# Mathematics Written Calculations Policy for Whitefield Primary School

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#### Introduction

Children are introduced to the processes of calculation through practical, oral and mental activities.

As children begin to understand the underlying ideas they develop ways of recording to support their thinking and calculation methods, use particular methods that apply to special cases, and learn to interpret and use the signs and symbols involved. Over time children learn how to use models and images to support their mental and informal written methods of calculation. As children's mental methods are strengthened and refined, so too are their informal written methods. These methods become more efficient and succinct and lead to efficient written methods that can be used more generally.

By the end of Year 6 children are equipped with mental, written and calculator methods that they understand and can use correctly. When faced with a calculation, children are able to decide which method is most appropriate and have strategies to check its accuracy. At whatever stage in their learning, and whatever method is being used, it must still be underpinned by a secure and appropriate knowledge of number facts, along with those mental skills that are needed to carry out the process and judge if it was successful.

#### **Aims**

The overall aim is that when children leave primary school they:

- have a secure knowledge of number facts and a good understanding of the four operations;
- are able to use this knowledge and understanding to carry out calculations mentally and to apply general strategies when using one-digit and two-digit numbers and particular strategies to special cases involving bigger numbers;
- make use of diagrams and informal notes to help record steps and part answers when using mental methods that generate more information than can be kept in their heads;
- have an efficient, reliable, compact written method of calculation for each operation that children can apply with confidence when undertaking calculations that they cannot carry out mentally;
- use a calculator effectively, using their mental skills to monitor the process, check the steps involved and decide if the numbers displayed make sense.

#### Mental methods of calculation

Oral and mental work in mathematics is essential, particularly so in calculation. Early practical, oral and mental work must lay the foundations by providing children with a good understanding of how the four operations build on efficient counting strategies and a secure knowledge of place value and number facts.

Later work must ensure that children recognise how the operations relate to one another and how the rules and laws of arithmetic are to be used and applied. Ongoing oral and mental work provides practice and consolidation of these ideas. It must give children the opportunity to apply what they have learned to particular cases, exemplifying how the rules and laws work, and to general cases where children make decisions and choices for themselves.

The ability to calculate mentally forms the basis of all methods of calculation and has to be maintained and refined. A good knowledge of numbers or a 'feel' for numbers is the product of structured practice and repetition. It requires an understanding of number patterns and relationships developed through directed enquiry, use of models and images and the application of acquired number knowledge and skills. Secure mental calculation requires the ability to:

- recall key number facts instantly
- use taught strategies to work out the calculation
- understand how the rules and laws of arithmetic are used and applied

Before carrying out a calculation, children should be encouraged to consider:

- Can I solve the problem mentally?
- What is an estimate for the answer?
- What jottings can I make?

# Progression Towards a Written Method for Addition

In developing a written method for addition, it is important that children understand the concept of addition, in that it is:

- Combining two or more groups to give a total or sum
- Increasing an amount

They also need to understand and work with certain principles, i.e. that it is:

- the inverse of subtraction
- commutative i.e. 5 + 3 = 3 + 5
- associative i.e. 5 + 3 + 7 = 5 + (3 + 7)

The fact that it is commutative and associative means that calculations can be rearranged, e.g.

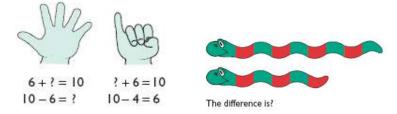
4 + 13 = 17 is the same as 13 + 4 = 17.

#### **RECEPTION**

#### **Early Learning Goal:**

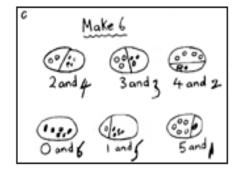
Using quantities and objects, children add two single-digit numbers and count on to find the answer.

Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of practical equipment, including small world play, role play, counters, cubes etc.



#### Counting all method

Children will begin to develop their ability to add by using practical equipment to count out the correct amount for each number in the calculation and then combine them to find the total. For example, when calculating 4 + 2, they are encouraged to count out four counters and count out two counters.



#### Counting on method

To support children in moving from a counting all strategy to one involving counting on, children should still have two groups of objects but one should be covered so that it cannot be counted. For example, when calculating 4 + 2, count out the two groups of counters as before.

Those who are ready may record their own calculations.

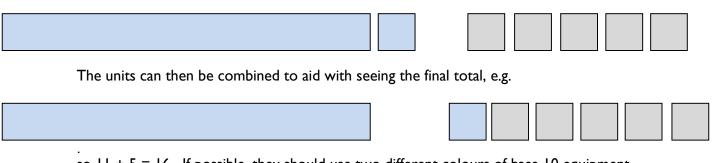
#### YEAR I

#### **End of Year Objective:**

Add one-digit and two-digit numbers to 20, including zero (using concrete objects and pictorial representations).

