

Calculation Policy: Guidance

An Overview of the Calculations



St Hugh of Lincoln
R.C Primary School

St Hugh of Lincoln have adopted the White Rose Scheme. Teachers have reviewed the White Rose Calculation Policy and have slightly altered layout in some of the calculations.

For more detail regarding Mathematical Models and Representations please see the White Rose Calculation Policy.

Teachers will use Mathematical Models and Representations to support understanding.

In KS1, concrete and pictorial are used to help develop firm foundations in children's mathematical understanding before moving on to abstract methods. In KS2 children, teachers can use concrete and pictorial resources alongside abstract methods (written) to support learning and understanding.

Updated: July 2021

Concrete representation – a pupil is first introduced to a concept/skill by acting it out with real objects. This is a ‘hands on’ component using real objects and a foundation for conceptual understanding.

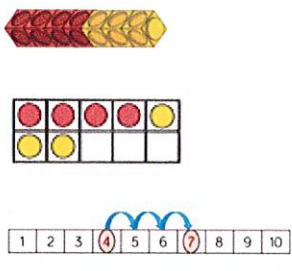
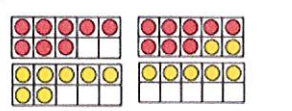
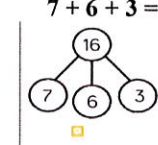
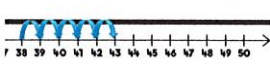
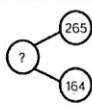
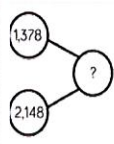
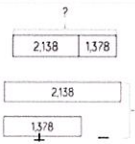
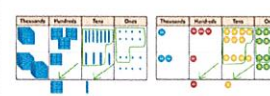
Pictorial representation – a pupil can relate to representations that present a concept/skill in a picture or a diagram

Abstract representation – a pupil is now capable of representing problems by using mathematical notation, for example $12 \times 3 = 36$

Mathematics Mastery

At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to achieve. They should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply learn rote procedures but demonstrate a clear understanding of these procedures through the use of concrete and pictorial representations.

For each of the four rules of number, different concrete and pictorial representations/models are highlighted in red. The policy does not recommend one set of resources over another, rather that a variety of resources are used.

<p>Addition</p> <p><i>Key Language</i></p> <p>sum</p> <p>total</p> <p>parts</p> <p>wholes</p> <p>plus</p> <p>add</p> <p>altogether</p> <p>more</p> <p>equal</p>	<p><u>Year 1</u></p> <p>Add two 1-digit numbers to 10</p> <p>Using numicon/cubes Tens frames Number tracks</p>  <p>$4 + 3 = 7$</p> <p>Add 1- and 2-digit numbers to 20</p> <p>Using Part Whole Model Numicon/cubes Tens frames Number tracks/Number lines (labelled)</p> <p>$8 + 7 = 15$</p> 	<p><u>Year 2</u></p> <p>Add three 1-digit numbers</p> <p>Using numicon/cubes Tens frames Part Whole Model</p> <p>$7 + 6 + 3 = 16$</p>  <p>Add 1-digit and 2-digit numbers to 100.</p> <p>Counting on from larger number. Using number tracks and number lines</p> <p>$38 + 5 = 43$</p>  <p>Add two 2-digit numbers to 100</p> <p>Blank number line</p> <p>Partitioning</p> <p>$37 + 26 = 63$ $30 + 20 = 50$ $7 + 6 = 13$ $50 + 13 = 63$</p>	<p><u>Year 3</u></p> <p>Add two 2-digit numbers to 100</p> <p>(See Yr. 2 methods) Year 2 do not need to learn formal methods for addition, but pupils could begin to think about the two quantities arranged in columns under the place value headings of tens and ones. (Using counters or drawing dots)</p> <p>Formal Method Expanded Method</p> <p>T O $30 + 8$ $20 + 3$ $+ 10$ <hr/>$60 + 1 = 61$</p> <p>Column Addition</p> <p>38 23 $+ 1$ <hr/>61</p> <p>Add numbers with up to 3-digits</p> <p>Part Whole Bar Model Place Value Counters</p>  <p>265 164 $+ 1$ <hr/>429</p>	<p><u>Year 4</u></p> <p>Add numbers with up to 4 digits</p> <p>Place Value Counters Part Whole Model Bar Model</p>    <p>Formal Method Column Addition</p> <p>1378 2148 $+ 11$ <hr/>3526</p>	<p><u>Year 5/6</u></p> <p>Add numbers with more than 4-digits</p> <p>Place Value Counters Part Whole Model Bar Model</p> <p>At this stage children are encouraged to work in the abstract, using the column method to add larger numbers efficiently.</p> <p>104325 61731 $+ 1$ <hr/>166056</p> <p>Add with up to 3 decimal places</p> <p>3.65 2.41 $+ 1$ <hr/>6.06</p> <p>Children have experience of adding decimals with a variety of decimal places.</p>
---	---	---	---	--	--

