## Mathematics Progression Map

This progression document aims to give guidance on the progression of Mathematics knowledge and skills across St. Joseph's Catholic Primary School. It can be used by teachers to differentiate work \& expectations appropriately for pupils working above and below age-related expectations. Pupils should also be encouraged to access mathematical problems presented in a wide range of different, complex ways, ask their own mathematical questions and follow their own lines of enquiry when exploring an open-ended maths problem. Pupils' use of mathematical language, fluency
in the fundamentals, reasoning mathematically following a line of enquiry and solving problem by applying their mathematical skills should be evident in their mathematics books'

## St Joseph's Mathematical Vision

~ A positive attitude to mathematics as an interesting and valuable subject;
~ A range of learning strategies: working both cooperatively, collaboratively and independently;
$\sim$ Confidence and competence with numbers and the number system;
~ Be able to explore features of shape and space, and develop measuring skills in a range of contexts;
~ An understanding of the importance of mathematics in everyday life;
~ To ensure pupils become fluent in the fundamentals of mathematics;
~ Develop conceptual knowledge and an ability to recall and apply knowledge rapidly and accurately;
~ Ensure that pupils can reason mathematically and solve problems;
~ For our children to develop a 'can do' attitude and perceive themselves as mathematicians.

## Key features of our Maths Mastery curriculum:

* High expectations for every child;
* Fewer topics, greater depth;
* Number sense and place value come first;
* Focus on mathematical thinking and language;
* Problem solving is central;
* Calculate with confidence-understand why it works.

|  |  | Mathemati | Progression | Map |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| EYFS | KS1 |  | KS2 |  |  |  |
| Number and Place Value |  |  |  |  |  |  |
| Counting |  |  |  |  |  |  |
| EYFS <br> Three and four year olds Reception ELG | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Recite numbers past 5. - Say one number name for each item in order: 1, 2, 3, 4, 5. $\cdot$ Know that the last number reached when counting a small set of objects tells you how many there are in total ('cardinal principle'). <br> Count objects, actions and sounds. Count beyond ten. Verbally count beyond 20, recognising the pattern of the counting system. | count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number |  |  | count backwards through zero to include negative numbers | interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero | use negative numbers in context, and calculate intervals across zero |
|  | count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens | count in steps of 2, 3, and 5 from 0 , and in tens from any number, forward or backward | count from 0 in multiples of $4,8,50$ and 100; | count in multiples of $6,7,9,25$ and 1 000 | count forwards or backwards in steps of powers of 10 for any given number up to 1 000000 |  |
|  | given a number, identify one more and one less |  |  |  |  |  |


| Compare quantities using language: 'more than', 'fewer than'. <br> Compare numbers. <br> Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity. | use the language of: equal to, more than, less than (fewer), most, least | compare and order numbers from 0 up to 100 ; use <, > and = signs | compare and order numbers up to 1000 | order and compare numbers beyond 1 000 | read, write, order and compare numbers to at least 1 000000 and determine the value of each digit (appears also in Reading and Writing Numbers) | read, write, order and compare numbers up to 10000000 and determine the value of each digit (appears also in Reading and Writing Numbers) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | compare numbers with the same number of decimal places up to two decimal places (Also in fractions) |  |  |
| Identifying, Representing and Estimating Numbers |  |  |  |  |  |  |
| Develop fast recognition of up to 3 objects, without having to count them individually ('subitising'). Show 'finger numbers' up to 5. Link numerals and amounts: for example, showing the right number of objects to match the numeral, up to 5. | identify and represent numbers using objects and pictorial representations including the number line | identify, represent and estimate numbers using different representations, including the number line | identify, represent and estimate numbers using different representations | identify, represent and estimate numbers using different representations |  |  |


