ST. MATTHEW'S C.E. PRIMARY SCHOOL & NURSERY



LOWER KEY STAGE 2 MATHS CALCULATION POLICY

Reviewed: September 2021

By: Mrs Bryden

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Mission Statement:

St. Matthew's C.E. Primary School and Nursery is dedicated to providing an education which enables every child to fulfil their best potential. It seeks to promote academic, emotional and spiritual growth in a Christian environment, welcoming children drawn from diverse cultures.

Vision Statement:

Inspired by Jesus' words (Matthew 5: 1-12), we strive to promote academic, emotional and spiritual growth in a Christian environment for all members of our school family.

We can all 'Be blessed by God, be happy and aspire to be...'

Calculation policy, LKS2

The following pages show the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns.

By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2. **Multiplication and division:** Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35.

Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively.

Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.

Children develop column methods to support multiplications in these cases.

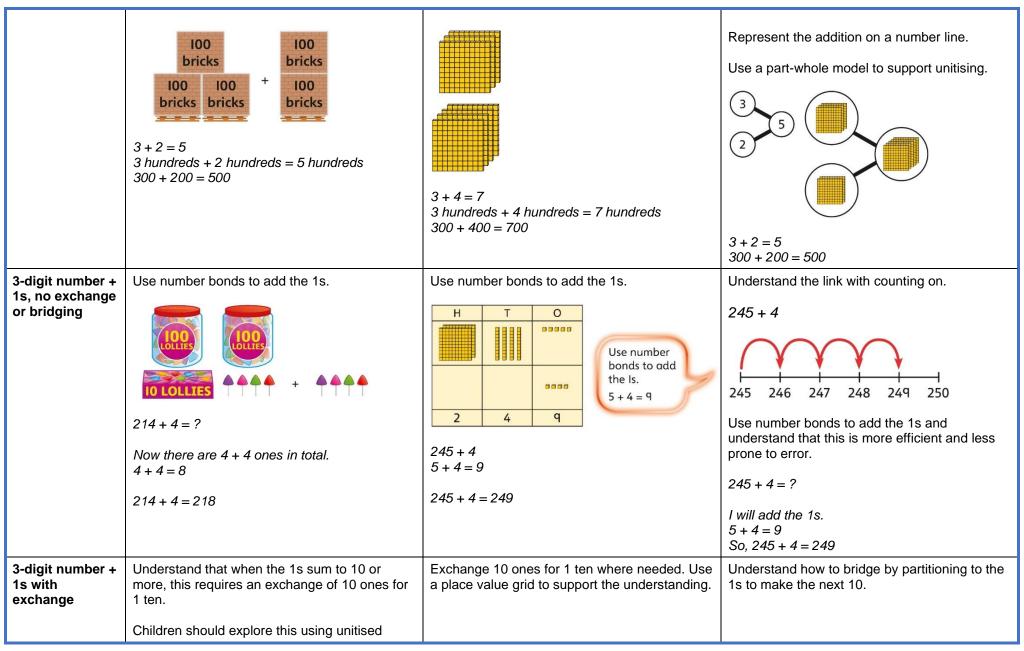
For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

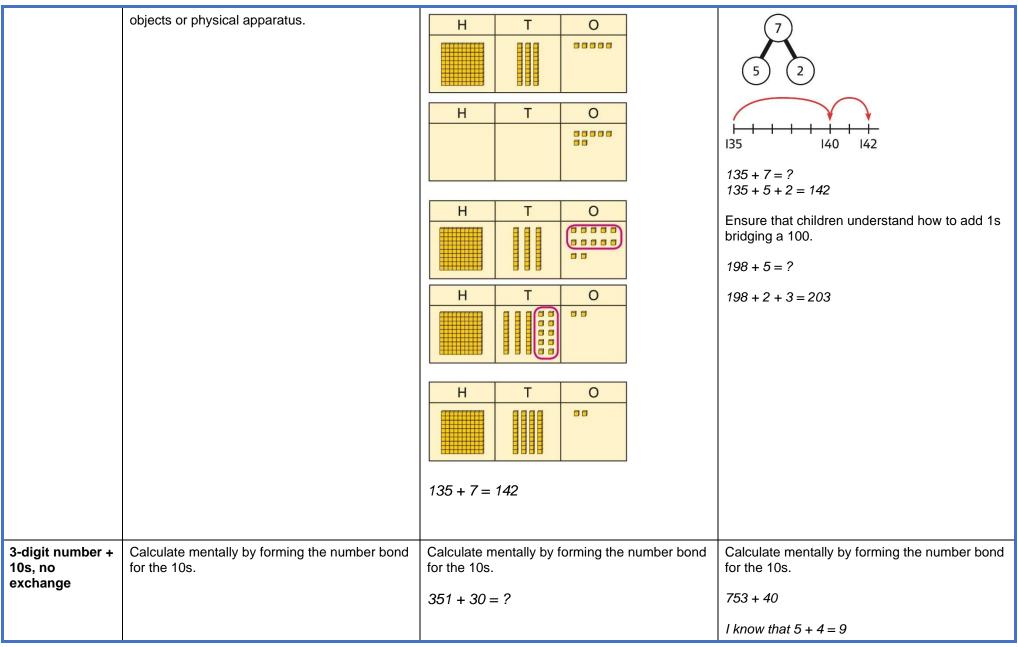
Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