Children will continue to use practical equipment, combining groups of objects to find the total by counting all or counting on. Using their developing understanding of place value, they will move on to be able to use Base 10 equipment to make teens numbers using separate tens and units.

For example, when adding II and 5, they can make the II using a ten rod and a unit.



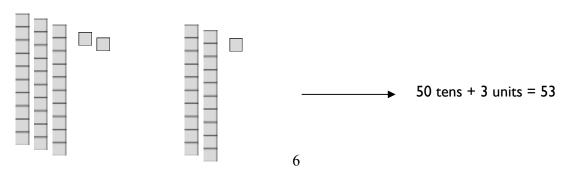
so 11 + 5 = 16. If possible, they should use two different colours of base 10 equipment so that the initial amounts can still be seen.

#### YEAR 2

#### **End of Year Objective:**

Add numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones; a two-digit number and tens; two two-digit numbers; three one-digit numbers.

Children will continue to use the Base 10 equipment to support their calculations. For example, to calculate 32 + 21, they can make the individual amounts, counting the tens first and then count on the units.

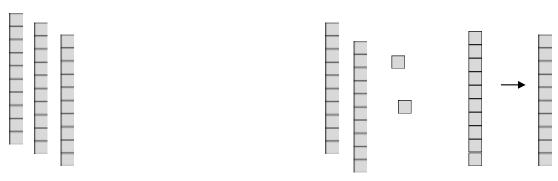


When the units total more than 10, children should be encouraged to exchange 10 units/ones for 1 ten. This is the start of children understanding 'carrying' in vertical addition. For example, when calculating

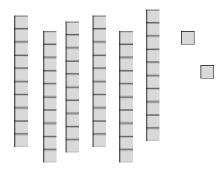
35 + 27, they can represent the amounts using Base 10 as shown:



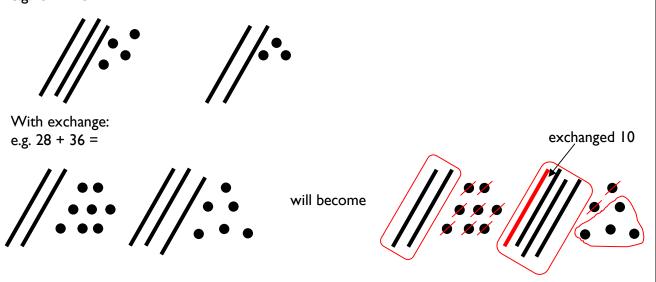
Then, identifying the fact that there are enough units/ones to exchange for a ten, they can carry out this exchange:



To leave:



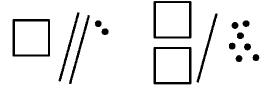
Children can also record the calculations using their own drawings of the Base 10 equipment (as slanted lines for the 10 rods and dots for the unit blocks). e.g. 34 + 23 =



so 28 + 36 = 64

It is important that children cross out the units/ones that they have exchanged to a 10 in order to eliminate them and circle the remaining tens and units/ones to identify the amount remaining.

This method can also be used with adding three digit numbers, e.g. 122 + 217 using a square as the representation of 100.



#### YEAR 3

**End of Year Objective:** 

Add numbers with up to three digits, using formal written method of columnar addition.\*

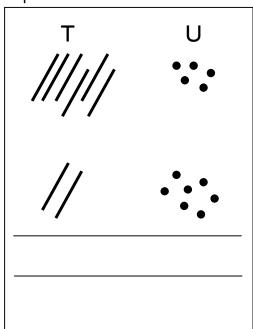
Children will build on their knowledge of using Base 10 equipment from Y2 and continue to use the idea of exchange.

Children should add the **least significant digits** first (i.e. start with the units/ones), and in an identical method to that from year 2, should identify whether there are greater than ten units which can be exchanged for one ten.

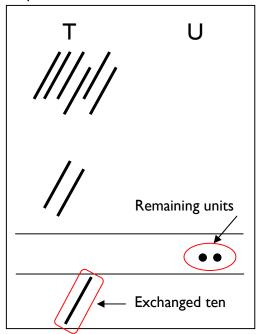
They can use a place value grid to begin to set the calculation out vertically and to support their knowledge of exchange between columns (as in Step I in the diagram below).

e.g. 65 + 27

Step I



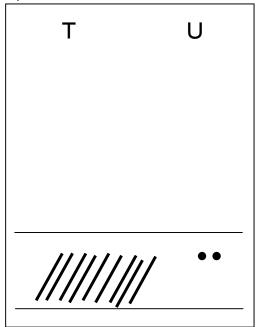
Step 2



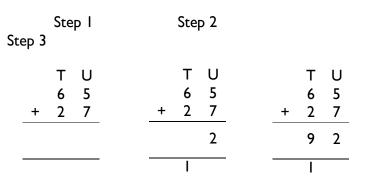
Children would exchange ten units/ones for a ten, placing the exchanged ten below the equals sign. Any remaining units/ones that cannot be exchanged for a ten move into the equals sign as they are the units part of the answer (as in the diagram in Step 2 above).

