



**Number: Number and Place Value Progression**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery 3/4	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Counting	<ul style="list-style-type: none"> <li>Recite numbers past 5.</li> <li>Say one number for each item in order: 1,2,3,4,5.</li> <li>Know that the last number reached when counting a small set of objects tells you how many there are in total ('cardinal principle').</li> </ul>	<ul style="list-style-type: none"> <li>Count objects, actions and sounds. (DM)</li> <li>Count beyond ten. (DM)</li> <li>Verbally count beyond 20, recognising the pattern of the counting system. (ELG)</li> <li>Understand the 'one more than/one less than' relationship between consecutive numbers.(DM)</li> </ul>	<ul style="list-style-type: none"> <li>count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number</li> <li>count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens</li> <li>given a number, identify one more and one less</li> </ul>	<ul style="list-style-type: none"> <li>count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward</li> </ul>	<ul style="list-style-type: none"> <li>count from 0 in multiples of 4, 8, 50 and 100;</li> <li>find 10 or 100 more or less than a given number</li> </ul>	<ul style="list-style-type: none"> <li>count backwards through zero to include negative numbers</li> <li>count in multiples of 6, 7, 9, 25 and 1 000</li> <li>find 1 000 more or less than a given number</li> </ul>	<ul style="list-style-type: none"> <li>interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero</li> <li>count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000</li> </ul>	<ul style="list-style-type: none"> <li>use negative numbers in context, and calculate intervals across zero</li> </ul>
Comparing Numbers	<ul style="list-style-type: none"> <li>Compare quantities using language: 'more than', 'fewer than'.</li> </ul>	<ul style="list-style-type: none"> <li>Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity. (ELG)</li> <li>Compare numbers. (DM)</li> </ul>	<ul style="list-style-type: none"> <li>use the language of: equal to, more than, less than (fewer), most, least</li> </ul>	<ul style="list-style-type: none"> <li>compare and order numbers from 0 up to 100; use &lt;, &gt; and = signs</li> </ul>	<ul style="list-style-type: none"> <li>compare and order numbers up to 1 000</li> </ul>	<ul style="list-style-type: none"> <li>order and compare numbers beyond 1 000</li> <li>compare numbers with the same number of decimal places up to two decimal places</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers up to 10 000 000 and determine the value of each digit</li> </ul>
Identifying, representing and estimating numbers	<ul style="list-style-type: none"> <li>Develop fast recognition of up to 3 objects, without having to count them individually ('subitising').</li> <li>Show 'finger numbers' up to 5.</li> </ul>	<ul style="list-style-type: none"> <li>Have a deep understanding of number to 10, including the composition of each number (ELG)</li> <li>Subitise (recognise quantities without counting) up to 5. (ELG)</li> <li>Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally. (ELG)</li> </ul>	<ul style="list-style-type: none"> <li>identify and represent numbers using objects and pictorial representations including the number line</li> </ul>	<ul style="list-style-type: none"> <li>identify, represent and estimate numbers using different representations, including the number line</li> </ul>	<ul style="list-style-type: none"> <li>identify, represent and estimate numbers using different representations</li> </ul>	<ul style="list-style-type: none"> <li>identify, represent and estimate numbers using different representations</li> </ul>		
Reading and writing numbers	<ul style="list-style-type: none"> <li>Link numerals and amounts: for example, showing the right number of objects to match the numeral, up to 5.</li> <li>Experiment with their own symbols and marks as well as numerals.</li> </ul>	<ul style="list-style-type: none"> <li>Link the number symbol (numeral) with its cardinal number value. (DM)</li> </ul>	<ul style="list-style-type: none"> <li>read and write numbers from 1 to 20 in numerals and words.</li> </ul>	<ul style="list-style-type: none"> <li>read and write numbers to at least 100 in numerals and in words</li> </ul>	<ul style="list-style-type: none"> <li>read and write numbers up to 1 000 in numerals and in words</li> </ul>		<ul style="list-style-type: none"> <li>read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit</li> <li>(appears also in Comparing Numbers)</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers up to 10 000 000 and determine the value of each digit</li> <li>(appears also in Understanding Place Value)</li> </ul>
Understanding Place Value				<ul style="list-style-type: none"> <li>recognise the place value of each digit in a two-digit number (tens, ones)</li> </ul>	<ul style="list-style-type: none"> <li>recognise the place value of each digit in a three-digit number (hundreds, tens, ones)</li> </ul>	<ul style="list-style-type: none"> <li>recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones)</li> <li>find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as units, tenths and hundredths</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit</li> <li>recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers up to 10 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers)</li> <li>identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1 000 where the answers are up to three decimal places</li> </ul>