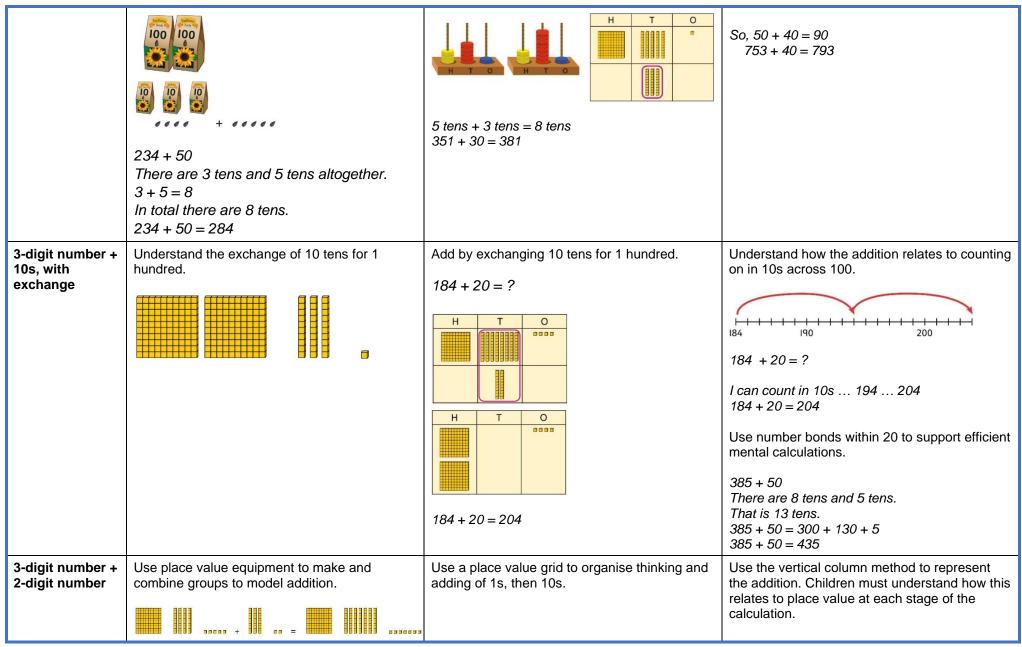
in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.

		Year 3	
	Concrete	Pictorial	Abstract
Year 3 Addition			
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens. Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use a place value grid to support the structure of numbers to 1,000. Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.	Represent the parts of numbers to 1,000 using a part-whole model. $ 215 $ $ 200 $ $ 10 $ $ 5 $ Recognise numbers to 1,000 represented on a number line, including those between intervals.
Adding 100s	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.







