## St Matthew's Church of England Primary Academy <br> Maths Calculation Policy - Addition and Subtraction

## Mission Statement:

St. Matthew's C.E. Primary Academy is dedicated to providing an education which enables every child to fulfil their best potential. It seeks to promote academic, emotional and spiritual growth in a Christian environment, welcoming children drawn fromdiverse cultures.

## Vision Statement:

Inspired by Jesus' words (Matthew 5: 1-12), we strive to promote academic, emotional and spiritual growth in a Christian environmentfor all members of our school family.

We can all 'Be blessed by God, be happy and aspire to be...'

## Calculation policy - addition and subtraction

The following pages show the progression in calculation (addition and subtraction) and how this works in line with the National
Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operationsin an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

## Year 1-6

## Calculation Policy Addition and Subtraction

## \#MathsEveryoneCan

Notes and Guidance

## Calculation Policy

Welcome to the White Rose Maths Calculation Policy.
This document is broken down into addition andsubbraction, and multiplication and division.

At the start of each policy, there is an overview of thedifferent models and images that can support the teaching of different concepts. These provide explanations of the benefits of using the models and show the links between different operations.


Each operation is then broken down into skills andeach skill has a dedicated page showing the different models and images that could be used toeffectively teach that concept.


There is an overview of skills linked to year groupsto support consistency throughout school. A glossary of terms is provided at the end of the calculation policy to support understanding of the key language used to teach the four operations.

## Part-Whole Model


$7=4+3$
$7-3=4$
$7=3+4$
$7-4=3$

## Benefits

This part-whole model supports children in their understanding of aggregation and partitioning. Due to its shape, it can be referred to as a cherry part-whole model.

When the parts are complete and the whole is empty, children use aggregation to add the parts together to findthe total.

When the whole is complete and at least one of the partsis empty, children use partitioning (a form of subtraction) to find the missing part.

Part-whole models can be used to partition a number into two or more parts, or to help children to partition a number into tens and ones or other place value columns.

In KS2, children can apply their understanding of the part-whole model to add and subtract fractions, decimalsand percentages.

## Bar Model (single)

## Concrete



Combination


## Benefits

The single bar model is another type of a part-wholemodel that can support children in representing calculations to help them unpick the structure.

Cubes and counters can be used in a line as a concreterepresentation of the bar model.

Discrete bar models are a good starting point withsmaller numbers. Each box represents one whole.

The combination bar model can support children to calculate by counting on from the larger number. It is a good steppingstone towards the continuous bar model.

Continuous bar models are useful for a range of values. Each rectangle represents a number. The question markindicates the value to be found.

In KS2, children can use bar models to represent largernumbers, decimals and fractions.

## Bar Model (multiple)

## Discrete



Continuous

$2,394-1,014=1,380$

## Benefits

The multiple bar model is a good way to comparequantities whilst still unpicking the structure.

Two or more bars can be drawn, with a bracket labellingthe whole positioned on the right-hand side of the bars. Smaller numbers can be represented with a discrete barmodel whilst continuous bar models are more effective for larger numbers.

Multiple bar models can also be used to represent the difference in subtraction. An arrow can be used to modelthe difference.

When working with smaller numbers, children can use cubes and a discrete model to find the difference. This supports children to see how counting on can help whenfinding the difference.

## Number Shapes



## Benefits

Number shapes can be useful to support children tosubitise numbers as well as explore aggregation, partitioning and number bonds.

When adding numbers, children can see how the parts come together making a whole. As children use numbershapes more often, they can start to subitise the total dueto their familiarity with the shape of each number.

When subtracting numbers, children can start with the whole and then place one of the parts on top of the whole to see what part is missing. Again, children will start to be able to subitise the part that is missing due totheir familiarity with the shapes.

Children can also work systematically to find number bonds. As they increase one number by 1 , they can seethat the other number decreases by I to find all the possible number bonds for a number.

## Cubes



$$
7=3+4
$$


$7-3=4$


$$
7-3=4
$$

## Benefits

Cubes can be useful to support children with the additionand subtraction of one-digit numbers.

When adding numbers, children can see how the parts come together to make a whole. Children could use twodifferent colours of cubes to represent the numbers before putting them together to create the whole.

When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model ofsubtraction is reduction, or take away.

Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then linedup to find the difference between the numbers.

Cubes are useful when working with smaller numbersbut are less efficient with larger numbers as they are difficult to subitise and children may miscount them.

## Ten Frames (within 10)



## Benefits

When adding and subtracting within 10 , the ten framecan support children to understand the different structures of addition and subtraction.