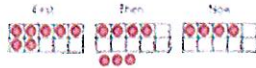
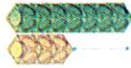
Subtraction

Key Language
take away
less than
the
difference
subtract
minus
fewer
decrease

Year 1

Subtract two 1-digit numbers to 10

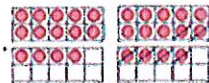
Using numicon/cubes
Tens frames
Number tracks
Part Whole Models



$$7 - 3 = 4$$

Subtract 1- and 2-digit numbers to 20

Using numicon/cubes
Tens frames
Number tracks/number lines



$$14 - 6 = 8$$

Year 2

Subtract 1- and 2-digit numbers to 20

Using numicon/cubes
Tens frames
Number tracks/number lines
(See Year 1)



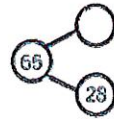
$$14 - 6 = 8$$

Subtract 1- and 2-digit numbers to 100

Blank number line to count on and find the difference



$$65 - 28 = 37$$



$$65 - 20 = 45$$

$$45 - 8 = 37$$

Year 2 do not need to learn formal methods for subtraction, but pupils could begin to think about the two quantities arranged in columns under place value headings of tens and ones. (Using counters or drawing dots)

Year 3

Subtract numbers with up to 3-digits

Part whole model
Bar model
Place Value Counters

Formal Method
Expanded Column

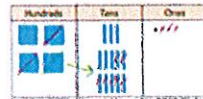
$$\begin{array}{r} \text{T} \quad \text{O} \\ 50 \quad 1 \\ 60 \quad 5 \\ - 20 \quad 8 \\ \hline 30 \quad 7 \end{array}$$

Column Subtraction

$$65 - 28 = 37$$

$$\begin{array}{r} 65 \\ - 28 \\ \hline 37 \end{array}$$

$$435 - 273 = 262$$



Expanded Column

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{O} \\ 300 \quad 1 \\ 400 \quad 30 \quad 5 \\ 200 \quad 70 \quad 3 \\ \hline 100 \quad 60 \quad 2 \end{array}$$

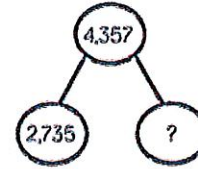
Column Subtraction

$$\begin{array}{r} 31 \\ 435 \\ - 273 \\ \hline 162 \end{array}$$

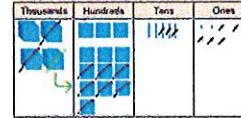
Year 4

Subtract numbers with up to 4- digits

Part Whole Model
Bar model



Place Value Counters used alongside a place value grid



$$4,357 - 2,735 = 1,622$$

Formal Method
Column Subtraction

$$\begin{array}{r} 3 \quad 1 \\ 4357 \\ - 2735 \\ \hline 1622 \end{array}$$

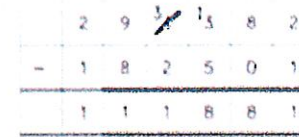
Year 5/6

Subtract numbers with more than 4-digits

Part Whole Model
Bar Model

Place Value Counters used alongside a grid

$$294,382 - 182,501 = 111,881$$



Subtract with up to 3 decimal places

$$5.43 - 2.7 = 2.73$$

Formal Method
Column Subtraction

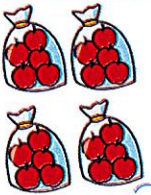
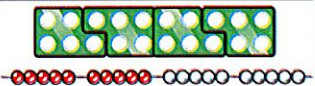
$$\begin{array}{r} 4 \quad 1 \\ 5.43 \\ - 2.7 \\ \hline 2.73 \end{array}$$