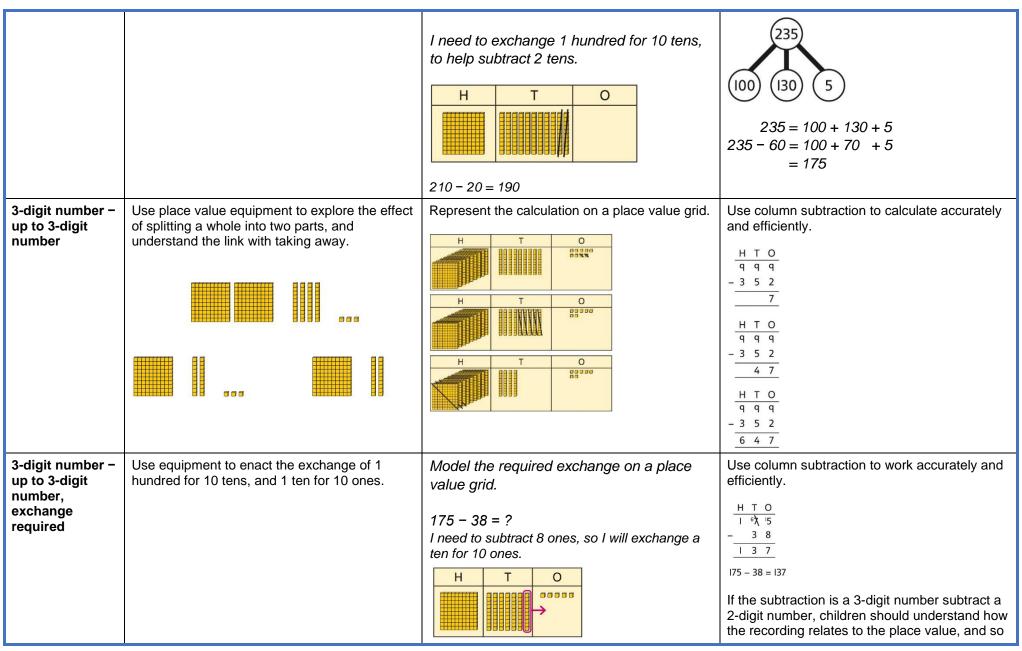
3-digit number + 2-digit number, exchange required	Use place value equipment to model addition and understand where exchange is required. Use place value counters to represent 154 + 72. Use this to decide if any exchange is required. There are 5 tens and 7 tens. That is 12 tens so I will exchange.	Represent the required exchange on a place value grid using equipment. 275 + 16 = ? H T O H T O 275 + 16 = 291 Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value. Children should be encouraged at every stage to select methods that are accurate and efficient.	Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation. HTO TO TO TO TO TO TO TO TO T
3-digit number + 3-digit number, no exchange	Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid. 326 + 541 is represented as:	Represent the place value grid with equipment to model the stages of column addition.	Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.

3-digit number + 3-digit number, exchange required	Use place value equipment to enact the exchange required. H T O S S S S S S S S S S S S S S S S S S	Model the stages of column addition using place value equipment on a place value grid. H T O H	Use column addition, ensuring understanding of place value at every stage of the calculation. $ \frac{H T O}{126} + \frac{T O}{217} $ $ \frac{H T O}{126} + \frac{12}{217} $ $ \frac{H T O}{126} + \frac{12}{217} $ $ \frac{H T O}{126} + \frac{12}{217} $ $ \frac{126 + 217 = 343}{343} $ Note: Children should also study examples where exchange is required in more than one solvers for example 405 + 210 + 240 +	
Representing addition	Encourage children to use their own drawings and choices of place value equipment to	Children understand and create bar models to represent addition problems.	column, for example 185 + 318 = ? Use representations to support choices of appropriate methods.	
problems, and selecting appropriate methods	represent problems with one or more steps. These representations will help them to select appropriate methods.	275 + 99 = ? 374 275 qq	I will add 100, then subtract 1 to find the solution.	
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	275 + 99 = 374	128 + 105 + 83 = ? I need to add three numbers.
		128 + 105 = 233
		233 1 128 105 83
		233 83
		,

Subtracting			
100s	Use known facts and unitising to subtract multiples of 100. 100 bricks 100 bricks 5 - 2 = 3 500 - 200 = 300	Use known facts and unitising to subtract multiples of 100. $4-2=2$ $400-200=200$	Understand the link with counting back in 100s. $ \begin{array}{cccccccccccccccccccccccccccccccccc$
3-digit number – 1s, no exchange	Use number bonds to subtract the 1s. $214 - 3 = ?$ 100	Use number bonds to subtract the 1s. H T O 319 - 4 = ? H T O 319 - 4 = ? 9 - 4 = 5 319 - 4 = 315	Understand the link with counting back using a number line. Use known number bonds to calculate mentally. $476 - 4 = ?$ 476 400 70 6 $6 - 4 = 2$ $476 - 4 = 472$
3-digit number – 1s, exchange or bridging	Understand why an exchange is necessary by exploring why 1 ten must be exchanged.	Represent the required exchange on a place value grid.	Calculate mentally by using known bonds. $151 - 6 = ?$