Using the language of parts and wholes represented by objects on the ten frame introduces children to aggregation and partitioning.
Aggregation is a form of addition where parts are combined together to make a whole. Partitioning is a form of subtraction where the whole is split into parts. Using these structures, the ten frame can enable children to find all the number bonds for a number.

Children can also use ten frames to look at augmentation (increasing a number) and take-away (decreasing a number). This can be introduced through a first, then, now structure which shows the change in the number in the 'then' stage. This can be put into a story structure to help children understand the change e.g. First, there were 7 cars. Then, 3 cars left. Now, there are 4 cars.

## Ten Frames (within 20)



## Benefits

When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This supports children to see how they have partitioned one ofthe numbers to make 10 , and makes links to effective mental methods of addition.

When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how you have partitioned the number to make 10 , this supports mental methods of subtraction.

When adding three single-digit numbers, children can make each number on 3 separate 10 frames before considering which order to add the numbers in. They may be able to find a number bond to $I O$ which makes the calculation easier. Once again, the ten frames support the link to effective mental methods of addition as well as the importance of commutativity

## Bead Strings

## -00-00000000--000-0000000-

## -00-000000000000000000--000-00000000000000000-



## Benefits

Different sizes of bead strings can support children atdifferent stages of addition and subtraction.

## Bead strings to 10 are very effective at helping children to

 investigate number bonds up to 10They can help children to systematically find all the number bonds to $I O$ by moving one bead at a time to see
the different numbers they have partitioned the 10 beadsinto e.g. $2+8=10$, move one bead, $3+7=10$.

Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to $I O$ and see the links tonumber bonds to 20 .

Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping whenadding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.

## Number Tracks



$$
10-4=6
$$



$$
8+7=15
$$



## Benefits

Number tracks are useful to support children in their understanding of augmentation and reduction.

When adding, children count on to find the total of the numbers. On a number track, children can place a counter on the starting number and then count on to findthe total.

When subtracting, children count back to find their answer. They start at the minuend and then take awaythe subtrahend to find the difference between the numbers.

Number tracks can work well alongside ten frames andbead strings which can also model counting on or counting back.

Playing board games can help children to become familiar with the idea of counting on using a numbertrack before they move on to number lines.

## Number Lines (labelled)



## Benefits

Labelled number lines support children in theirunderstanding of addition and subbraction as augmentation and reduction.

Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.

Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames. The smaller number is partitioned to support children to make a number bondto 10 and to then add on the remaining part.

Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames sochildren can see how they partition the smaller number into the two separate
jumps.

## Number Lines (blank)

$$
35+37=72
$$


$35+37=72$

$72-35=37$


## Benefits

Blank number lines provide children with a structure toadd and subtract numbers in smaller parts.

Developing from labelled number lines, children can addby jumping to the nearest $I O$ and then adding the rest ofthe number either as a whole or by adding the tens and ones separately.

Children may also count back on a number line to subtract, again by jumping to the nearest $I O$ and thensubtracting the rest of the number.

Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. Theythen add up the parts they have counted on to find the difference between the $n$

## Straws



## Benefits

Straws are an effective way to support children in their understanding of exchange when adding and subtracting2-digit numbers.

Children can be introduced to the idea of bundling groups of ten when adding smaller numbers and when representing 2-digit numbers. Use elastic bands or otherties to make bundles of ten straws.

When adding numbers, children bundle a group of 10 straws to represent the exchange from 10 ones to 1 ten. They then add the individual straws (ones) and bundlesof straws (tens) to find the total.

When subtracting numbers, children unbundle a group of 10 straws to represent the exchange from I ten to 10 ones.

Straws provide a good steppingstone to adding andsubtracting with Base 10/Dienes.

## Base 10/Dienes (addition)



38
$+23$
61
1

265
$+164$
429
1

## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing Base 10 so they can see theclear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange.. The representationbecomes less efficient with larger numbers due to the size of Base 10 . In this case, place value counters may bethe better model to use.

When adding, always start with the smallest place value column. Here are some questions to support children. How many ones are there altogether?
Can we make an exchange? (Yes or No)
How many do we exchange? (IO ones for I ten, show exchanged 10 in tens column by writing I in column) How many ones do we have left? (Write in ones column) Repeat for each column.

## Base 10/Dienes (subtraction)


${ }^{3} 4^{135}$
$-273$
162

## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing Base 10 so they can see theclear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. When building the model, children should just make the minuend using Base 10 , they then subtract the subtrahend. Highlight this difference to addition to avoid errors by making both numbers. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g.exchange I ten for 10 ones. They can then subtract efficiently. This model is efficient with up to 4 -digit numbers. Placevalue counters are more efficient with larger numbers and decimals.