Rounding						<ul style="list-style-type: none"> <li>round any number to the nearest 10, 100 or 1 000</li> <li>round decimals with one decimal place to the nearest whole number</li> </ul>	<ul style="list-style-type: none"> <li>round any number up to 1 000 000 to the nearest 10, 100, 1 000, 10 000 and 100 000</li> <li>round decimals with two decimal places to the nearest whole number and to one decimal place</li> </ul>	<ul style="list-style-type: none"> <li>round any whole number to a required degree of accuracy</li> <li>solve problems which require answers to be rounded to specified degrees of accuracy</li> </ul>
Problem Solving				<ul style="list-style-type: none"> <li>use place value and number facts to solve problems</li> </ul>	<ul style="list-style-type: none"> <li>solve number problems and practical problems involving these ideas.</li> </ul>	<ul style="list-style-type: none"> <li>solve number and practical problems that involve all of the above and with increasingly large positive numbers</li> </ul>	<ul style="list-style-type: none"> <li>solve number problems and practical problems that involve all of the above</li> </ul>	<ul style="list-style-type: none"> <li>solve number and practical problems that involve all of the above</li> </ul>



**Number: Addition and Subtraction**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Number Bonds		<ul style="list-style-type: none"> <li>Explore the composition of numbers to 10. (DM)</li> <li>Automatically recall number bonds for numbers 0–5 and some to 10. (DM)</li> <li>Have a deep understanding of number to 10, including the composition of each number (ELG)</li> <li>Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts. (ELG)</li> </ul>	<ul style="list-style-type: none"> <li>represent and use number bonds and related subtraction facts within 20</li> </ul>	<ul style="list-style-type: none"> <li>recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100</li> </ul>				
Mental Calculation			<ul style="list-style-type: none"> <li>add and subtract one-digit and two-digit numbers to 20, including zero</li> <li>read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs</li> <li>(appears also in Written Methods)</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract numbers using concrete objects, pictorial representations, and mentally, including:                             <ul style="list-style-type: none"> <li>a two-digit number and ones</li> <li>a two-digit number and tens</li> <li>two two-digit numbers</li> <li>adding three one-digit numbers</li> </ul> </li> <li>show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract numbers mentally, including:                             <ul style="list-style-type: none"> <li>a three-digit number and ones</li> <li>a three-digit number and tens</li> <li>a three-digit number and hundreds</li> </ul> </li> </ul>		<ul style="list-style-type: none"> <li>add and subtract numbers mentally with increasingly large numbers</li> </ul>	<ul style="list-style-type: none"> <li>perform mental calculations, including with mixed operations and large numbers</li> <li>use their knowledge of the order of operations to carry out calculations involving the four operations</li> </ul>
Written Methods			<ul style="list-style-type: none"> <li>read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs</li> <li>(appears also in Mental Calculation)</li> </ul>		<ul style="list-style-type: none"> <li>add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)</li> </ul>	
Inverse operations, estimating and checking				<ul style="list-style-type: none"> <li>recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.</li> </ul>	<ul style="list-style-type: none"> <li>estimate the answer to a calculation and use inverse operations to check answers</li> </ul>	<ul style="list-style-type: none"> <li>estimate and use inverse operations to check answers to a calculation</li> </ul>	<ul style="list-style-type: none"> <li>use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy</li> </ul>	<ul style="list-style-type: none"> <li>use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.</li> </ul>