required	Use place value equipment.	151 - 6 = ?	
			151 - 1 - 5 = 145
		H T O	
		H T O	
		XXXXX	
3-digit number – 10s, no	Subtract the 10s using known bonds.	Subtract the 10s using known bonds.	Use known bonds to subtract the 10s mentally.
exchange	1 4 1	H T O	<i>372</i> − <i>50</i> = ?
			70 - 50 = 20
	HTO		So, 372 - 50 = 322
	381 - 10 = ?	8 tens - 1 ten = 7 tens 381 - 10 = 371	
	8 tens with 1 removed is 7 tens.		
	381 - 10 = 371		
3-digit number – 10s, exchange or bridging	Use equipment to understand the exchange of 1 hundred for 10 tens.	Represent the exchange on a place value grid using equipment.	Understand the link with counting back on a number line.
required		210 - 20 = ?	Use flexible partitioning to support the calculation.
		H T O	235 - 60 = ?



	H T O H T O SSSSSS NNNNNNNNNNNNNNNNNNNNNNNNNNNNN	how to line up the digits correctly. Children should also understand how to exchange in calculations where there is a zero in the 10s column. H T 0
Representing subtraction problems	Use bar models to represent subtractions. 'Find the difference' is represented as two bars for comparison. Team A 454 Team B 128 ? Bar models can also be used to show that a part must be taken away from the whole.	Children use alternative representations to check calculations and choose efficient methods. Children use inverse operations to check additions and subtractions. The part-whole model supports understanding. I have completed this subtraction. 525 - 270 = 255 I will check using addition. H T O

Year 3 Multiplication			
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non-examples using objects. Children recognise that arrays can be used to model commutative multiplications. I can see 3 groups of 8. I can see 8 groups of 3.	Children recognise that arrays demonstrate commutativity. This is 3 groups of 4. This is 4 groups of 3.	Children understand the link between repeated addition and multiplication. $ \begin{array}{cccccccccccccccccccccccccccccccccc$
Using commutativity to support understanding of the timestables	Understand how to use times-tables facts flexibly.	Understand how times-table facts relate to commutativity.	Understand how times-table facts relate to commutativity. I need to work out 4 groups of 7. I know that 7 × 4 = 28 so, I know that 4 groups of 7 = 28

	There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls. I can use $6 \times 4 = 24$ to work out both totals.	4 × 6 = 24	and 7 groups of 4 = 28.
Understanding and using ×3, ×2, ×4 and ×8 tables.	Children learn the times-tables as 'groups of', but apply their knowledge of commutativity. I can use the ×3 table to work out how many keys. I can also use the ×3 table to work out how many batteries.	Children understand how the $\times 2$, $\times 4$ and $\times 8$ tables are related through repeated doubling.	Children understand the relationship between related multiplication and division facts in known times-tables. $2 \times 5 = 10$ $5 \times 2 = 10$ $10 \div 5 = 2$ $10 \div 2 = 5$
Using known facts to multiply 10s, for example 3 x 40	Explore the relationship between known timestables and multiples of 10 using place value equipment. Make 4 groups of 3 ones. Make 4 groups of 3 tens.	Understand how unitising 10s supports multiplying by multiples of 10.	Understand how to use known times-tables to multiply multiples of 10. +2 +2 +2 +2 +2 +2 +2 +2 +2 +2 +2 +2 +2 +

	What is the same? What is different?	10 10 10 10 10 4 groups of 2 ones is 8 ones. 4 groups of 2 tens is 8 tens. $4 \times 2 = 8$ $4 \times 20 = 80$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Multiplying a 2-digit number by a 1-digit number number	Understand how to link partitioning a 2-digit number with multiplying. Each person has 23 flowers. Each person has 2 tens and 3 ones. There are 3 groups of 2 tens. There are 3 groups of 3 ones. Use place value equipment to model the multiplication context.	Use place value to support how partitioning is linked with multiplying by a 2-digit number. $3 \times 24 = ?$ T O 3 × 4 = 12 T O 3 × 4 = 12 $3 \times 20 = 60$ $60 + 12 = 72$	Use addition to complete multiplications of 2-digit numbers by a 1-digit number. $4 \times 13 = ?$ $4 \times 3 = 12$ $4 \times 10 = 40$ $12 + 40 = 52$ $4 \times 13 = 52$