| Experiment with their own <br> symbols and marks as well as <br> numerals. |  |  |  |  |
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| Subitise. <br> Link the number symbol (numeral) with its cardinal number value. <br> Subitise (recognising quantities without counting) up to 5 . |  |  |  |  |  |  |
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|  | Reading and Writing Numbers (including Roman Numerals) |  |  |  |  |  |
| Link numerals and amounts: for example, showing the right number of objects to match the numeral, up to 5 . <br> Experiment with their own symbols and marks as well as numerals. <br> Link the number symbol (numeral) with its cardinal number value. | read and write numbers from 1 to 20 in numerals and words. | read and write numbers to at least 100 in numerals and in words | read and write numbers up to 1000 in numerals and in words <br> tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks (Also in Measurement) | read Roman numerals to 100 (I to C ) and know that over time, the numeral system changed to include the concept of zero and place value. | read, write, order and compare numbers to at least 1 000000 and determine the value of each digit (appears also in Comparing Numbers) read Roman numerals to 1000 (M) and recognise years written in Roman numerals. | read, write, order and compare numbers up to 10000000 and determine the value of each digit (appears also in Understanding Place Value |


| Understand the 'one more than/one less than' relationship between consecutive numbers. Explore the composition of numbers to 10. <br> Have a deep understanding of numbers to 10 , including the composition of each number. |  | recognise the place value of each digit in a two-digit number (tens, ones) | recognise the place value of each digit in a three-digit number (hundreds, tens, ones) | recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) find the effect of dividing a one- or two-digit number | read, write, order and compare numbers to at least 1 000000 and determine the value of each digit (appears also in Reading and Writing Numbers) | read, write, order and compare numbers up to 10000000 and determine the value of each digit (appears also in Reading and Writing Numbers) <br> identify the value of |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |



|  |  |  | round decimals with one decimal place to the nearest whole number (copied from Fractions) | round decimals with two decimal places to the nearest whole number and to one decimal place (copied from Fractions) | solve problems which require answers to be rounded to specified degrees of accuracy (copied from Fractions) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Problem Solving |  |  |  |  |  |
| Solve real world mathematical problems with numbers up to 5 . | use place value and number facts to solve problems | solve number problems and practical problems involving these ideas. | solve number and practical problems that involve all of the above and with increasingly large positive numbers | solve number problems and practical problems that involve all of the above | solve number and practical problems that involve all of the above |

## Number: Addition and Subtraction





| Problem Solving |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed evenly. | solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = 9 | solve problems with addition and subtraction: <br> using concrete <br> objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change (copied from Measurement) | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | solve addition and subtraction twostep problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multistep problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why <br> Solve problems involving addition, subtraction, multiplication and division |
| Number: Multiplication and Division |  |  |  |  |  |  |
| Multiplication and Division |  |  |  |  |  |  |
|  | count in multiples of twos, fives and tens (copied from Number and Place Value) | count in steps of 2, 3, and 5 from 0 , and in tens from any number, forward or backward (copied from Number and Place Value) | count from 0 in multiples of 4, 8, 50 and 100 (copied from Number and Place Value) | count in multiples of 6, 7, 9, 25 and 1 000 (copied from Number and Place Value) | count forwards or backwards in steps of powers of 10 for any given number up to 1000000 (copied from Number and Place Value) |  |




| Written Calculation |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication ( $\times$ ), division ( $\div$ ) and equals (=) signs | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times onedigit numbers, using mental and progressing to formal written methods (appears also in Mental Methods) | multiply two-digit and three-digit numbers by a onedigit number using formal written layout | multiply numbers up to 4 digits by a oneor two-digit number using a formal written method, including long multiplication for two-digit numbers | multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication |



| Properties of numbers: prime, square, cube, factors and multiples. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | recognise and use factor pairs and commutativity in mental calculations (repeated) | identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers. <br> know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers <br> establish whether a number up to 100 is prime and recall prime numbers up to 19 | identify common factors, common multiples and prime numbers <br> use common factors to simplify fractions; use common multiples to express fractions in the same denomination (copied from Fractions) |
|  |  |  | recognise and use square numbers and cube numbers, and the notation for 2squared () and cubed 3 () | calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm3) and cubic metres (m3), and extending to other units such as mm3 and km3 <br> (copied from Measures) |



|  |  |  |  | objects are connected to m objects | combination of these, including understanding the meaning of the equals sign solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ratio and Proportion |  |  |  |  |  |  |
|  |  |  |  |  |  | solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts |
|  |  |  |  |  |  | solve problems involving the calculation of percentages [for example, of measures, and such as $15 \%$ of 360 ] and the use of percentages for comparison |
|  |  |  |  |  |  | solve problems involving similar shapes where the scale factor is known or can be found |


| Measurement |  | solve problems involving <br> unequal sharing and <br> grouping using <br> knowledge of fractions <br> and multiples. |
| :---: | :---: | :---: | :---: | :--- |