Problem Solving	<ul style="list-style-type: none"> <li>Solve real world mathematical problems with numbers up to 5.</li> </ul>		<ul style="list-style-type: none"> <li>solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as</li> <li><math>7 = \_ - 9</math></li> </ul>	<ul style="list-style-type: none"> <li>solve problems with addition and subtraction:             <ul style="list-style-type: none"> <li>using concrete objects and pictorial representations, including those involving numbers, quantities and measures</li> <li>applying their increasing knowledge of mental and written methods</li> </ul> </li> <li>solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change</li> </ul>	<ul style="list-style-type: none"> <li>solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction</li> </ul>	<ul style="list-style-type: none"> <li>solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why</li> </ul>	<ul style="list-style-type: none"> <li>solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why</li> </ul>	<ul style="list-style-type: none"> <li>solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why</li> <li>Solve problems involving addition, subtraction, multiplication and division</li> </ul>
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**Number: Multiplication and Division**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Multiplication and Division facts		<ul style="list-style-type: none"> <li>Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally. (ELG)</li> </ul>	<ul style="list-style-type: none"> <li>count in multiples of twos, fives and tens</li> </ul>	<ul style="list-style-type: none"> <li>count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward</li> <li>recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers</li> </ul>	<ul style="list-style-type: none"> <li>count from 0 in multiples of 4, 8, 50 and 100</li> <li>recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables</li> </ul>	<ul style="list-style-type: none"> <li>count in multiples of 6, 7, 9, 25 and 1 000</li> <li>recall multiplication and division facts for multiplication tables up to <math>12 \times 12</math></li> </ul>	<ul style="list-style-type: none"> <li>count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000</li> </ul>	
Mental Calculation				<ul style="list-style-type: none"> <li>show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot</li> </ul>	<ul style="list-style-type: none"> <li>write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods</li> </ul>	<ul style="list-style-type: none"> <li>use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers</li> <li>recognise and use factor pairs and commutativity in mental calculations</li> </ul>	<ul style="list-style-type: none"> <li>multiply and divide numbers mentally drawing upon known facts</li> <li>multiply and divide whole numbers and those involving decimals by 10, 100 and 1000</li> </ul>	<ul style="list-style-type: none"> <li>perform mental calculations, including with mixed operations and large numbers</li> <li>associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. <math>\frac{3}{8}</math>)</li> </ul>
Written Calculation				<ul style="list-style-type: none"> <li>calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (<math>\times</math>), division (<math>\div</math>) and equals (=) signs</li> </ul>	<ul style="list-style-type: none"> <li>write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods</li> </ul>	<ul style="list-style-type: none"> <li>multiply two-digit and three-digit numbers by a one-digit number using formal written layout</li> </ul>	<ul style="list-style-type: none"> <li>multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers</li> <li>divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context</li> </ul>	<ul style="list-style-type: none"> <li>multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication</li> <li>divide numbers up to 4-digits by a two-digit whole number using the formal written method of short division where appropriate for the context divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context</li> <li>use written division methods in cases where the answer has up to two decimal places</li> </ul>
Properties of numbers: multiples, factors, primes, square and cube numbers						<ul style="list-style-type: none"> <li>recognise and use factor pairs and commutativity in mental calculations (repeated)</li> </ul>	<ul style="list-style-type: none"> <li>identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.</li> <li>know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers</li> <li>establish whether a number up to 100 is prime and recall prime numbers up to 19</li> <li>recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3)</li> </ul>	<ul style="list-style-type: none"> <li>identify common factors, common multiples and prime numbers</li> <li>use common factors to simplify fractions; use common multiples to express fractions in the same denomination (copied from Fractions)</li> </ul>