## Place Value Counters (addition)




## Benefits

Using place value counters is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children
to experience the exchange between columns.
When adding money, children can also use coins to support their understanding. It is important that childrenconsider how the coins link to the written calculation especially when adding decimal amounts.

## Place Value Counters (Subtraction)




## Benefits

Using place value counters is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first subtract without an exchange beforemoving on to subtraction with exchange. If you don't haveplace value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When building the model, children should just make the minuend using counters, they then subtract the subtrahend Children start with the smallest place value column. When there are not enough ones/tens/hundredsto subtract in a column, children need to move to the column to the left and exchange e.g. exchange I ten for 10 ones. They can then subtract efficiently.

## Addition

| Skill | Year | Representations and models |  |
| :---: | :---: | :---: | :---: |
| Add two 1-digit <br> numbers to 10 | 1 | Part-whole model <br> Bar model <br> Number shapes | Ten frames (within 10) <br> Bead strings (10) <br> Number tracks |
| Add 1 and 2-digit <br> numbers to 20 | 1 | Part-whole model <br> Bar model <br> Number shapes <br> Ten frames (within 20) | Bead strings (20) <br> Number tracks <br> Number lines (labelled) <br> Straws |
| Add three 1-digit | 2 | Part-whole model <br> Bar model | Ten frames (within 20) <br> Number shapes |
| Add 1 and 2-digit <br> numbers to 100 | 2 | Part-whole model <br> Bar model <br> Number lines (labelled) | Number lines (blank) <br> Straws <br> Hundred square |


| Skill | Year | Representations and models |  |
| :---: | :---: | :---: | :---: |
| Add two 2-digit numbers | 2 | Part-whole model Bar model Number lines (blank) Straws | Base 10 <br> Place value counters |
| Add with up to 3-digits | 3 | Part-whole model Bar model | Base 10 <br> Place value counters Column addition |
| Add with up to 4-digits | 4 | Part-whole model Bar model | Base 10 <br> Place value counters Column addition |
| Add with more than 4 digits | 5 | Part-whole model Bar model | Place value counters Column addition |
| Add with up to 3 decimal places | 5 | Part-whole model Bar model | Place value counters Column addition |











## Subtraction

| Skill | Year | Representations and models |  |
| :---: | :---: | :---: | :---: |
| Subtract two 1-digit <br> numbers to 10 | 1 | Part-whole model <br> Bar model <br> Number shapes | Ten frames (within 10) <br> Bead strings (10) <br> Number tracks |
| Subtract 1 and 2-digit <br> numbers to 20 | 1 | Part-whole model <br> Bar model <br> Number shapes <br> Ten frames (within 20) | Bead string (20) <br> Number tracks <br> Number lines (labelled) <br> Straws |
| Subtract 1 and 2-digit <br> numbers to 100 | 2 | Part-whole model <br> Bar model <br> Number lines (labelled) | Number lines (blank) <br> Straws <br> Hundred square |
| Subtract two 2-digit | 2 | Part-whole model <br> Bar model <br> numbers | Number lines (blank) <br> Straws |
| Base 10 |  |  |  |


| Skill | Year | Representations and models |  |
| :---: | :---: | :---: | :---: |
| Subtract with up to 3- <br> digits | 3 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column subtraction |
| Subtract with up to 4- <br> digits | 4 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column subtraction |
| Subtract with more than <br> 4 digits | 5 | Part-whole model <br> Bar model | Place value counters <br> Column subtraction |
| Subtract with up to 3 <br> decimal places | 5 | Part-whole model <br> Bar model | Place value counters |
| Column subtraction |  |  |  |









## Glossary

Addend - A number to be added to another

Aggregation - combining two or more quantities or measures to find a total

Augmentation - increasing a quantity or measure byanother quantity.

Commutative - numbers can be added in any order.
Complement - in addition, a number and itscomplement make a total e.g. 300 is the complement to 700 to make I,000

Difference - the numerical difference between two numbers is found by comparing the quantity in eachgroup.

Exchange - Change a number or expression foranother of an equal value.

Minuend - A quantity or number from which a notheris subtracted.

Partitioning - Splitting a number into its componentparts.
Reduction - Subtraction as take away.

Subitise - Instantly recognise the number of objects in a small group without needing to count.

Subtrahend - A number to be subtracted fromanother.

Sum - The result of an addition.
Total - The aggregate or the sum found by addition.