If there are any tens that can be exchanged for a hundred, this can be done next. If not, the tens move into the equals sign as they are the tens part of the answer (as in the diagram in Step 3 below).

Step 3



Written method



Children should utilise this practical method to link their understanding of exchange to how the column method is set out. Teachers should model the written method alongside this practical method initially.

This should progress to children utilising the written and practical methods alongside each other and finally, and when they are ready, to children utilising just the written method.

By the end of year 3, children should also extend this method for three digit numbers.

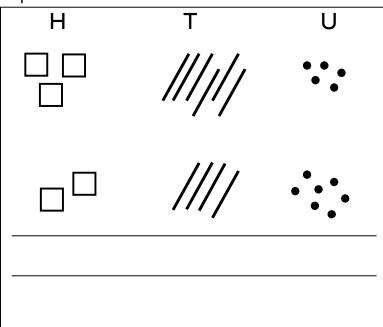
## YEAR 4

# **End of Year Objective:**

Add numbers with up to 4 digits and decimals with one decimal place using the formal written method of columnar addition where appropriate.

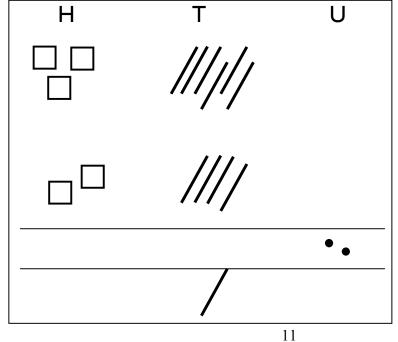
Children will move to year 4 using whichever method they were using as they transitioned from year 3.

Step I

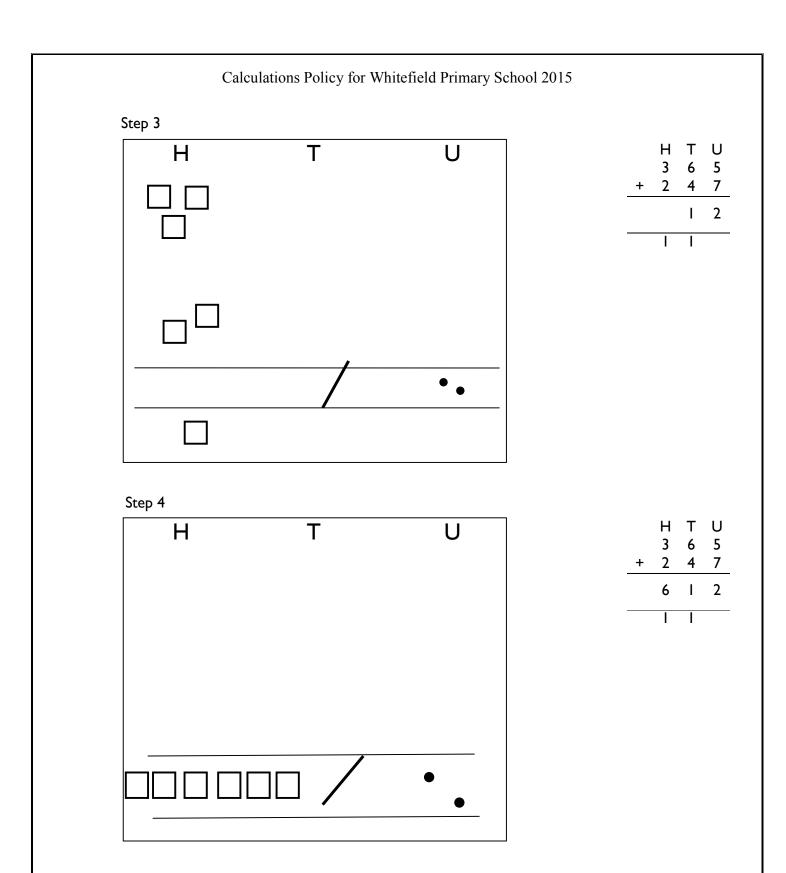


	Н	Т	U
	3	6	5
+	2	4	7

Step 2



	Н	Т	U
	3	6	5
+	2	4	7
			2
-		-	



By the end of year 4, children should be using the written method confidently and with understanding.

#### YEAR 5

**End of Year Objective:** 

Add whole numbers with more than 4 digits and decimals with two decimal places, including formal written methods (columnar addition).

Children should continue to use the carrying method to solve calculations such as:

## YEAR 6

**End of Year Objective:** 

Add whole numbers and decimals using formal written methods (columnar addition).

Children should extend the carrying method and use it to add whole numbers and decimals with any number of digits.