	T O There are 3 groups of 3 ones. There are 3 groups of 2 tens.	3 × 24 = 72	
Multiplying a 2-digit number by a 1-digit number, expanded column method	Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications. $3 \times 24 = ?$ $3 \times 20 = 60$ $3 \times 4 = 12$ $3 \times 24 = 60 + 12$ $3 \times 24 = 70 + 2$ $3 \times 24 = 72$	Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s. $4 \times 23 = ?$ T O $4 \times 23 = 92$	Children may write calculations in expanded column form, but must understand the link with place value and exchange. Children are encouraged to write the expanded parts of the calculation separately. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

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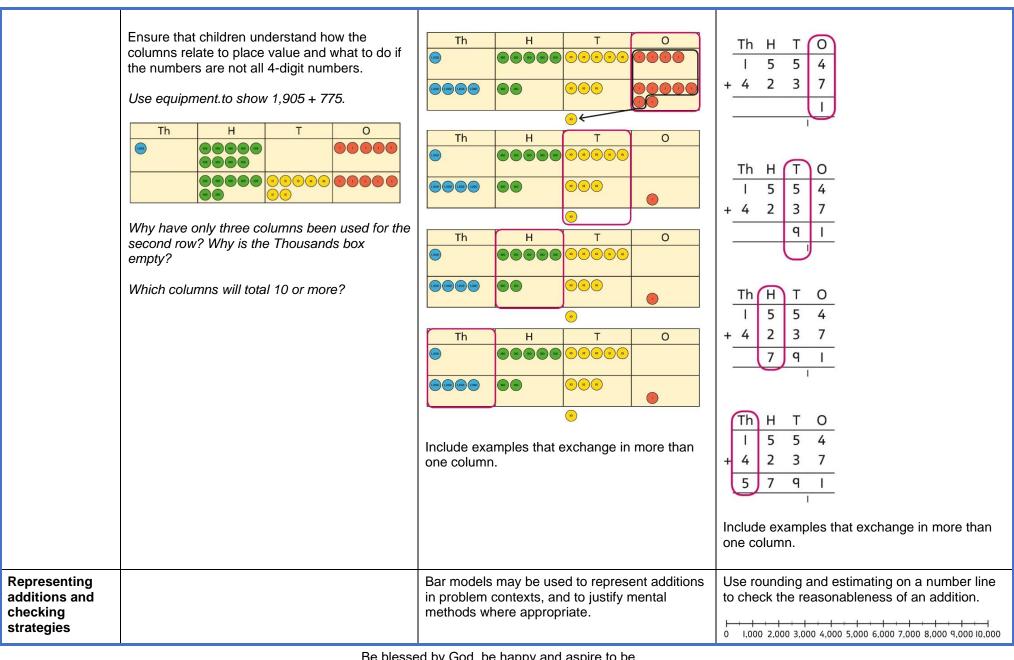
	T O	
	$5 \times 20 = 100$ $5 \times 23 = 115$	

Year 3 Division			
Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions. 24 divided into groups of 8. There are 3 groups of 8.	Use knowledge of known times-tables to calculate divisions.	Use knowledge of known times-tables to calculate divisions. I need to work out 30 shared between 5. I know that $6 \times 5 = 30$ so I know that $30 \div 5 = 6$. A bar model may represent the relationship between sharing and grouping. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.	Use images to explain remainders.	Understand that the remainder is what cannot be shared equally from a set.