## Comparing and Estimating

| Make comparisons between objects relating to size, length, weight and capacity. <br> Compare length, weight and capacity. | compare, describe and solve practical problems for: <br> * lengths and heights [e.g. long/short, longer/shorter, tall/short, double/half] <br> * mass/weight [e.g. heavy/light, heavier than, lighter than] <br> * capacity and volume [e.g. full/empty, more than, less than, half, half full, quarter] <br> time [e.g. quicker, slower, earlier, later] | compare and order lengths, mass, volume/capacity and record the results using $>$, < and = |  | estimate, compare and calculate different measures, including money in pounds and pence (also included in Measuring | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm2) and square metres (m2) and estimate the area of irregular shapes (also included in measuring) estimate volume (e.g. using 1 cm3 blocks to build cubes and cuboids) and capacity (e.g. using water) | calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm3) and cubic metres (m3), and extending to other units such as mm3 and km3. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |


|  | sequence events in <br> chronological order <br> using language <br> [e.g. | compare and sequence <br> intervals of time | compare durations of <br> events, for example to <br> calculate the time |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



## Measuring and Calculating

|  | measure and begin to record the following: <br> * lengths and heights <br> * mass/weight <br> * capacity and volume <br> * time (hours, minutes, seconds) | choose and use appropriate standard units to estimate and measure length/height in any direction ( $\mathrm{m} / \mathrm{cm}$ ); mass (kg/g); temperature ( ${ }^{\circ} \mathrm{C}$ ); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels | measure, compare, add and subtract: lengths ( $\mathrm{m} / \mathrm{cm} / \mathrm{mm}$ ); mass (kg/g); volume/capacity ( $1 / \mathrm{ml}$ ) | estimate, compare and calculate different measures, including money in pounds and pence (appears also in Comparing) | use all four operations to solve problems involving measure (e.g. length, mass, volume, money) using decimal notation including scaling. | solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate (appears also in Converting) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | measure the perimeter of simple 2 D shapes | measure and calculate the perimeter of a | measure and calculate the perimeter of | recognise that shapes with the same areas can have different |


|  |  |  | rectilinear figure <br> (including squares) <br> in centimetres and <br> metres | composite rectilinear <br> shapes in <br> centimetres and <br> metres |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| versa |  |  |  |  |


|  | recognise and know the value of different denominations of coins and notes | recognise and use symbols for pounds ( $£$ ) and pence (p); combine amounts to make a particular value <br> find different combinations of coins that equal the same amounts of money <br> solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change | add and subtract amounts of money to give change, using both $£$ and $p$ in practical contexts |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | find the area of rectilinear shapes by counting squares | calculate and compare the area of squares and rectangles including using standard units, square centimetres <br> 2 <br> (cm ) and square <br> 2 metres (m ) and estimate the area of irregular shapes <br> recognise and use square numbers and cube numbers, and the notation for | calculate the area of parallelograms and triangles calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) and cubic metres (m3), and extending to other units [e.g. mm3 and km3]. recognise when it is possible to use formulae |


|  |  |  |  |  | 2squared () and cubed 3 () (copied from Multiplication and Division) | for area and volume of shapes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Telling the Time |  |  |  |  |  |  |
| Begin to describe a sequence of events, real or fictional, using words, such as 'first', 'then...' | tell the time to the hour and half past the hour and draw the hands on a clock face to show these times | tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times. | tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks | read, write and convert time between analogue and digital 12 and 24-hour clocks (appears also in Converting) |  |  |
|  | recognise and use language relating to dates, including days of the week, weeks, months and years | know the number of minutes in an hour and the number of hours in a day. <br> (appears also in Converting) | estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o'clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight (appears also in Comparing and Estimating) |  |  |  |


|  |  |  | solve problems involving converting from hours to minutes; minutes to seconds; years to | solve problems involving converting between units of time |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | months; weeks to days <br> (appears also in Converting) |  |  |
| Converting |  |  |  |  |  |
|  | know the number of minutes in an hour and the number of hours in a day. <br> (appears also in Telling the Time) | know the number of seconds in a minute and the number of days in each month, year and leap year | convert between different units of measure (e.g. kilometre to metre; hour to minute) | convert between different units of metric measure (e.g. kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) |  |
|  |  |  | read, write and convert time between analogue and digital 12 and 24-hour clocks (appears also in Converting) | solve problems involving converting between units of time | solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate (appears also in <br> Measuring and Calculating) |


|  |  |  | understand and use <br> solve problems <br> involving converting <br> from hours to <br> equalences <br> between metric units <br> and kilometres miles <br> minutes; minutes to <br> and common <br> imperial units such as <br> seconds; years to <br> months; weeks to <br> inches, pounds and <br> days <br> (appears also in <br> Telling the Time) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