When adding decimals with different numbers of decimal places, children should be taught and encouraged to make them the same through identification that 2 tenths is the same as 20 hundredths,

# <u>Progression Towards a Written Method for Subtraction</u>

In developing a written method for subtraction, it is important that children understand the concept of subtraction, in that it is:

- Removal of an amount from a larger group (take away)
- Comparison of two amounts (difference)

They also need to understand and work with certain principles, i.e. that it is:

- the inverse of addition
- not commutative i.e. 5 3 is not the same as 3 5
- not associative i.e. 10 3 2 is not the same as 10 (3 2)

#### **RECEPTION**

#### **Early Learning Goal:**

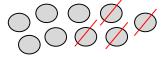
Using quantities and objects, children subtract two single-digit numbers and count on or back to find the answer.

Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of practical equipment, including small world play, role play, counters, cubes etc.



#### Taking away

Children will begin to develop their ability to subtract by using practical equipment to count out the first number and then remove or take away the second number to find the solution by counting how many are left e.g. 9 - 4.



Children would be encouraged to physically remove these using touch counting. By touch counting and dragging in this way, it allows children to keep track of how many they are removing so they don't have to keep recounting. They will then touch count the amount that are left to find the answer.



**Those who are ready** may record their own calculations.

#### YEAR I

## **End of Year Objective:**

Subtract one-digit and two-digit numbers to 20, including zero (using concrete objects and pictorial representations).

Children will continue to use practical equipment and taking away strategies. To avoid the need to exchange for subtraction at this stage, it is advisable to continue to use equipment such as counters, cubes and the units from the Base 10 equipment, but not the tens, e.g. 13 - 4



Touch count and remove the number to be taken away, in this case 4.



Touch count to find the number that remains.

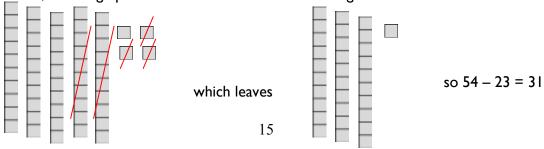


#### YEAR 2

## **End of Year Objective:**

Subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones; a two-digit number and tens; two-two-digit numbers.

Children will begin to use the Base 10 equipment to support their calculations, still using a take away, or removal, method. They need to understand that the number being subtracted does not appear as an amount on its own, but rather as part of the larger amount. For example, to calculate 54 - 23, children would count out 54 using the Base 10 equipment (5 tens and 4 units). They need to consider whether there are enough units/ones to remove 3, in this case there are, so they would remove 3 units and then two tens, counting up the answer of 3 tens and 1 unit to give 31.



Children can also record the calculations using their own drawings of the Base 10 equipment (as slanted lines for the 10 rods and dots for the unit blocks), e.g. to calculate 39 – 17 children would draw 39 as 3 tens (lines) and 4 units (dots) and would cross out 7 units and then one ten, counting up the answer of 2 tens and 2 units to give 22.



Crossing out the tens and units/ones circling those that remain will help children to identify how many remain.

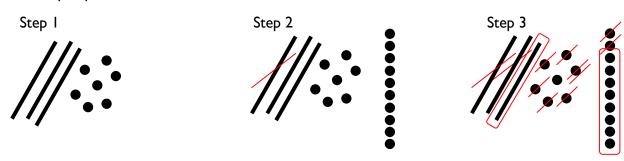
When the amount of units to be subtracted is greater than the units in the original number, an exchange method is required. This relies on children's understanding of ten units being an equivalent amount to one ten. To calculate 53 - 26, by using practical equipment, they would count out 53 using the tens and units, as in Step I. They need to consider whether there are enough units/ones to remove 6. In this case there are not so they need to exchange a ten into ten ones to make sure that there are enough, as in step 2.



The children can now see the 53 represented as 40 and 13, still the same total, but partitioned in a different way, as in step 3 and can go on to take away the 26 from the calculation to leave 27 remaining, as in Step 4.



When recording their own drawings, when calculating 37 - 19, children would cross out a ten and exchange for ten units. Drawing them in a vertical line, as in Step 2, ensures that children create ten ones and do not get them confused with the units that were already in place.



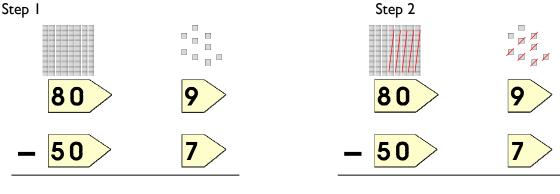
Crossing out the tens and units/ones circling those that remain will help children to identify how many remain.

**Y3** 

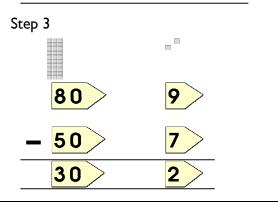
## **End of Year Objective:**

Subtract numbers with up to three digits, using formal written method of columnar subtraction.\*

Children will build on their knowledge of using Base 10 equipment from Y2 and continue to use the idea of exchange. This process should be demonstrated using arrow cards to show the partitioning and Base 10 materials to represent the first number, removing the units and tens as appropriate (as with the more informal method in Y2).