Order of Operations								<ul style="list-style-type: none"> <li>use their knowledge of the order of operations to carry out calculations involving the four operations</li> </ul>
Inverse Operations, estimating and checking answers					<ul style="list-style-type: none"> <li>estimate the answer to a calculation and use inverse operations to check answers (copied from Addition and Subtraction)</li> </ul>	<ul style="list-style-type: none"> <li>estimate and use inverse operations to check answers to a calculation (copied from Addition and Subtraction)</li> </ul>		<ul style="list-style-type: none"> <li>use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy</li> </ul>
Problem Solving			<ul style="list-style-type: none"> <li>solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts</li> </ul>	<ul style="list-style-type: none"> <li>solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes</li> <li>solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign</li> <li>solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving addition, subtraction, multiplication and division</li> </ul>

**Number: Fractions, including decimals and percentages**

Counting in fractional steps	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
				<ul style="list-style-type: none"> <li><i>Pupils should count in fractions up to 10, starting from any number and using the 1/2 and 2/4 equivalence on the number line (Non Statutory Guidance)</i></li> </ul>	<ul style="list-style-type: none"> <li>count up and down in tenths</li> </ul>	<ul style="list-style-type: none"> <li>count up and down in hundredths</li> </ul>		



Recognising fractions			<ul style="list-style-type: none"> <li>recognise, find and name a half as one of two equal parts of an object, shape or quantity</li> <li>recognise, find and name a quarter as one of four equal parts of an object, shape or quantity</li> </ul>	<ul style="list-style-type: none"> <li>recognise, find, name and write fractions <math>\frac{1}{3}</math>, <math>\frac{1}{4}</math>, <math>\frac{2}{4}</math> and <math>\frac{3}{4}</math> of a length, shape, set of objects or quantity</li> </ul>	<ul style="list-style-type: none"> <li>recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators</li> <li>recognise that tenths arise from dividing an object into 10 equal parts and in dividing one – digit numbers or quantities by 10.</li> <li>recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators</li> </ul>	<ul style="list-style-type: none"> <li>recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten</li> </ul>	<ul style="list-style-type: none"> <li>recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (appears also in Equivalence)</li> </ul>	
Comparing fractions					<ul style="list-style-type: none"> <li>compare and order unit fractions, and fractions with the same denominators</li> </ul>		<ul style="list-style-type: none"> <li>compare and order fractions whose denominators are all multiples of the same number</li> </ul>	<ul style="list-style-type: none"> <li>compare and order fractions, including fractions <math>&gt;1</math></li> </ul>
Comparing decimals						<ul style="list-style-type: none"> <li>compare numbers with the same number of decimal places up to two decimal places</li> </ul>	<ul style="list-style-type: none"> <li>read, write, order and compare numbers with up to three decimal places</li> </ul>	<ul style="list-style-type: none"> <li>identify the value of each digit in numbers given to three decimal places</li> </ul>
Rounding including						<ul style="list-style-type: none"> <li>round decimals with one decimal place to the nearest whole number</li> </ul>	<ul style="list-style-type: none"> <li>round decimals with two decimal places to the nearest whole number and to one decimal place</li> </ul>	<ul style="list-style-type: none"> <li>solve problems which require answers to be rounded to specified degrees of accuracy</li> </ul>
Equivalence, including fractions, decimals and percentages				<ul style="list-style-type: none"> <li>write simple fractions e.g. <math>\frac{1}{2}</math> of 6 = 3 and recognise the equivalence of <math>\frac{2}{4}</math> and <math>\frac{1}{2}</math>.</li> </ul>	<ul style="list-style-type: none"> <li>recognise and show, using diagrams, equivalent fractions with small denominators</li> </ul>	<ul style="list-style-type: none"> <li>recognise and show, using diagrams, families of common equivalent fractions</li> <li>recognise and write decimal equivalents of any number of tenths or hundredths</li> <li>recognise and write decimal equivalents to <math>\frac{1}{4}</math>; <math>\frac{1}{2}</math>; <math>\frac{3}{4}</math></li> </ul>	<ul style="list-style-type: none"> <li>identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths</li> <li>read and write decimal numbers as fractions (e.g. <math>0.71 = \frac{71}{100}</math>)</li> <li>recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents</li> <li>recognise the per cent symbol (%) and understand that per cent relates to “number of parts per hundred”, and write percentages as a fraction with denominator 100 as a decimal fraction</li> </ul>	<ul style="list-style-type: none"> <li>use common factors to simplify fractions; use common multiples to express fractions in the same denomination</li> <li>associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. <math>\frac{3}{8}</math>)</li> <li>recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.</li> </ul>