## Pattern

| Talk about and identify the patterns around them. For example, stripes on clothes, designs on rugs and wallpaper. Use informal language like 'pointy', 'spotty', 'blobs', etc. Extend and create ABAB patterns - stick, leaf, stick, leaf. Notice and correct an error in a repeating pattern. <br> Continue, copy and create repeating patterns. | order and arrange combinations of mathematical objects in patterns and sequences |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |



## Drawing and Constructing



|  |  |  | distinguish between <br> regular and irregular <br> polygons based on <br> reasoning about <br> equal sides and <br> angles |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


Fractions (including decimals and percentages
Counting in fractional steps

| Pupils should count in <br> fractions up to 10, | count up and down in <br> tenths | count up and down <br> in hundredths |
| :--- | :--- | :--- |





|  |  |  | recognise and write decimal equivalents $1 \quad 1 \quad 3$ <br> to / ; / ; <br> $\begin{array}{lll}4 & 2 & 4\end{array}$ | recognise the per cent symbol (\%) and understand that per cent relates to "number of parts per hundred", and write percentages as a fraction with denominator 100 as a decimal fraction | recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Addition and subtraction of fractions |  |  |  |  |  |
|  |  | add and subtract fractions with the same denominator within one whole (e.g. $5 \quad 1 \quad 6$ $/+/=/ 1$ | add and subtract fractions with the same denominator | add and subtract fractions with the same denominator and multiples of the same number | add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions |
|  |  |  |  | recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number (e.g. 2 / + / = / = $1 /$ ) $\begin{array}{llll}5 & 5 & 5 & 5\end{array}$ |  |


|  |  |  |  |  | multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams | multiply simple pairs of proper fractions, writing the answer in its $\begin{aligned} & \text { simplest form (e.g. }{ }_{4}^{1} \times \\ & \underbrace{1}_{4}=/_{8}^{1} \\ & 2 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  |  |  |  | divide proper fractions by whole numbers (e.g. ${\underset{3}{1} / \div 2=/)_{6}^{1}}^{1}$ |

## Multiplication and division of decimals

|  |  |  |  |  |  |
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|  |  |  |  | find the effect of <br> dividing a one- or <br> two-digit number <br> by 10 and 100, <br> identifying the <br> value of the digits in <br> the answer as ones, <br> tenths and <br> numbers by divide 100 and <br> 1000 where the answers <br> are up to three decimal <br> places |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |



|  |  |  | solve problems that involve all of the above | solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | solve problems involving numbers up to three decimal places |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | solve simple measure and money problems involving fractions and | solve problems which require knowing percentage |  |  |



| Experiment with their own symbols and marks, as well as numerals. | interpret and construct simple pictograms, tally charts, block diagrams and simple tables | interpret and present data using bar charts, pictograms and tables | interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs | complete, read and interpret information in tables, including timetables | interpret and construct pie charts and line graphs and use these to solve problems |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity |  |  |  |  |
|  | ask and answer questions about totalling and comparing categorical data |  |  |  |  |


|  |  |  | solve one-step and two-step questions [e.g. 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables. | solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs. | solve comparison, sum and difference problems using information presented in a line graph | calculate and interpret the mean as an average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Algebra |  |  |  |  |  |  |
| Equations |  |  |  |  |  |  |
|  | involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = 9 <br> (copied from Addition and Subtraction) | recognise and use the inverse relationship between addition and subtraction and use this to check calculations and missing number problems. (copied from Addition and Subtraction) | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction. (copied from Addition and Subtraction) |  | use the properties of rectangles to deduce related facts and find missing lengths and angles (copied from Geometry: Properties of Shapes) | express missing number problems algebraically |