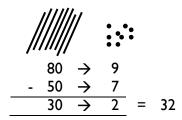
17



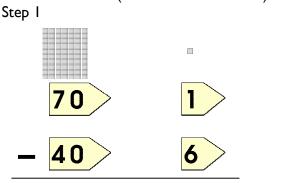
Emphasise that the second (bottom) number is being subtracted from the first (top) number rather than the lesser number from the greater.

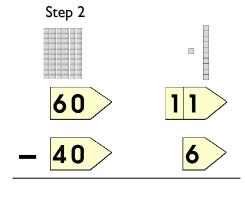
This will be recorded by the children as:

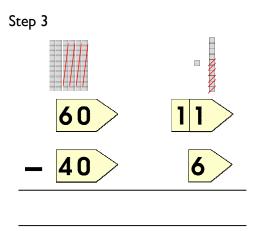
Children can also use jottings of the Base 10 materials (as in Year 2) to support with their calculation, as in the example below.

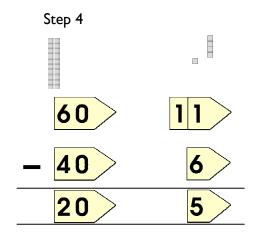


From this the children will begin to solve problems which involve exchange. Children need to consider whether there are enough units/ones to remove 6. In this case there are not (Step I) so they need to exchange a ten into ten ones to make sure that there are enough, as they have been doing in the method for Year 2 (Step 2). They should be able to see that the number is just partitioned in a different way, but the amount remains the same (71 = 70 + 1 = 60 + 11).









This will be recorded by the children as:

By the end of year 3, children should also extend this method for three digit numbers.

### YEAR 4

## **End of Year Objective:**

Subtract numbers with up to 4 digits and decimals with one decimal place using the formal written method of columnar subtraction where appropriate.

Children will move to Y4 using whichever method they were using as they transitioned from Y3.

Step I to units)

Step 2 (exchanging from tens

Step 4

Step 3 (exchanging from hundreds to tens)

This would be recorded by the children as:

When children are ready, this leads on to the compact method of decomposition:

By the end of Y4, children should be using the written method confidently and with understanding.

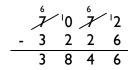
19

#### YEAR 5

**End of Year Objective:** 

Subtract whole numbers with more than 4 digits and decimals with two decimal places, including formal written methods (columnar subtraction).

Children should continue to use the decomposition method to solve calculations such as:

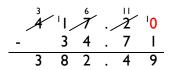


#### YEAR 6

**End of Year Objective:** 

Subtract whole numbers and decimals using formal written methods (columnar subtraction).

Children should extend the decomposition method and use it to subtract whole numbers and decimals with any number of digits.



When subtracting decimals with different numbers of decimal places, children should be taught and encouraged to make them the same through identification that 2 tenths

# Progression Towards a Written Method for Multiplication

In developing a written method for multiplication, it is important that children understand the concept of multiplication, in that it is:

repeated addition

They should also be familiar with the fact that it can be represented as an array

They also need to understand and work with certain principles, i.e. that it is:

- the inverse of division
- commutative i.e.  $5 \times 3$  is the same as  $3 \times 5$
- associative i.e.  $2 \times 3 \times 5$  is the same as  $2 \times (3 \times 5)$

#### **YR**

## **Early Learning Goal:**

Children solve problems, including doubling.

Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of equipment, including small world play, role play, counters, cubes etc.

Children may also investigate putting items into resources such as egg boxes, ice cube trays and baking tins which are arrays.





They may develop ways of recording calculations using pictures, etc.



A child's jotting showing the fingers on each hand as a double.



A child's jotting showing double three as three cookies on each plate.



#### YEAR I

#### **End of Year Objective:**

Solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the

In year one, children will continue to solve multiplication problems using practical equipment and jottings. They may use the equipment to make groups of objects. Children should see everyday versions of arrays, e.g. egg boxes, baking trays, ice cube trays, wrapping paper etc and use this in their learning, answering questions such as 'How many eggs would we need to fill the egg box? How do you know?'

#### <u>Y2</u>

#### **End of Year Objective:**

Calculate mathematical statements for multiplication (using repeated addition) and write them using the multiplication (x) and equals (=) signs.

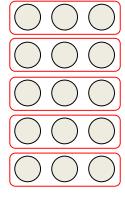
Children should understand and be able to calculate multiplication as repeated addition, supported by the use of practical apparatus such as counters or cubes. e.g.

5 x 3 can be shown as five groups of three with counters:

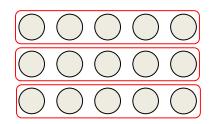


Children should then develop this knowledge to show how multiplication calculations can be represented by an array, (this knowledge will support with the development of the grid method in the future). Again, children should be encouraged to use practical apparatus and jottings to support their understanding, e.g.