Addition and subtraction of fractions					<ul style="list-style-type: none"> <li>add and subtract fractions with the same denominator within one whole (e.g. <math>5/7 + 1/7 = 6/7</math>)</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract fractions with the same denominator</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract fractions with the same denominator and multiples of the same number</li> <li>recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements <math>&gt; 1</math> as a mixed number (e.g. <math>2/5 + 4/5 = 6/5 = 11/5</math>)</li> </ul>	<ul style="list-style-type: none"> <li>add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions</li> </ul>
Multiplication and division of fractions							<ul style="list-style-type: none"> <li>multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams</li> </ul>	<ul style="list-style-type: none"> <li>multiply simple pairs of proper fractions, writing the answer in its simplest form (e.g. <math>1/4 \times 1/2 = 1/8</math>)</li> <li>divide proper fractions by whole numbers (e.g. <math>1/3 \div 2 = 1/6</math>)</li> </ul>
Multiplication and division of decimals						<ul style="list-style-type: none"> <li>find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths</li> </ul>		<ul style="list-style-type: none"> <li>multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places</li> <li>identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places</li> <li>associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. <math>3/8</math>)</li> <li>use written division methods in cases where the answer has up to two decimal places</li> </ul>
Problem Solving					<ul style="list-style-type: none"> <li>solve problems that involve all of the above</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number</li> <li>solve simple measure and money problems involving fractions and decimals to two decimal places.</li> </ul>	<ul style="list-style-type: none"> <li>solve problems involving numbers up to three decimal places</li> <li>solve problems which require knowing percentage and decimal equivalents of <math>1/2</math>, <math>1/4</math>, <math>1/5</math>, <math>2/5</math>, <math>4/5</math> and those with a denominator of a multiple of 10 or 25.</li> </ul>	

**Ratio and Proportion** (Statements only appear in Year 6, but should be connected to previous learning, particularly fractions and multiplication and division)