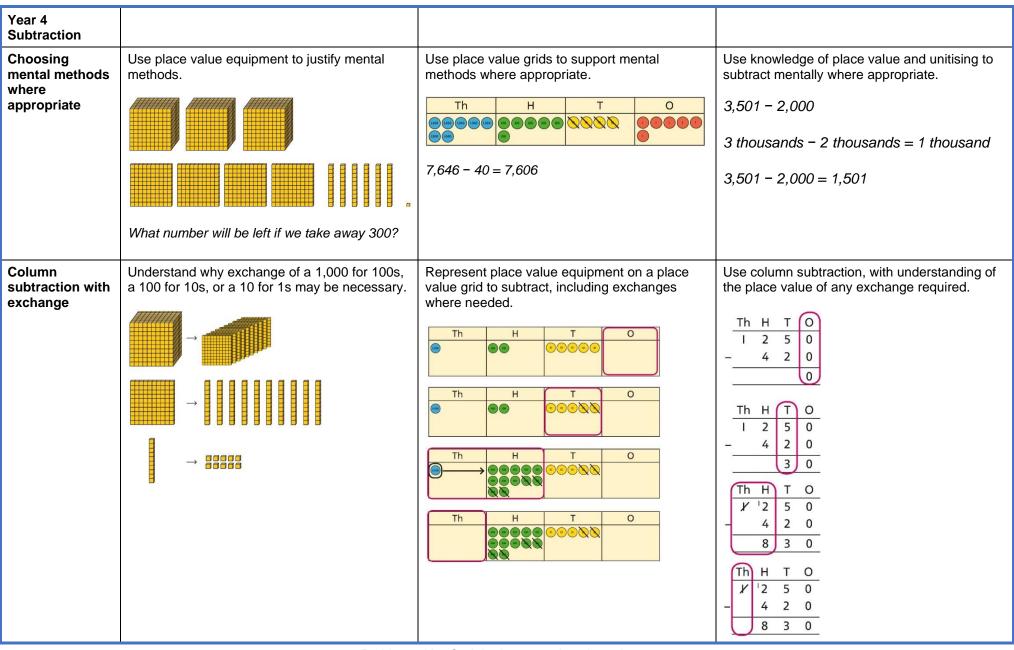
	ı	I	
		••••	22 ÷ 5 = ?
		00000	3 × 5 = 15
		00000	$4 \times 5 = 20$
	There are 13 sticks in total.		$5 \times 5 = 25 \dots$ this is larger than 22
	There are 3 groups of 4, with 1 remainder.	22 ÷ 5 = 4 remainder 2	So, 22 ÷ 5 = 4 remainder 2
Using known facts to divide	Use place value equipment to understand how to divide by unitising.	Divide multiples of 10 by unitising.	Divide multiples of 10 by a single digit using known times-tables.
multiples of 10	Make 6 ones divided by 3.		180 ÷ 3 = ?
			180 is 18 tens.
	Now make 6 tens divided by 3.	10 (18 divided by 3 is 6.
		12 tens shared into 3 equal groups. 4 tens in each group.	18 tens divided by 3 is 6 tens.
		4 tens in each group.	·
			18 ÷ 3 = 6
			180 ÷ 3 = 60
	What is the same? What is different?		
2-digit number divided by	Children explore dividing 2-digit numbers by using place value equipment.	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate.
1-digit number, no remainders			
		42	68
			$\langle \rangle$
		(40) (2)	(60) (8)
		0.0	
	48 ÷ 2 = ?	CHICAGO	$60 \div 2 = 30$ $8 \div 2 = 4$
	40 - 2 - :		30 + 4 = 34
			68 ÷ 2 = 34
	First divide the 10s.	I need to partition 42 differently to divide by 3.	Children partition flexibly to divide where appropriate.
			42 ÷ 3 = ?
			42 = 40 + 2