 $5 \times 3^*$  can be represented as an array in two forms (as it has commutativity):



$$3 + 3 + 3 + 3 + 3 = 15$$



$$5 + 5 + 5 = 15$$

\*For mathematical accuracy  $5 \times 3$  is represented by the second example above, rather than the first as it is five, three times. However, because we use terms such as 'groups of' or 'lots of', children are more familiar with the initial notation. Once children understand the commutative order of multiplication the order is irrelevant).

#### YEAR 3

## **End of Year Objective:**

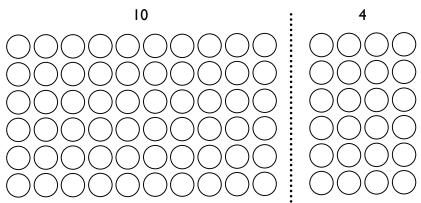
Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, progressing to formal written methods.\*

Initially, children will continue to use arrays where appropriate. This may be extended by making jottings on squared paper.

х	X	X	Х	х	Х	Х	Х	
x	X	X	x	х	X	X	X	
x	Х	Х	х	х	Х	Х	х	

$$3 \times 8 = 8 + 8 + 8 = 24$$

As they progress to multiplying a two-digit number by a single digit number, children should use their knowledge of partitioning two digit numbers into tens and units/ones to help them. For example, when calculating  $14 \times 6$ , children should set out the array, then partition the array so that one array has ten columns and the other four.



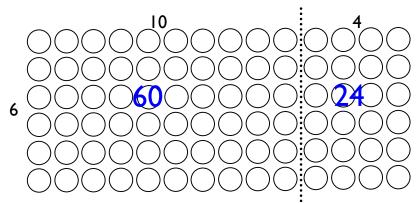
Partitioning in this way, allows children to identify that the first array shows  $10 \times 6$  and the second array shows  $4 \times 6$ . These can then be added to calculate the answer:

$$(6 \times 10) + (6 \times 4)$$

NB There is no requirement for children to record in this way, but it could be used as a jotting to support development if needed.

= 84

This method is the precursor step to the grid method. Using a two-digit by single digit array, they can partition as above, identifying the number of rows and the number of columns each side of the partition line.



By placing a box around the array, as in the example below, and by removing the array, the grid method can be seen.

Х	10	4
6	60	24

It is really important that children are confident with representing multiplication statements as arrays and understand the rows and columns structure before they develop the written method of recording.

From this, children can use the grid method to calculate two-digit by one-digit multiplication calculations. Children should be encouraged to set out their addition in a column at the side to ensure the place value is maintained. When children are working with numbers where they can confidently and correctly calculate the addition mentally, they may do so.

 $13 \times 8$ 

×	10	3
8	80	24

#### **Y**4

## **End of Year Objective:**

Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.

By the end of the year, they will extend their use of the grid method to be able to multiply three-digit numbers by a single digit number, e.g.

 $346 \times 8$ 

x	300	40	6
8	2400	320	48

#### **Y5**

## **End of Year Objective:**

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers.

Children should continue to use the grid method and extend it to multiplying numbers with up to four digits by a single digit number, e.g.

 $4346 \times 8$ 

x	4 000	300	40	6
8	32 000	2400	320	48

and numbers with up to four digits by a two-digit number, e.g.

 $2693 \times 24$ 

×	2000	600	90	3
20	40000	12000	1800	60
4	8000	2400	360	12

The long list of numbers in the addition part can be used to check that all of the answers from the grid have been included, however, when children are working with numbers where they can confidently and correctly calculate the addition (or parts of the addition) mentally, they should be encouraged to do so. For example,

x	2000	600	90	3	
20	40000	12000	1800	60	= 53 860
4	8000	2400	360	12	= 10 772 +
					64 632

During Year 5, the transition from the grid method into the formal vertical method for multiplication can take place when the children are ready. It is most effective to begin with the grid method, moving to an expanded vertical layout, before introducing the compact form. This allows children to see, and understand, how the processes relate to each other and where the individual multiplication answers come from e.g.  $368 \times 6$ 

becomes

Which can then become

Long multiplication could also be introduced by comparing the grid method with the compact vertical method. Mentally totalling each row of answers is an important step in children making the link between the grid method and the compact method.

x	600	90	3		1 1	
20	12000	1800	60	=	13 860	
4	2400	360	12	=	2 772	+
					16 632	

Children should only be expected to move towards this next method if they have a secure understanding of place value.

2 7 7 2 (693 x 4)

 $(693 \times 20)$ 

When using the compact method for long multiplication, all carried digits should be placed below the line of that answer e.g.  $3 \times 4$  is 12, so the 2 is written in the units column and the 10 is carried as a small 1 in the tens column.

This carrying below the answer is in line with the written addition policy in which carried digits are always written below the answer/line.

