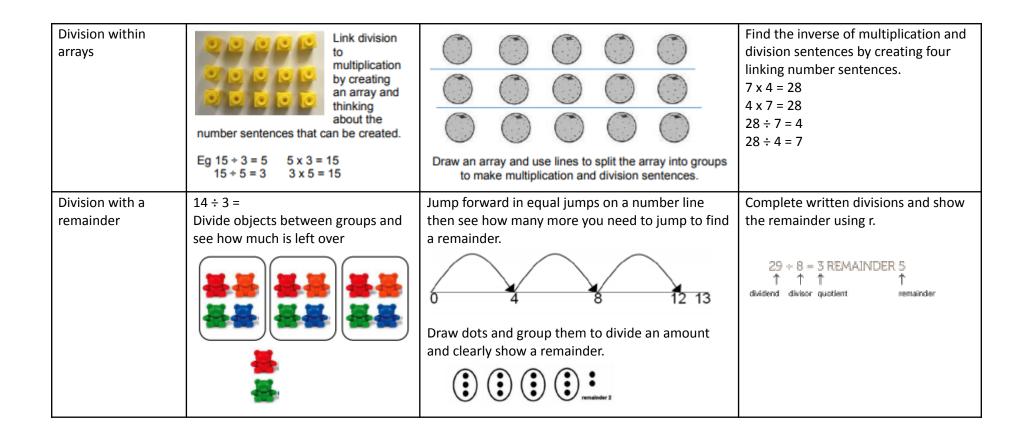
If it helps, children can write out what they are solving next to their answer.

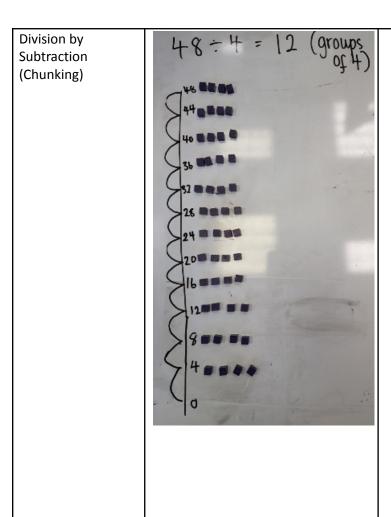


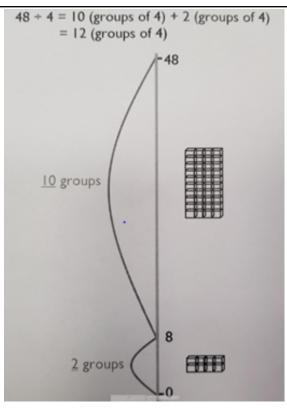
This moves to the more compact method.

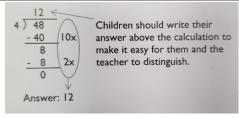
# **Division**

Objective and strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities.  8 ÷ 2 = 4	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.  96 + 3 = 32	Use a number line to show jumps in groups. The number of jumps equals the number of groups.  O 1 2 3 4 5 6 7 8 9 10 11 12  Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	28 ÷ 7 = 4  Divide 28 into 7 groups. How many are in each group?

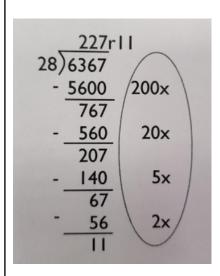






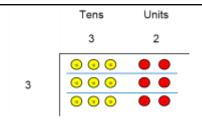


Progressing to:

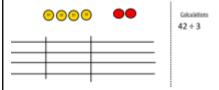


If children have full conceptual understanding and are proficient with chunking method, they may be taught short (bus stop) and long division.

Short division

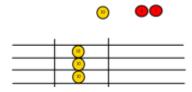


Use place value counters to divide using the bus stop method alongside

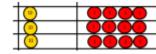


42 ÷ 3=

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

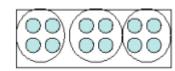


We exchange this ten for ten ones and then share the ones equally among the groups.



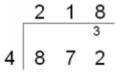
We look how much in 1 group so the answer is 14.

Children can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



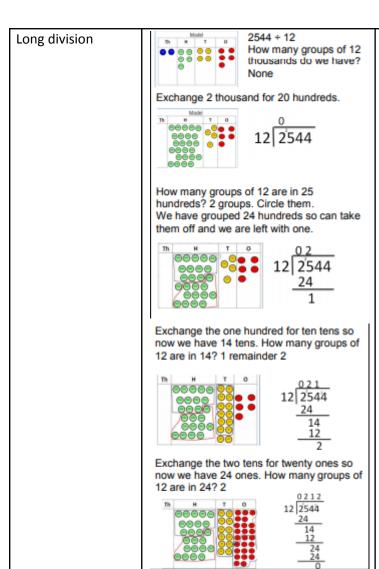
Encourage them to move towards counting in multiples to divide more efficiently

Begin with divisions that divide equally with no remainder



Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.



Instead of using physical counters, children can draw the counters and circle the groups on a whiteboard or in their books.

Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process.