Multiplication

Key Language

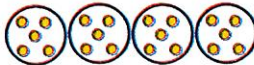
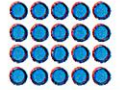
double times multiplied by the product of lots of equal groups

Year 1
Solve 1-step problems using multiplication
Numicon
Counters
Tens frames
Bead Strings
Number line
Real Life Objects

Year 1 not expected to record multiplication formally
Year 1 use concrete and pictorial representations to solve problems

Year 2
Solve 1-step problems using multiplication
Numicon
Counters
Tens frames
Bead Strings
Number line

$5 + 5 + 5 + 5 = 20$
 $4 \times 5 = 20$
 $5 \times 4 = 20$

Repeated grouping/repeated addition
 $5 + 5 + 5 + 5 = 20$

Year 2 are introduced to the multiplication symbol
 $4 \times 5 = 20$
 $5 \times 4 = 20$

Use arrays to illustrate commutatively

Year 3
Multiply 2-digit numbers by 1 digit
Partition to multiply using Numicon/base 10
Grid Method

X	10	5
4	40	20

$15 \times 4 = 60$
 $10 \times 4 = 40$
 $5 \times 4 = 20$

Formal Method
Expanded Column

H	T	0
	3	4
X		5
	2	0 (5x4)
1	5	0 (5x30)
1	7	0

Place value counters could be used to support understanding

Year 4
Formal Method
Short Multiplication Method

H	T	0
	3	4
X		5
	1	7
		0
1		2

Multiply 3-digit numbers by 1-digit numbers
Base 10/place value counters could be used to support the understanding of the written method

H	T	0
	2	4
x		4
	9	8
		0
1		2

Year 5
Multiply 4 -digit numbers by 1-digit numbers
Place Value Counters could be used to continue to support understanding
Encourage use of multiplication grids if children are struggling with times tables.

$1,826 \times 3 = 5,478$

TH	H	T	0
	1	8	2
X			3
	5	4	7
			8
2			1

Multiply 2-digit numbers by 2- digit numbers
Area Model – Base 10
Grid Method before moving on to the formal written multiplication

X	20	2
30	600	60
1	20	2

H	T	0
	2	2
X		3
	2	2
	6	6
		0
6	8	2

Year 5

Multiply 3-digit numbers by 2-digit numbers

Area Model using base ten/place value counters

X	200	30	4
30	6,000	900	120
2	400	60	8

Formal Method



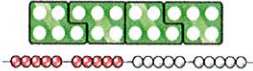
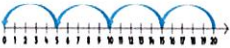
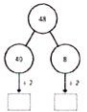
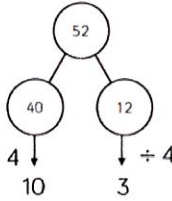
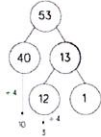
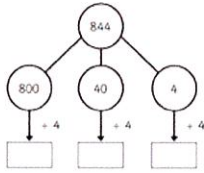
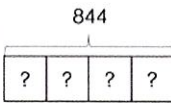
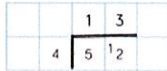
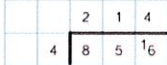
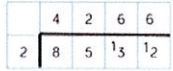
$$\begin{array}{r} \text{TH H T O} \\ 234 \\ \times 32 \\ \hline 468 \\ 171020 \\ \hline 7488 \end{array}$$

Year 5/6

Multiply 4-digit numbers by 2-digit numbers

$$\begin{array}{r} \text{TTh Th H T O} \\ 2739 \\ \times 28 \\ \hline 225139712 \\ 1541780 \\ \hline 76692 \\ 1 \end{array}$$

Children struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.