#### YEAR 6

## **End of Year Objective:**

Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.

Multiply one-digit numbers with up to two decimal places by whole

By the end of year 6, children should be able to use the grid method to multiply any number by a two-digit number. They could also develop the method to be able to multiply decimal numbers with up to two decimal places, but having been introduced to expanded and compact vertical methods in Year 5, it may be appropriate to use the expanded vertical method when introducing multiplication involving decimals.

 $4.92 \times 3$ 

T U . t h  
4 . 9 2  

$$\times$$
 3  
0 . 0 6 (0.02 x 3)  
2 . 7 (0.9 x 3)  
+ 1 2  
1 4 . 7 6

# **Progression Towards a Written Method for Division**

In developing a written method for division, it is important that children understand the concept of division, in that it is:

• repeated subtraction

They also need to understand and work with certain principles, i.e. that it is:

- the inverse of multiplication
- not commutative i.e. 15 ÷3 is not the same as 3 ÷ 15
- not associative i.e.  $30 \div (5 \div 2)$  is not the same as  $(30 \div 5) \div 2$

#### YR

#### **Early Learning Goal:**

Children solve problems, including halving and sharing.

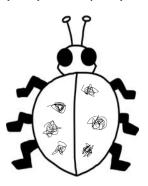
Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of equipment, including small world play, role play, counters, cubes etc.

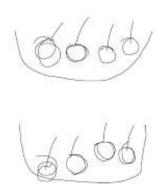
Children may also investigate sharing items or putting items into groups using items such as egg boxes, ice cube trays and baking tins which are arrays.





They may develop ways of recording calculations using pictures, etc.





#### YEAR I

#### **End of Year Objective:**

Solve one-step problems involving division by calculating the answer using concrete objects, pictorial representations and arrays with the support of the

In year one, children will continue to solve division problems using practical equipment and jottings. They should use the equipment to share objects and separate them into groups.

#### YEAR 2

## **End of Year Objective:**

Calculate mathematical statements for division within the multiplication tables and write them using the division  $(\div)$  and equals (=) signs.

Children will utilise practical equipment to represent division calculations as grouping (repeated subtraction) and use jottings to support their calculation, e.g.

 $12 \div 3 =$ 



Children need to understand that this calculation reads as 'How many groups of 3 are there in 12?'

Children should also continue to develop their knowledge of division with remainders, e.g.

 $13 \div 4 =$ 



 $13 \div 4 = 3$  remainder I

#### YEAR 3

#### **End of Year Objective:**

Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers divided by one-digit numbers, progressing to formal written methods.\*

Initially, children will continue to use division by grouping including those with remainders).

e.g.

43 ÷ 8 =

# 

 $43 \div 8 = 5$  remainder 3

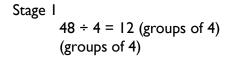
In preparation for developing the 'chunking' method of division, children should first use the repeated subtraction on a vertical number line alongside the continued use of practical equipment. There are two stages to this:

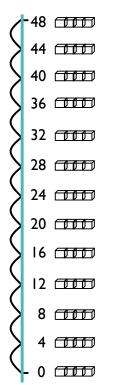
Stage I – repeatedly subtracting individual groups of the divisor

Stage 2 – subtracting multiples of the divisor (initially 10 groups and individual groups, then 10 groups

and other multiples in line with tables knowledge)

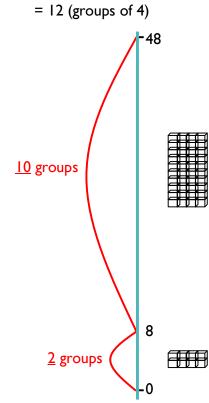
After each group has been subtracted, children should consider how many are left to enable them to identify the amount remaining on the number line.





Stage 2  

$$48 \div 4 = 10 \text{ (groups of 4)} + 2$$
  
 $= 12 \text{ (groups of 4)}$ 

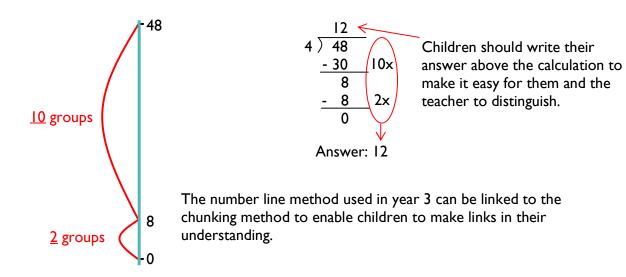


#### YEAR 4

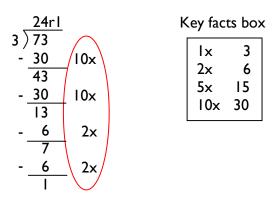
## **End of Year Objective:**

Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Children will continue to develop their use of grouping (repeated subtraction) to be able to subtract multiples of the divisor, moving on to the use of the 'chunking' method.