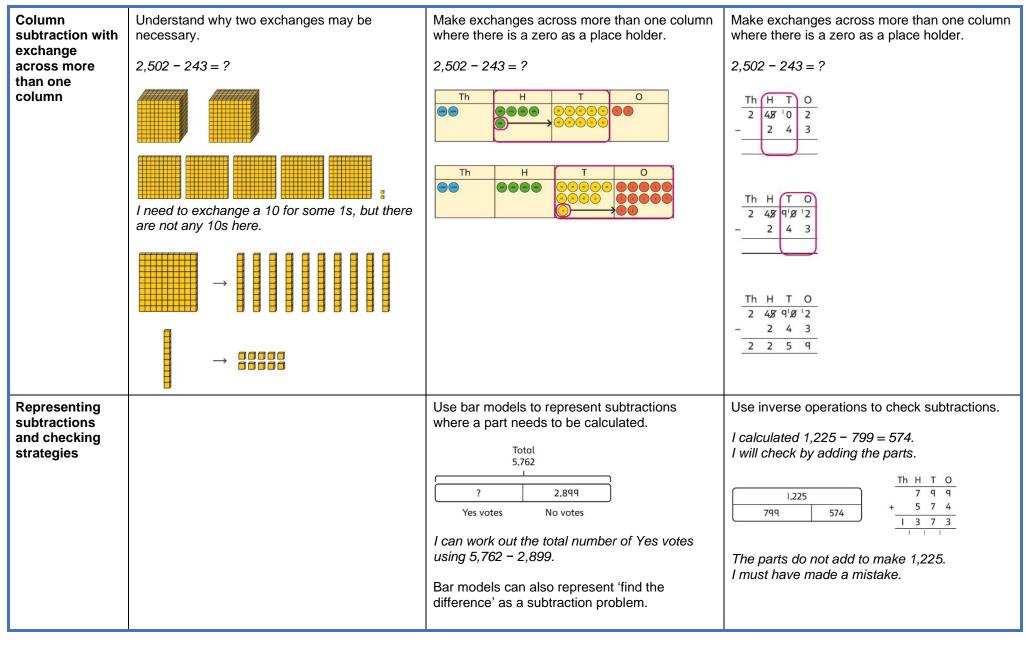
	Then divide the 1s.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	I need to partition 42 differently to divide by 3. $42 = 30 + 12$ $30 \div 3 = 10$ $12 \div 3 = 4$ $10 + 4 = 14$ $42 \div 3 = 14$
2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder. Make 29 from place value equipment. Share it into 2 equal groups. There are two groups of 14 and 1 remainder.	Use place value equipment to understand the concept of remainder in division. $29 \div 2 = ?$ $29 \div 2 = 14 \text{ remainder } 1$	Partition to divide, understanding the remainder in context. 67 children try to make 5 equal lines. 67 = 50 + 17 50 ÷ 5 = 10 17 ÷ 5 = 3 remainder 2 67 ÷ 5 = 13 remainder 2 There are 13 children in each line and 2 children left out.

	Year 4				
	Concrete	Pictorial	Abstract		
Year 4 Addition					
Understanding numbers to 10,000	Use place value equipment to understand the place value of 4-digit numbers. 4 thousands equal 4,000. 1 thousand is 10 hundreds.	Represent numbers using place value counters once children understand the relationship between 1,000s and 100s. 2,000 + 500 + $40 + 2 = 2,542$	Understand partitioning of 4-digit numbers, including numbers with digits of 0. $5,000 + 60 + 8 = 5,068$ Understand and read 4-digit numbers on a number line.		
Choosing mental methods where	Use unitising and known facts to support mental calculations.	Use unitising and known facts to support mental calculations.	Use unitising and known facts to support mental calculations.		
appropriate	Make 1,405 from place value equipment. Add 2,000. Now add the 1,000s. 1 thousand + 2 thousands = 3 thousands 1,405 + 2,000 = 3,405	I can add the 100s mentally. 200 + 300 = 500 So, 4,256 + 300 = 4,556	4,256 + 300 = ? $2 + 3 = 5$ $200 + 300 = 500$ $4,256 + 300 = 4,556$		
Column addition with exchange	Use place value equipment on a place value grid to organise thinking.	Use place value equipment to model required exchanges.	Use a column method to add, including exchanges.		



	1,373 799 574 + 5 7 4 1 3 7 3	912 + 6,149 = ? I used rounding to work out that the answer should be approximately 1,000 + 6,000 = 7,000.
	I chose to work out 574 + 800, then subtract 1. 6,000 2,999 3,001	
	This is equivalent to 3,000 + 3,000.	