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6





Comparing and estimating	<ul style="list-style-type: none"> <li>Make comparisons between objects relating to size, length, weight and capacity.</li> <li>Begin to describe a sequence of events, real or fictional, using words such as 'first', 'then...'</li> </ul>	<ul style="list-style-type: none"> <li>Compare length, weight and capacity. (DM)</li> </ul>	<ul style="list-style-type: none"> <li>compare, describe and solve practical problems for: <ul style="list-style-type: none"> <li>lengths and heights [e.g. long/short, longer/shorter, tall/short, double/half]</li> <li>mass/weight [e.g. heavy/light, heavier than, lighter than]</li> <li>capacity and volume [e.g. full/empty, more than, less than, half, half full, quarter]</li> <li>time [e.g. quicker, slower, earlier, later]</li> </ul> </li> <li>sequence events in chronological order using language [e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening]</li> </ul>	<ul style="list-style-type: none"> <li>compare and order lengths, mass, volume/capacity and record the results using <math>&gt;</math>, <math>&lt;</math> and <math>=</math></li> <li>compare and sequence intervals of time</li> </ul>	<ul style="list-style-type: none"> <li>compare durations of events, for example to calculate the time taken by particular events or tasks</li> <li>estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o'clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight (appears also in Telling the Time)</li> </ul>	<ul style="list-style-type: none"> <li>estimate, compare and calculate different measures, including money in pounds and pence</li> </ul>	<ul style="list-style-type: none"> <li><i>calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm<sup>2</sup>) and square metres (m<sup>2</sup>) and estimate the area of irregular shapes</i></li> <li><i>estimate volume (e.g. using 1 cm<sup>3</sup> blocks to build cubes and cuboids) and capacity (e.g. using water)</i></li> </ul>	<ul style="list-style-type: none"> <li><i>calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm<sup>3</sup>) and cubic metres (m<sup>3</sup>), and extending to other units such as mm<sup>3</sup> and km<sup>3</sup>.</i></li> </ul>
Measuring and calculating			<ul style="list-style-type: none"> <li>measure and begin to record the following: <ul style="list-style-type: none"> <li>lengths and heights</li> <li>mass/weight</li> <li>capacity and volume</li> <li>time (hours, minutes, seconds)</li> </ul> </li> <li>recognise and know the value of different denominations of coins and notes</li> </ul>	<ul style="list-style-type: none"> <li>choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels</li> <li>recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value</li> <li>find different combinations of coins that equal the same amounts of money</li> <li>solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change</li> </ul>	<ul style="list-style-type: none"> <li>measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)</li> <li>measure the perimeter of simple 2-D shapes</li> <li>add and subtract amounts of money to give change, using both £ and p in practical contexts</li> </ul>	<ul style="list-style-type: none"> <li>estimate, compare and calculate different measures, including money in pounds and pence</li> <li>measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres</li> <li>find the area of rectilinear shapes by counting squares</li> </ul>	<ul style="list-style-type: none"> <li><i>use all four operations to solve problems involving measure (e.g. length, mass, volume, money) using decimal notation including scaling.</i></li> <li><i>measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres</i></li> <li><i>calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm<sup>2</sup>) and square metres (m<sup>2</sup>) and estimate the area of irregular shapes</i></li> </ul>	<ul style="list-style-type: none"> <li><i>solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate</i></li> <li><i>recognise that shapes with the same areas can have different perimeters and vice versa</i></li> <li><i>calculate the area of parallelograms and triangles</i></li> <li><i>calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm<sup>3</sup>) and cubic metres (m<sup>3</sup>), and extending to other units [e.g. mm<sup>3</sup> and km<sup>3</sup>].</i></li> <li><i>recognise when it is possible to use formulae for area and volume of shapes</i></li> </ul>
Telling the time			<ul style="list-style-type: none"> <li>tell the time to the hour and half past the hour and draw the hands on a clock face to show these times.</li> <li>recognise and use language relating to dates, including days of the week, weeks, months and years</li> </ul>	<ul style="list-style-type: none"> <li>tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times.</li> <li>know the number of minutes in an hour and the number of hours in a day. (appears also in Converting)</li> </ul>	<ul style="list-style-type: none"> <li>tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks</li> <li>estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o'clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight</li> </ul>	<ul style="list-style-type: none"> <li>read, write and convert time between analogue and digital 12 and 24-hour clocks (appears also in Converting)</li> </ul>		