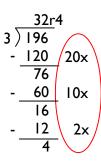


When developing their understanding of 'chunking', children should utilise a 'key facts' box, as shown below. This enables an efficient recall of tables facts and will help them in identifying the largest group they can subtract in one chunk. Any remainders should be shown as integers, e.g.



By the end of year 4, children should be able to use the chunking method to divide a three digit number by a single digit number. To make this method more efficient, the key facts in the menu box should be extended to include 4x and 20x, e.g.

196 ÷ 6



Key facts box

lx	6
2x	12
4x	24
5x	30
I0x	60
20x	120

#### YEAR 5

## **End of Year Objective:**

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Children may continue to use the key facts box for as long as they find it useful. Using their knowledge of linked tables facts, children should be encouraged to use higher multiples of the divisor. During Year 5, children should be encouraged to be efficient when using the chunking method and not have any subtraction steps that repeat a previous step. For example, when performing  $347 \div 8$  an initial subtraction of  $160 (20 \times 8)$  and a further subtraction of  $160 (20 \times 8)$  should be changed to a single subtraction of  $320 (40 \times 8)$ . Also, any remainders should be shown as integers, e.g.

523 ÷ 8

By the end of year 5, children should be able to use the chunking method to divide a four digit number by a single digit number. If children still need to use the key facts box, it can be extended to include 100x.

 $2458 \div 7$ 

#### YEAR 6

#### **End of Year Objective:**

Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.

Use written division methods in cases where the answer has up to two decimal

To develop the chunking method further, it should be extended to include dividing a four-digit number by a two-digit number, e.g.  $6367 \div 28$ 

Children with understanding may start to use short division (when dividing by number up to 9 only)

Children will also be shown how to record remainders as decimals.

This should first be demonstrated using a simple calculation such as  $13 \div 4$  to show the remainder initially as a fraction.



Using practical equipment, children can see that for  $13 \div 4$ , the answer is 3 remainder I, or put another way, there are three whole groups and a remainder of I. This remainder is one part towards a full group of 4, so is  $\frac{1}{4}$ . To show the remainder as a fraction, it becomes the numerator where the denominator is the divisor (the number that you are dividing by in the calculation).

 $3574 \div 8$ 

8) 
$$3574$$

-  $3200$ 
 $\overline{574}$ 

-  $\underline{560}$ 

14

-  $\underline{8}$ 

So  $3574 \div 8$  is  $471\frac{6}{8}$ 

(when the remainder is shown as a fraction)

To show the remainder as a decimal relies upon children's knowledge of decimal fraction equivalents. For decimals with no more than 2 decimal places, they should be able to identify:

Half: 
$$\frac{1}{2} = 0.5$$

Quarters: 
$$\frac{1}{4} = 0.25$$
,  $\frac{8}{4} = 0.75$ 

Fifths: 
$$\frac{1}{5} = 0.2$$
,  $\frac{2}{5} = 0.4$ ,  $\frac{3}{5} = 0.6$ ,  $\frac{4}{5} = 0.8$ 

Tenths: 
$$\frac{1}{10} = 0.1$$
,  $\frac{2}{10} = 0.2$ ,  $\frac{3}{10} = 0.3$ ,  $\frac{4}{10} = 0.4$ ,  $\frac{5}{10} = 0.5$ ,  $\frac{6}{10} = 0.6$ ,  $\frac{7}{10} = 0.7$ ,  $\frac{8}{10} = 0.8$ ,  $\frac{9}{10} = 0.9$ 

and reduce other equivalent fractions to their lowest terms.

In the example above,  $3574 \div 8$ , children should be able to identify that the remainder as a fraction of  $\frac{6}{8}$  can be written as  $\frac{3}{4}$  in its lowest terms. As  $\frac{3}{4}$  is equivalent to 0.75, the answer can therefore be written as 471.75.

#### **Summary**

\*Although the objective suggests that children should be using formal written methods, the National Curriculum document states "The programmes of study for mathematics are set out year-by-year for key stages I and 2. Schools are, however, only required to teach the relevant programme of study by the end of the key stage. Within each key stage, schools therefore have the flexibility to introduce content earlier or later than set out in the programme of study." p4

It is more beneficial for children's understanding to go through the expanded methods of calculation as steps of development towards a formal written method.

Children should be encouraged to:

- Estimate first
- Check the answer, preferably using a different method e.g. the inverse operation
- Decide first whether a mental method is appropriate
- Pay attention to language and refer to the actual value of digits. (e.g. 5 ones/units, 6 tens)
- Children who make persistent mistakes should return to the method that they can use accurately until ready to move on.
- Children need to know number and multiplication facts by heart.
- Discuss errors and diagnose the problem, then work through problem. Do not simply reteach the method.
  - Children should not be made to go onto the next stage if:
    - I) they are not ready.
    - 2) they are not confident.
  - Children should be encouraged to consider if a mental calculation would be appropriate before using written methods.

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