	Danny	

Year 4 Multiplication			
Multiplying by multiples of 10 and 100	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100. 3 groups of 4 ones is 12 ones. 3 groups of 4 tens is 12 tens. 3 groups of 4 hundreds is 12 hundreds.	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100. $3 \times 4 = 12$ $3 \times 40 = 120$ $3 \times 400 = 1,200$	Use known facts and understanding of place value and commutativity to multiply mentally. $4 \times 7 = 28$ $4 \times 70 = 280$ $40 \times 7 = 280$ $4 \times 700 = 2,800$ $400 \times 7 = 2,800$
Understanding times-tables up to 12 x 12	Understand the special cases of multiplying by 1 and 0. $5 \times 1 = 5$ $5 \times 0 = 0$	Represent the relationship between the $\times 9$ table and the $\times 10$ table. Represent the $\times 11$ table and $\times 12$ tables in relation to the $\times 10$ table. $2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 11 = 40 + 4$	Understand how times-tables relate to counting patterns. Understand links between the $\times 3$ table, $\times 6$ table and $\times 9$ table 5×6 is double 5×3 $\times 5$ table and $\times 6$ table 1 know that $7 \times 5 = 35$ so 1 know that $7 \times 6 = 35 + 7$. $\times 5$ table and $\times 7$ table $3 \times 7 = 3 \times 5 + 3 \times 2$ $3 \times 5 \times $
Understanding and using	Make multiplications by partitioning.	Understand how multiplication and partitioning are related through addition.	Use partitioning to multiply 2-digit numbers by a single digit.

partitioning in multiplication	4 x 12 is 4 groups of 10 and 4 groups of 2. 4 x 12 = 40 + 8	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
Column multiplication for 2- and 3-digit numbers multiplied by a single digit	Use place value equipment to make multiplications. Make 4 × 136 using equipment. Make 4 × 136 using equipment. I can work out how many 1s, 10s and 100s. There are 4 × 6 ones 24 ones There are 4 × 3 tens 12 tens There are 4 × 1 hundreds 4 hundreds 24 + 120 + 400 = 544	Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit. 3 1 2	Use the formal column method for up to 3-digit numbers multiplied by a single digit. $ \begin{array}{c cccc} 3 & 1 & 2 \\ \times & & 3 \\ \hline \hline & 9 & 3 & 6 \end{array} $ Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation. $ \begin{array}{c ccccc} 2 & 3 \\ \hline \times & 5 \\ \hline 1 & 5 \\ \hline 1 & 0 & 0 \\ \hline \hline 1 & 1 & 5 \\ \hline \end{array} $ $ \begin{array}{c ccccc} & 2 & 3 \\ \hline & 1 & 5 \\ \hline & 1 & 1 & 5 \\ \hline & 1 & 1 & 5 \\ \hline & 1 & 1 & 5 \\ \hline \end{array} $
Multiplying more than two numbers	Represent situations by multiplying three numbers together.	Understand that commutativity can be used to multiply in different orders.	Use knowledge of factors to simplify some multiplications. $24 \times 5 = 12 \times 2 \times 5$



Each sheet has 2 x 5 stickers. There are 3 sheets.

There are $5 \times 2 \times 3$ stickers in total.

$$5 \times 2 \times 3 = 30$$
$$10 \times 3 = 30$$

$$2 \times 6 \times 10 = 120$$

 $12 \times 10 = 120$

$$10 \times 6 \times 2 = 120$$

 $60 \times 2 = 120$

$$12 \times 2 \times 5 =$$
 $12 \times 10 = 120$
 $12 \times 10 = 120$

Year 4 Division			
Understanding the relationship between multiplication and division, including times- tables	Use objects to explore families of multiplication and division facts.	Represent divisions using an array.	Understand families of related multiplication and division facts. I know that 5 × 7 = 35 so I know all these facts:
	 4 x 6 = 24 24 is 6 groups of 4. 24 is 4 groups of 6. 24 divided by 6 is 4. 24 divided by 4 is 6. 	28 ÷ 7 = 4	$5 \times 7 = 35$ $7 \times 5 = 35$ $35 = 5 \times 7$ $35 = 7 \times 5$ $35 \div 5 = 7$ $35 \div 7 = 5$ $7 = 35 \div 5$ $5 = 35 \div 7$
Dividing multiples of 10 and 100 by a single digit	Use place value equipment to understand how to use unitising to divide. 8 ones divided into 2 equal groups 4 ones in each group 8 tens divided into 2 equal groups 4 tens in each group 8 hundreds divided into 2 equal groups 4 tens in each group 8 hundreds divided into 2 equal groups 4 hundreds in each group	Represent divisions using place value equipment. $ q \div 3 = $	Use known facts to divide 10s and 100s by a single digit. $15 \div 3 = 5$ $150 \div 3 = 50$ $1500 \div 3 = 500$