	Year 1/2	Year 1/2	Year 3/4	Year 4	Year 4/5	Year 5
<p>Division</p> <p><i>Key Language</i></p> <p>share</p> <p>group</p> <p>divide</p> <p>divided</p> <p>by</p> <p>half</p>	<p>Solve 1 step problems using multiplication (sharing)</p> <p>Children solve problems by sharing amounts into equal groups</p> <p>Real life objects Arrays Bar Model Counters</p>   <p>In Year 1, children are not expected to record division formally.</p> <p>In Year 2, children are introduced to the division symbol</p> <p>$20 \div 5 = 4$</p>	<p>Solve 1 step problems using division (grouping)</p> <p>Real life objects Numicon Bead Strings Number lines Arrays Counters</p>  <p>Children count in multiples, links to repeated subtraction on a number line.</p>  <p>Divide 2 digits by 1 digit (sharing with no exchange)</p> <p>Place Value Counters Part Whole Model</p> 	<p>Divide 2 digits by 1 digit (sharing with exchange)</p> <p>Base 10 Bar Model Place Value Counters Part-whole model</p>  <p>$52 \div 4 = 13$ $52 \div 4 = 13$ $40 \div 4 = 10$ $12 \div 4 = 3$</p> <p>Divide 2 digits by 1 digit (Sharing with remainders) $53 \div 4 = 13r1$</p> 	<p>Divide 3 digits by 1 digit (sharing)</p> <p>Place Value Counters Bar Model Part-Whole Model</p> <p>Partitioning</p>  <p>$844 \div 4 = 211$</p> 	<p>Divide 2 digits by 1 digit (grouping)</p> <p>Place Value Counters</p> <p>Formal Method Short division method</p> 	<p>Divide 3 digits by 1 digit (grouping)</p> <p>Place Value /Plain Counters</p> <p>Formal Method Short division method</p>  <p>Divide 4 digits by 1 digit (grouping)</p> <p>Place Value/Plain Counters</p>  <p>Children to be encouraged to move away from the concrete and the pictorial when dividing numbers with multiple exchanges.</p>

Year 6

Divide multi digits by 2 digits (Short Division)

Use of concrete and pictorial representations become less effective

Children can write out multiples to support their calculations

		0	3	6
	12	4	3	2

$$432 \div 12 = 36$$

$$7,335 \div 15 = 489$$

		0	4	8	9
15		7	3	3	5

15	30	45	60	75	90	105	120	135	150
----	----	----	----	----	----	-----	-----	-----	-----

Year 6

Divide multi digits by 2 digits (Long Division)

		0	3	6	
1	2	4	3	2	(x30)
	-	3	6	0	
			7	2	
	-		7	2	(x6)
				0	

- 12 x 1 = 12
- 12 x 2 = 24
- 12 x 3 = 36
- 12 x 4 = 48
- 12 x 5 = 60
- 12 x 6 = 72
- 12 x 7 = 84
- 12 x 8 = 96
- 12 x 9 = 108
- 12 x 10 = 120

$$432 \div 12 = 36$$

$$7,335 \div 15 = 489$$

		0	4	8	9		
15		7	3	3	5	(x400)	
	-	6	0	0	0		
			1	3	5		
	-		1	2	0	(x80)	
				1	3	5	
	-			1	3	5	(x9)
					0		

- 1 x 15 = 15
- 2 x 15 = 30
- 3 x 15 = 45
- 4 x 15 = 60
- 5 x 15 = 75
- 10 x 15 = 150

Glossary

Addend - A number to be added to another.

Aggregation - combining two or more quantities or measures to find a total.

Augmentation - increasing a quantity or measure by another quantity.

Commutative - numbers can be added in any order.

Complement - in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

Difference - the numerical difference between two numbers is found by comparing the quantity in each group.

Exchange - Change a number or expression for another of an equal value.

Minuend - A quantity or number from which another is subtracted.

Partitioning - Splitting a number into its component parts.

Reduction - Subtraction as take away.

Subitise - Instantly recognise the number of objects in a small group without needing to count.

Subtrahend - A number to be subtracted from another.

Sum - The result of an addition.

Total - The aggregate or the sum found by addition.