Converting				<ul style="list-style-type: none"> <li>know the number of minutes in an hour and the number of hours in a day. (appears also in Telling the Time)</li> </ul>	<ul style="list-style-type: none"> <li>know the number of seconds in a minute and the number of days in each month, year and leap year</li> </ul>	<ul style="list-style-type: none"> <li>convert between different units of measure (e.g. kilometre to metre; hour to minute)</li> <li>read, write and convert time between analogue and digital 12 and 24-hour clocks</li> <li>solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days</li> </ul>	<ul style="list-style-type: none"> <li><i>convert between different units of metric measure (e.g. kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre)</i></li> <li><i>solve problems involving converting between units of time</i></li> <li><i>understand and use equivalences between metric units and common imperial units such as inches, pounds and pints</i></li> </ul>	<ul style="list-style-type: none"> <li><i>use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places</i></li> <li><i>convert between miles and kilometres</i></li> <li><i>solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate</i></li> </ul>
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**Geometry – Properties of Shapes**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Identifying shapes and their properties	<ul style="list-style-type: none"> <li>Talk about and explore 2D and 3D shapes (for example, circles, rectangles, triangles and cuboids) using informal and mathematical language: 'sides', 'corners'; 'straight', 'flat', 'round'.</li> </ul>		<ul style="list-style-type: none"> <li>recognise and name common 2-D and 3-D shapes, including:               <ul style="list-style-type: none"> <li>2-D shapes [e.g. rectangles (including squares), circles and triangles]</li> <li>3-D shapes [e.g. cuboids (including cubes), pyramids and spheres].</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line</li> <li>identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces</li> <li>identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid]</li> </ul>		<ul style="list-style-type: none"> <li>identify lines of symmetry in 2-D shapes presented in different orientations</li> </ul>	<ul style="list-style-type: none"> <li>identify 3-D shapes, including cubes and other cuboids, from 2-D representations</li> </ul>	<ul style="list-style-type: none"> <li>recognise, describe and build simple 3-D shapes, including making nets</li> <li>illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius</li> </ul>
Drawing and constructing	<ul style="list-style-type: none"> <li>Select shapes appropriately: flat surfaces for building, a triangular prism for a roof, etc.</li> <li>Combine shapes to make new ones – an arch, a bigger triangle, etc.</li> </ul>	<ul style="list-style-type: none"> <li>Select, rotate and manipulate shapes to develop spatial reasoning skills. (DM)</li> <li>Compose and decompose shapes so that children recognise a shape can have other shapes within it, just as numbers can. (DM)</li> </ul>			<ul style="list-style-type: none"> <li>draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them</li> </ul>	<ul style="list-style-type: none"> <li>complete a simple symmetric figure with respect to a specific line of symmetry</li> </ul>	<ul style="list-style-type: none"> <li>draw given angles, and measure them in degrees (o)</li> </ul>	<ul style="list-style-type: none"> <li>draw 2-D shapes using given dimensions and angles</li> <li>recognise, describe and build simple 3-D shapes, including making nets</li> </ul>
Comparing and classifying				<ul style="list-style-type: none"> <li>compare and sort common 2-D and 3-D shapes and everyday objects</li> </ul>		<ul style="list-style-type: none"> <li>compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes</li> </ul>	<ul style="list-style-type: none"> <li>use the properties of rectangles to deduce related facts and find missing lengths and angles</li> <li>distinguish between regular and irregular polygons based on reasoning about equal sides and angles</li> </ul>	<ul style="list-style-type: none"> <li>compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons</li> </ul>
Angles					<ul style="list-style-type: none"> <li>recognise angles as a property of shape or a description of a turn</li> <li>identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle</li> <li>identify horizontal and vertical lines and pairs of perpendicular and parallel lines</li> </ul>	<ul style="list-style-type: none"> <li>identify acute and obtuse angles and compare and order angles up to two right angles by size</li> </ul>	<ul style="list-style-type: none"> <li>know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles</li> <li>identify:               <ul style="list-style-type: none"> <li>angles at a point and one whole turn (total 360o)</li> <li>angles at a point on a straight line and ½ a turn (total 180o)</li> <li>other multiples of 90o</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles</li> </ul>



**Geometry – Position and Direction**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Position, direction and movement	<ul style="list-style-type: none"> <li>Understand position through words alone – for example, “The bag is under the table,” – with no pointing.</li> <li>Describe a familiar route.</li> <li>Discuss routes and locations, using words like ‘in front of’ and ‘behind’.</li> </ul>	<ul style="list-style-type: none"> <li>Select, rotate and manipulate shapes to develop spatial reasoning skills. (DM)</li> </ul>	<ul style="list-style-type: none"> <li>describe position, direction and movement, including half, quarter and three-quarter turns.</li> </ul>	<ul style="list-style-type: none"> <li>use mathematical vocabulary to describe position, direction and movement including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise)</li> </ul>		<ul style="list-style-type: none"> <li>describe positions on a 2-D grid as coordinates in the first quadrant</li> <li>describe movements between positions as translations of a given unit to the left/right and up/down</li> <li>plot specified points and draw sides to complete a given polygon</li> </ul>	<ul style="list-style-type: none"> <li>identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed</li> </ul>	<ul style="list-style-type: none"> <li>describe positions on the full coordinate grid (all four quadrants)</li> <li>draw and translate simple shapes on the coordinate plane, and reflect them in the axes.</li> </ul>
Pattern	<ul style="list-style-type: none"> <li>Talk about and identify the patterns around them. For example: stripes on clothes, designs on rugs and wallpaper. Use informal language like ‘pointy’, ‘spotty’, ‘blobs’, etc.</li> <li>Extend and create ABAB patterns – stick, leaf, stick, leaf.</li> <li>Notice and correct an error in a repeating pattern.</li> </ul>	<ul style="list-style-type: none"> <li>Continue, copy and create repeating patterns. (DM)</li> </ul>		<ul style="list-style-type: none"> <li>order and arrange combinations of mathematical objects in patterns and sequences</li> </ul>				

**Statistics**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Interpreting, constructing and presenting data				<ul style="list-style-type: none"> <li>interpret and construct simple pictograms, tally charts, block diagrams and simple tables</li> <li>ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity</li> <li>ask and answer questions about totalling and comparing categorical data</li> </ul>	<ul style="list-style-type: none"> <li>interpret and present data using bar charts, pictograms and tables</li> </ul>	<ul style="list-style-type: none"> <li>interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs</li> </ul>	<ul style="list-style-type: none"> <li>complete, read and interpret information in tables, including timetables</li> </ul>	<ul style="list-style-type: none"> <li>interpret and construct pie charts and line graphs and use these to solve problems</li> </ul>
Solving Problems					<ul style="list-style-type: none"> <li>solve one-step and two-step questions [e.g. ‘How many more?’ and ‘How many fewer?’] using information presented in scaled bar charts and pictograms and tables.</li> </ul>	<ul style="list-style-type: none"> <li>solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs.</li> </ul>	<ul style="list-style-type: none"> <li>solve comparison, sum and difference problems using information presented in a line graph</li> </ul>	<ul style="list-style-type: none"> <li>calculate and interpret the mean as an average</li> </ul>



**Algebra**

	Early Years Foundation Stage		Key Stage 1		Lower Key Stage 2		Upper Key Stage 2	
	Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Equations			<ul style="list-style-type: none"> <li>solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as <math>7 = * - 9</math></li> </ul>	<ul style="list-style-type: none"> <li>recognise and use the inverse relationship between addition and subtraction and use this to check calculations and missing number problems.</li> </ul>	<ul style="list-style-type: none"> <li>solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction.</li> <li>solve problems, including missing number problems, involving multiplication and division, including integer scaling</li> </ul>		<ul style="list-style-type: none"> <li>use the properties of rectangles to deduce related facts and find missing lengths and angles</li> </ul>	<ul style="list-style-type: none"> <li>express missing number problems algebraically</li> <li>find pairs of numbers that satisfy number sentences involving two unknowns</li> <li>enumerate all possibilities of combinations of two variables</li> </ul>
Formulae						<ul style="list-style-type: none"> <li>Perimeter can be expressed algebraically as <math>2(a + b)</math> where a and b are the dimensions in the same unit.</li> </ul>		<ul style="list-style-type: none"> <li>use simple formulae</li> <li>recognise when it is possible to use formulae for area and volume of shapes</li> </ul>
Sequences			<ul style="list-style-type: none"> <li>sequence events in chronological order using language such as: before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening</li> </ul>	<ul style="list-style-type: none"> <li>compare and sequence intervals of time</li> <li>order and arrange combinations of mathematical objects in patterns</li> </ul>				<ul style="list-style-type: none"> <li>generate and describe linear number sequences</li> </ul>